

# New challenges in adaptive real-time systems with parametric WCET

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# Outline

- 1 Introduction
- 2 Automated parametric WCET analysis
- 3 Open problems for adaptive real-time systems

# Parametric WCET analysis

- Classical WCET analysis:
  - Compute a **single numeric value**;
  - Upper-bound for all software/hardware parameter combinations;
  - Often largely pessimistic;
- Parametric WCET analysis:
  - Compute a **formula** of software/hardware parameters;
  - **Instantiate** formula when parameter values become known.

# Example

## WCET variability

```
void f(int a){  
    // 10  
    if(a > 0)  
        // 15  
    else  
        // 5  
    //10  
}
```

$$WCET = 10 + \max(15, 5) + 10 = 35$$

# Example

## WCET variability

```
void f(int a){  
    // 10  
    if(a > 0)  
        // 15  
    else  
        // 5  
    //10  
}
```

$$WCET = \begin{cases} 10 + 15 + 10 = 35 & \text{if } a > 0 \\ 10 + 5 + 10 = 25 & \text{otherwise} \end{cases}$$

# Contribution

- Comparison with other parametric WCET approaches:
  - More parameter kinds;
  - Adaptive;
  - Embeddable;
  - Automated.
- **Applications:**
  - Off-line instantiation: parameter-space exploration;
  - On-line instantiation: adaptive system.

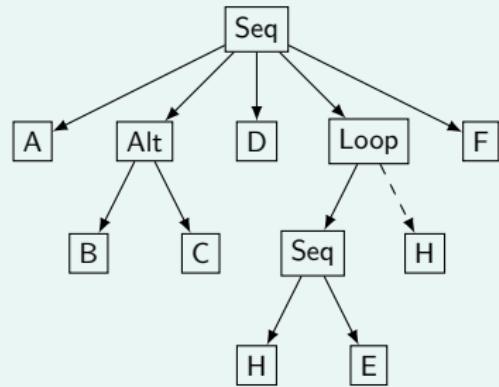
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# Tree-based WCET

## Control-Flow Tree

```
void f(int a, int b){
    // A
    if(a > 0)
        // B
    else
        // C
    // D
    for(int i=0; i<a+b; i++) // H
        // E
    // F
}
```



Compute WCET recursively on the tree:

- *Seq* = addition;
- *Alt* = max;
- *Loop* = multiply by max iterations.

# Problem: context-dependent WCET

- Execution time of a node often depends on its execution context;
- Easily represented in IPET (more ILP constraints);
- Not captured by the tree structure.

## Example: first-miss

Cache timing effect when iterating a node:

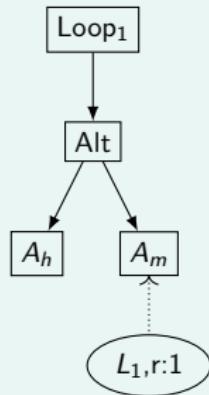
- Miss on first iteration  $\Rightarrow$  higher execution time
- Hit on other iterations  $\Rightarrow$  lower execution time.

# Context annotations [Ballabriga et al., 2017]

Context annotation  $(L_n, r : n)$ :

- For a complete execution of loop  $L_n \dots$
- ... annotated node is executed at most  $n$  times.

## First-miss



# WCET of a node

Context annotations  $\Rightarrow$  WCET is a list of values:

- Non-increasing order;
- Smallest element implicitly repeated infinitely;
- Specify which loop is taken as reference.

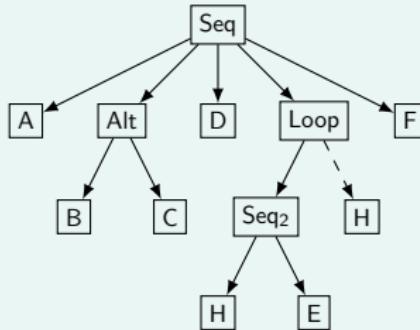
## Cache first-miss

- Assume:
  - $\omega(A_m) = (L_1, [25])$
  - $\omega(A_h) = (L_1, [15])$
  - $A_m$  annotated with  $(L_1, r : 1)$ ;
- Then:
  - $\omega(Alt(A_h, A_m)) = (L_1, [25, 15])$
  - When iterating inside  $L_1$ , WCET is 25, 15, 15, 15, ...

# WCET computation

- WCET formula computed inductively on the tree structure;
- Operations on WCET lists:
  - $w_1 \oplus w_2$ : point-wise sum;
  - $w_1 \uplus w_2$ : list union;
  - $w^n$ : sum values of  $w$  by packs of  $n$ .

## WCET formula

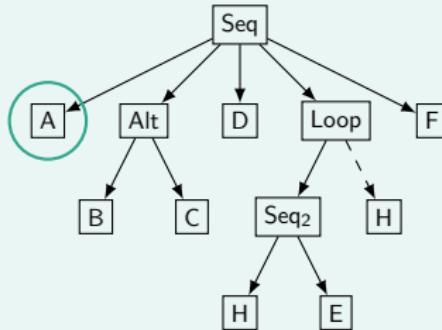


$$\omega(\text{Seq}) =$$

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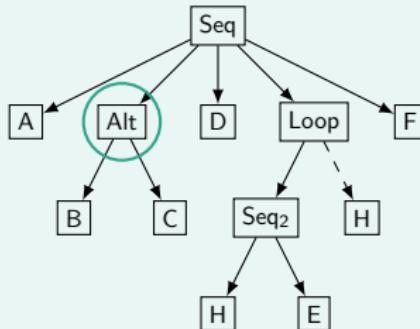


$$\begin{aligned}\omega(\text{Seq}) = \\ \omega(A)\end{aligned}$$

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## WCET formula



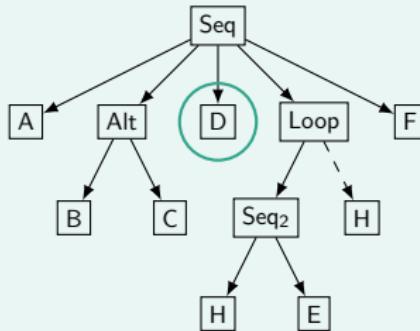
$$\omega(\text{Seq}) =$$

$$\omega(A) \oplus (\omega(B) \uplus \omega(C))$$

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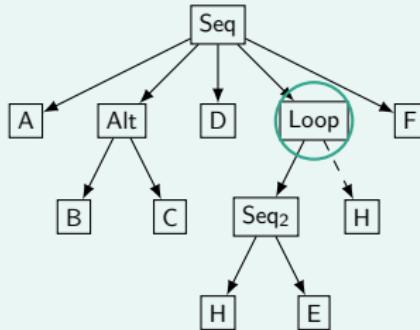
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$$\omega(A) \oplus (\omega(B) \uplus \omega(C)) \oplus \omega(D)$$

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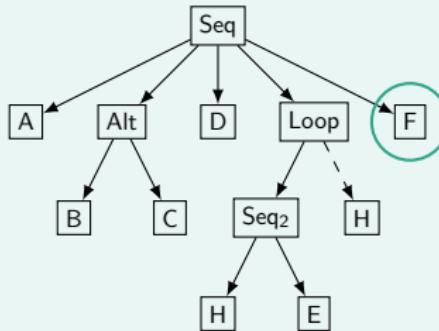
$$\omega(\text{Seq}) =$$

$$\omega(A) \oplus (\omega(B) \uplus \omega(C)) \oplus \omega(D) \oplus (\omega(H) \oplus \omega(E))^n \oplus \omega(H)$$

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## WCET formula



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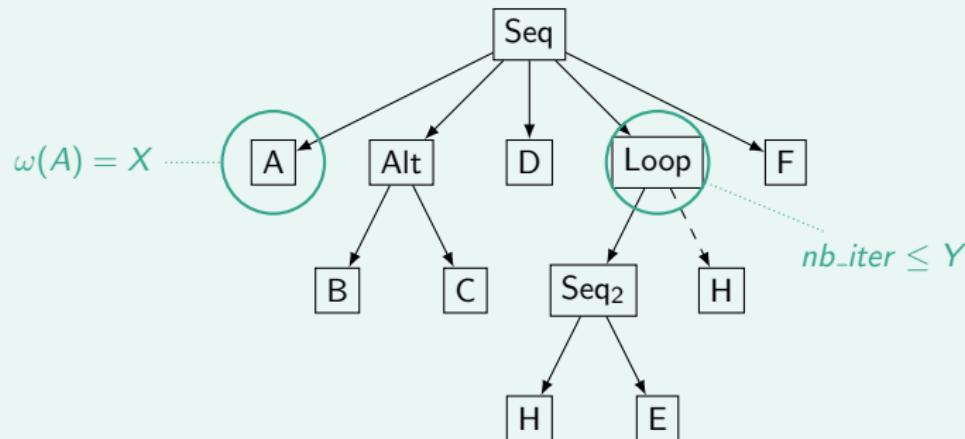
$$\omega(A) \oplus (\omega(B) \uplus \omega(C)) \oplus \omega(D) \oplus (\omega(H) \oplus \omega(E))^n \oplus \omega(H) \oplus \omega(F)$$

# Symbolic values

Some elements of the CFT can be unknown, a.k.a symbolic:

- Node with a symbolic WCET;
- Symbolic loop bounds.

## CFT with parameters



# Procedure arguments as parameters [Grebant et al., 2023]

Step 1: Infer branch conditions by **relational** abstract interpretation.

## Inferring input conditionals

```
f:                                     @ void f(int a, int b){  
@ ...  
str r0, [fp, #-16] @ // r0 contains arg1  
str r1, [fp, #-20] @ // r1 contains arg2  
@ ...  
ldr r3, [fp, #-16] @  
cmp r3, #0 @  
ble .L2 @ if(a > 0) {  
@ ...  
b .L3 @ }  
.L2: @ else {  
@ ...  
.L3: @ }  
@ ... @ // ...
```

# Procedure arguments as parameters [Grebant et al., 2023]

Step 1: Infer branch conditions by **relational** abstract interpretation.

## Inferring input conditionals

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ldr r3, [fp, #-16] @
cmp r3, #0          @ ▷ Test on arg1
ble .L2             @ if(a > 0) { ▷ not obvious in assembly
@ ...
b .L3               @ }
.L2:                         @ else {
@ ...
.L3:                         @ }
@ ...                                     @ // ...
```

# Procedure arguments as parameters [Grebant et al., 2023]

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ble .L2             @ if(a > 0) { ▷ not obvious in assembly
@ ...               @ ▷ "then" condition: arg1 > 0
b .L3               @ }
.L2:                                @ else {
@ ...
.L3:                                @ }
@ ...                                     @ // ...

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# Procedure arguments as parameters [Grebant et al., 2023]

Step 1: Infer branch conditions by **relational** abstract interpretation.

## Inferring input conditionals

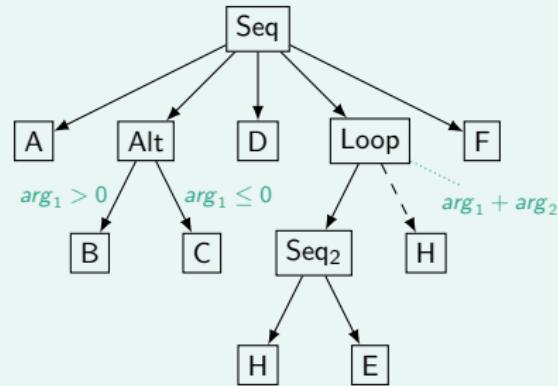
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cmp r3, #0                                @ ▷ Test on arg1
ble .L2                                    @ if(a > 0) { ▷ not obvious in assembly
@ ...                                     @ ▷ "then" condition: arg1 > 0
b .L3                                     @ }
.L2:                                     @ else {
@ ...                                     @ ▷ "else" condition: arg1 ≤ 0
.L3:                                     @ }
@ ...                                     @ // ...
}
```

# Procedure arguments as parameters

Step2: Insert AI results in the CFT.

- Condition of an alternative: conjunction of inequations on arguments;
- Loop bound: linear expression on arguments.

## Input conditionals in loops



# Formula simplification

- CFT with symbolic values  $\Rightarrow$  formula not reducible to a WCET list;
- Simplify formula based on algebraic properties:
  - Define custom rewriting rules  $I \mapsto r$ ;
  - Prove  $I \Leftrightarrow r$  for each rule;
  - Repeatedly apply rewriting rules;
- Simplified formula compiled to C code  $\Rightarrow$  on-line instantiation.

## Example

$$\begin{aligned} f &= ((a > 0) \circledast (I, [10, 5])) \uplus ((a \leq 0) \circledast (I, [10, 5])) \\ &= (I, [10, 5]) \quad (\text{Since } a > 0 \Leftrightarrow \neg(a \leq 0)) \end{aligned}$$

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# Input-dependent WCET formulas

WCET formulas vs other models with several WCET values:

- ① Explicit WCET-to-inputs dependence;
- ② A single input might impact the WCET of several tasks;
- ③ Not an obvious number of different WCET values for a task.

# Open problem 1

## Sensitivity analysis

Which input values make a task set schedulable?

Main difficulty:

(2) A single input might impact the WCET of several tasks.

# Open problem 2

## Semi-clairvoyant scheduling

Semi-clairvoyant scheduling of tasks with WCET formulas.

Main difficulty:

(3) **Not an obvious number of different WCET values.**

# Conclusion

Symbolic WCET computation:

- Embeddable;
- Adaptive;
- Automated.

Paving the way for new kinds of adaptive real-time systems?

## Downloads

- Polymalys (AI): <https://gitlab.cristal.univ-lille.fr/otawa-plugins/polymalys>
- WSymb (WCET): <https://gitlab.cristal.univ-lille.fr/otawa-plugins/WSymb>
- RTNS'23 artifact:  
[https://gitlab.cristal.univ-lille.fr/sgrebant/rtns\\_2023\\_artifact](https://gitlab.cristal.univ-lille.fr/sgrebant/rtns_2023_artifact)

# References

[Ballabriga et al., 2017] Ballabriga, C., Forget, J., and Lipari, G. (2017).

Symbolic WCET Computation.

*ACM Transactions on Embedded Computing Systems (TECS)*, 17(2):1 – 26.

[Grebant et al., 2023] Grebant, S., Ballabriga, C., Forget, J., and Lipari, G. (2023).

WCET analysis with procedure arguments as parameters.

In *RTNS 2023: The 31st International Conference on Real-Time Networks and Systems*.