

# Predictable Implementation of Real-Time Applications on Multiprocessor Systems on Chip

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# We want systems to be predictable!



**We want systems to be predictable!**

**Safety critical**



**We want systems to be predictable!**

**QoS should be  
guaranteed!**





## ■ Real-Time:

**Time constraints have to be satisfied!**



**Safe W(B)CETs have to be known**



☞ **Many current/future real-time applications need both**

- **performance**
- **predictability**



- **Strong(er) processors**
- **Multiprocessors on Chip**



☞ Many current/future real-time applications need both

- performance
- predictability



- Strong(er) processors
- Multiprocessors on Chip

Can we still achieve predictability?



- Background
- Hardware Architecture & Application Model
- The Problem and Possible Solutions
- WCET Analysis with TDMA Bus Schedule
- TDMA Bus Scheduling Approaches
- Bus Schedule Generation
- Conclusions

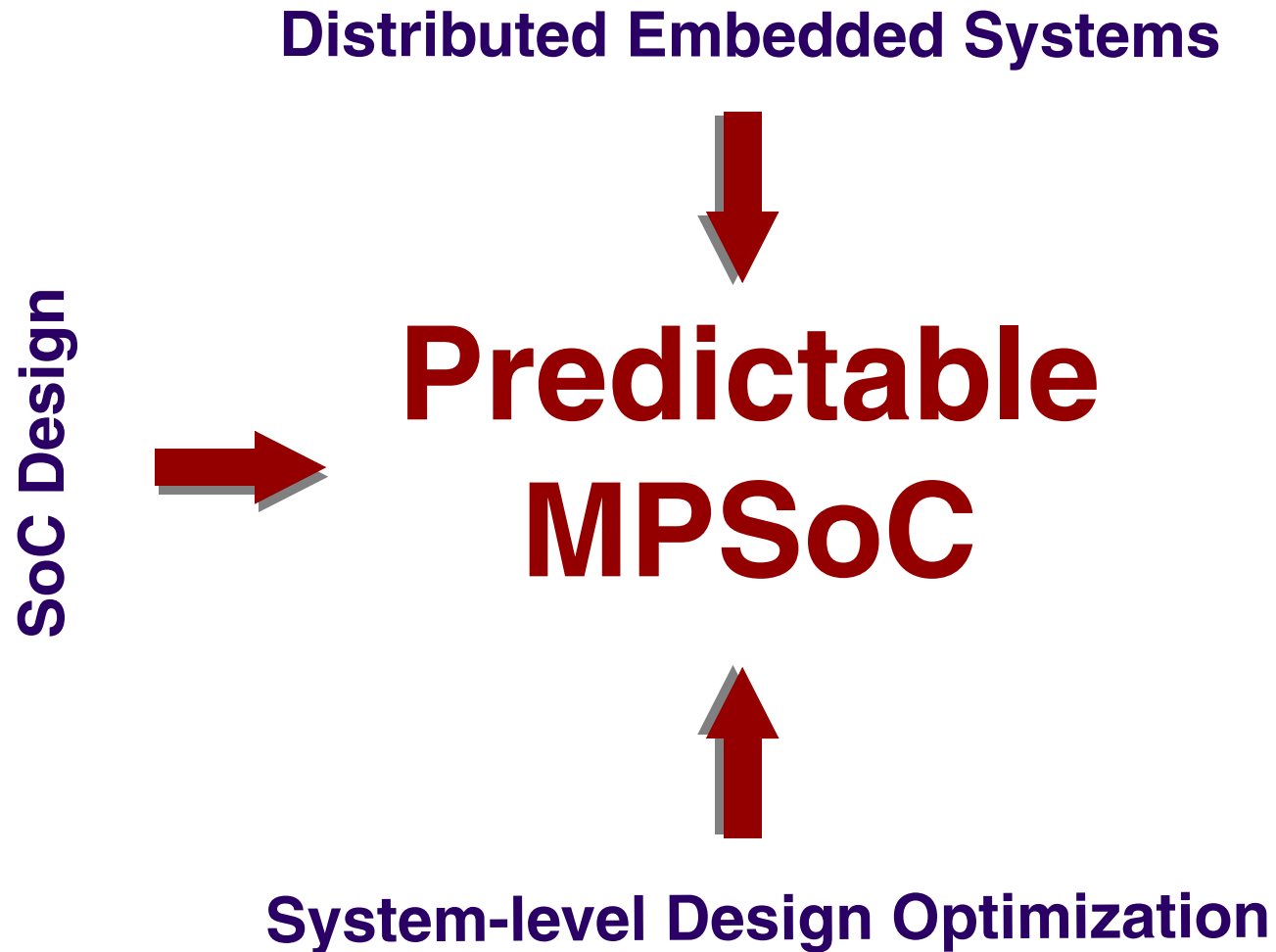




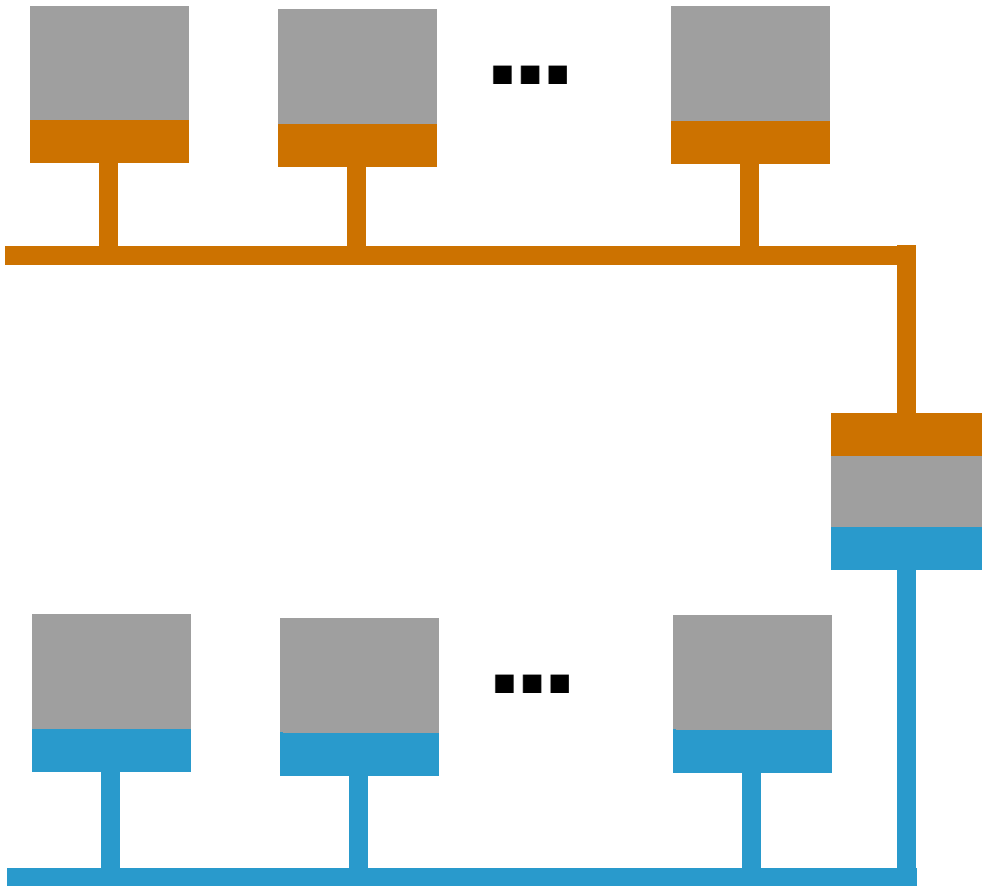
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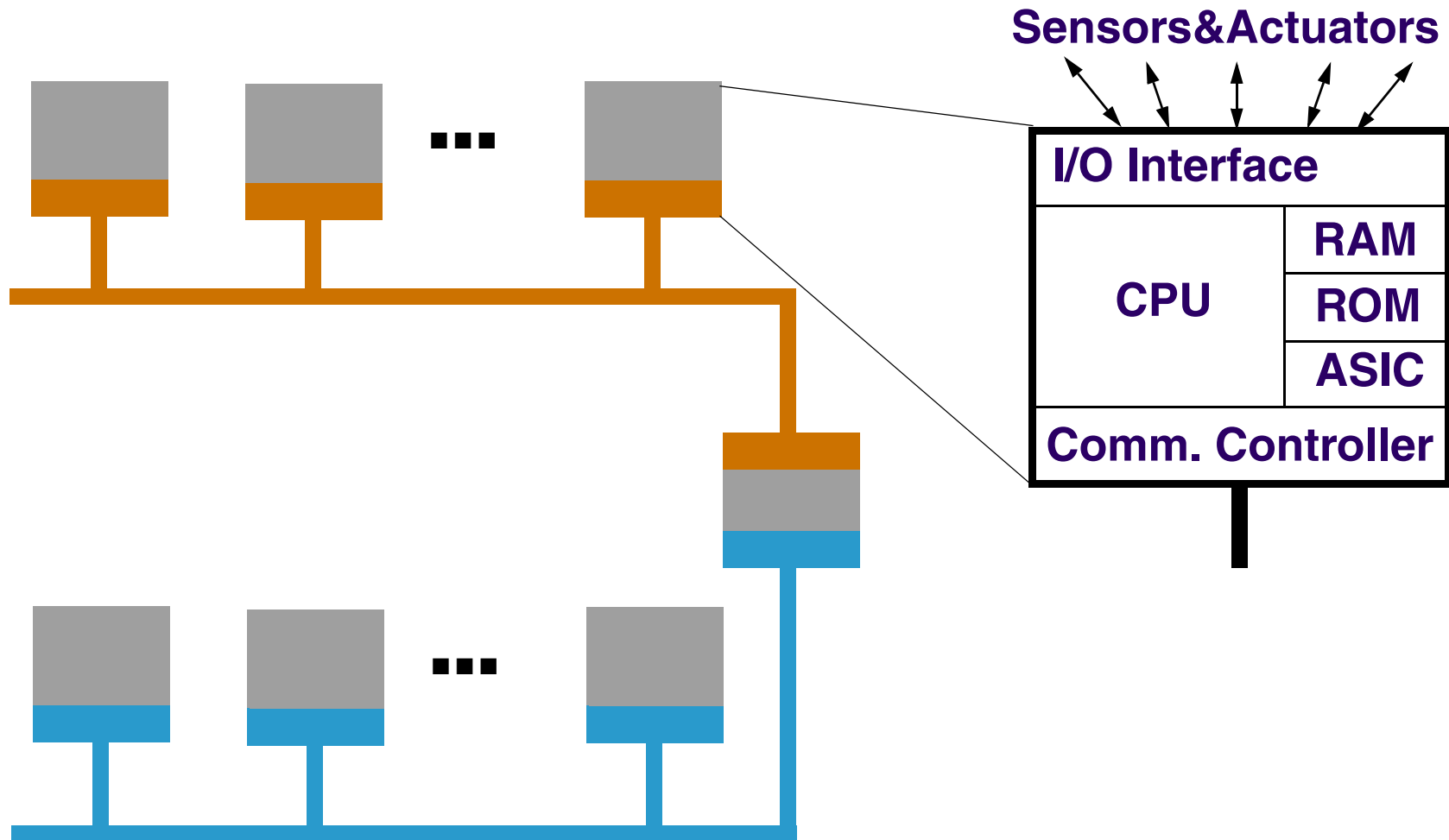
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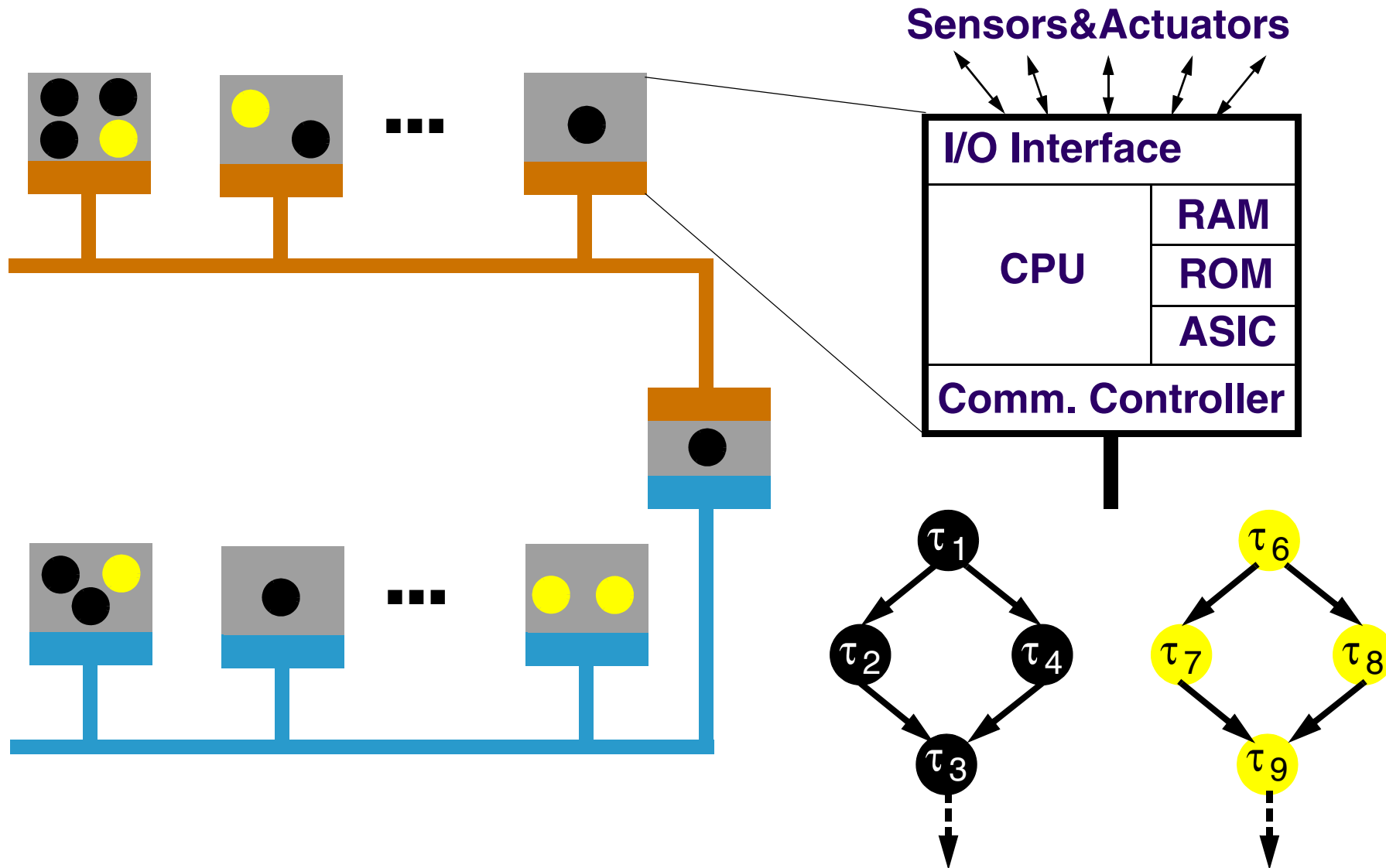
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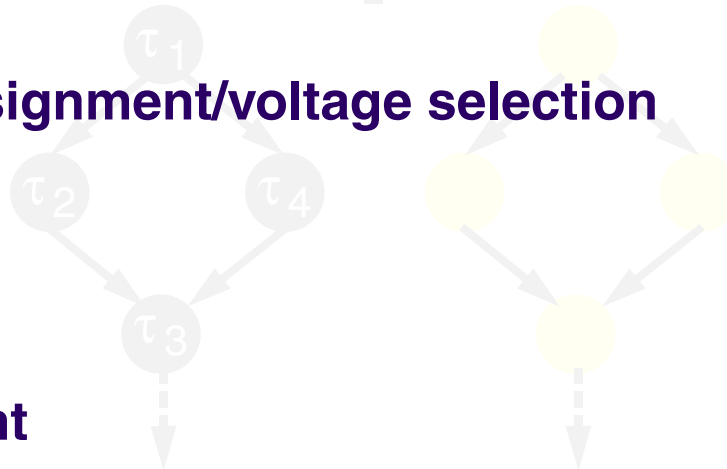
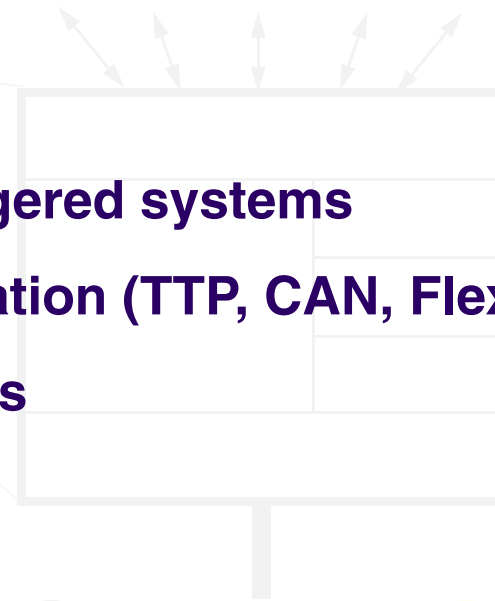


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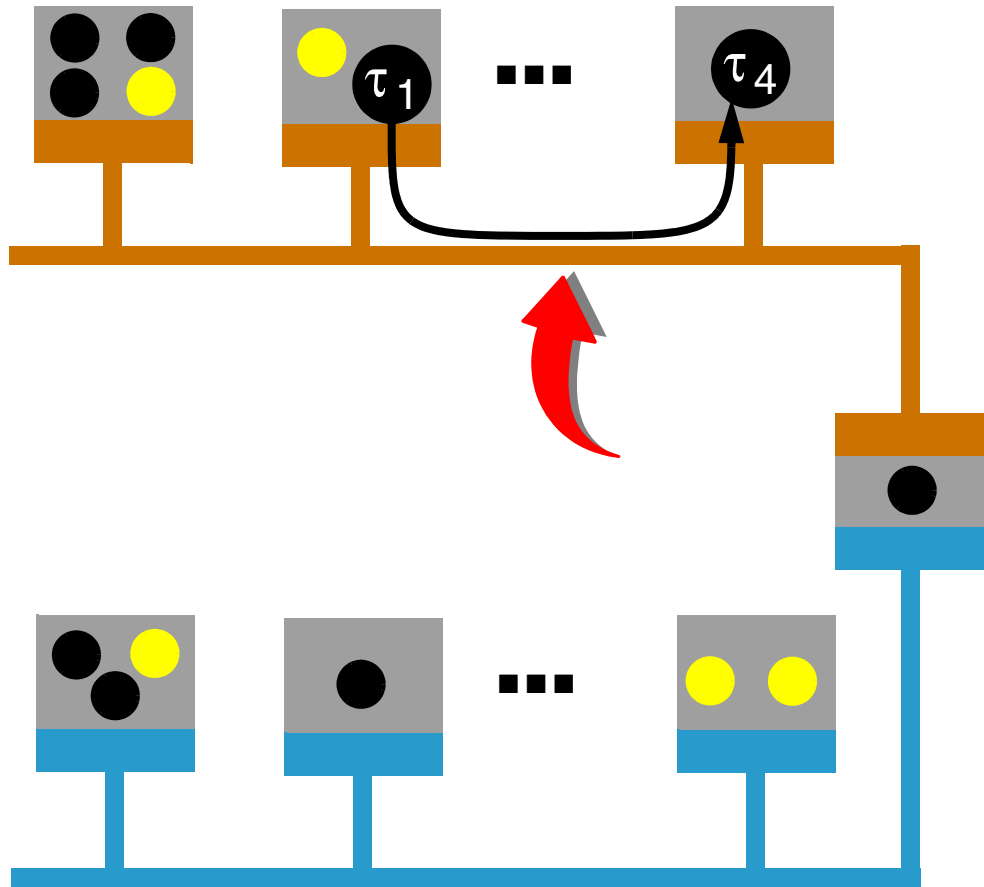


# Distributed Embedded Systems

- Worst-case response time analysis
  - Static-cyclic schedule generation
  - Analysis of heterogeneous time/event triggered systems
  - Static/Dynamic/heterogeneous communication (TTP, CAN, FlexRay)
  - Scheduling with Fault-tolerance constraints
- 
- Optimization problems:
    - schedule generation/priority assignment/voltage selection
    - task mapping
    - bus configuration
    - scheduling policy assignment
    - fault tolerance policy assignment

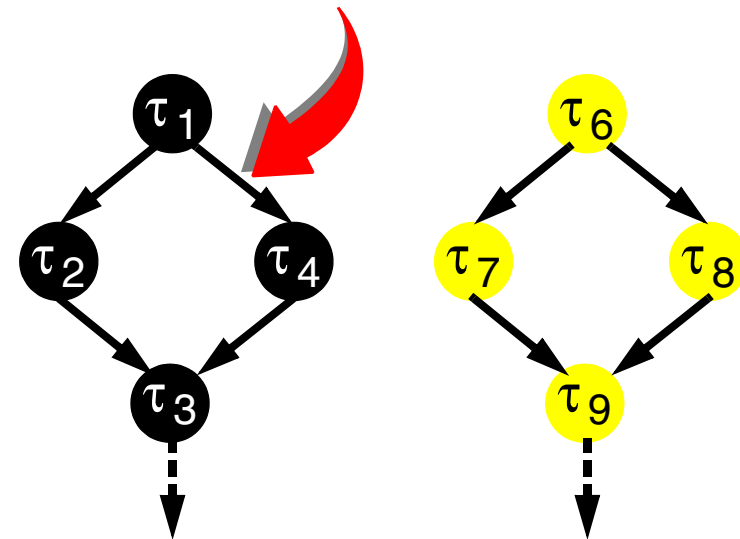


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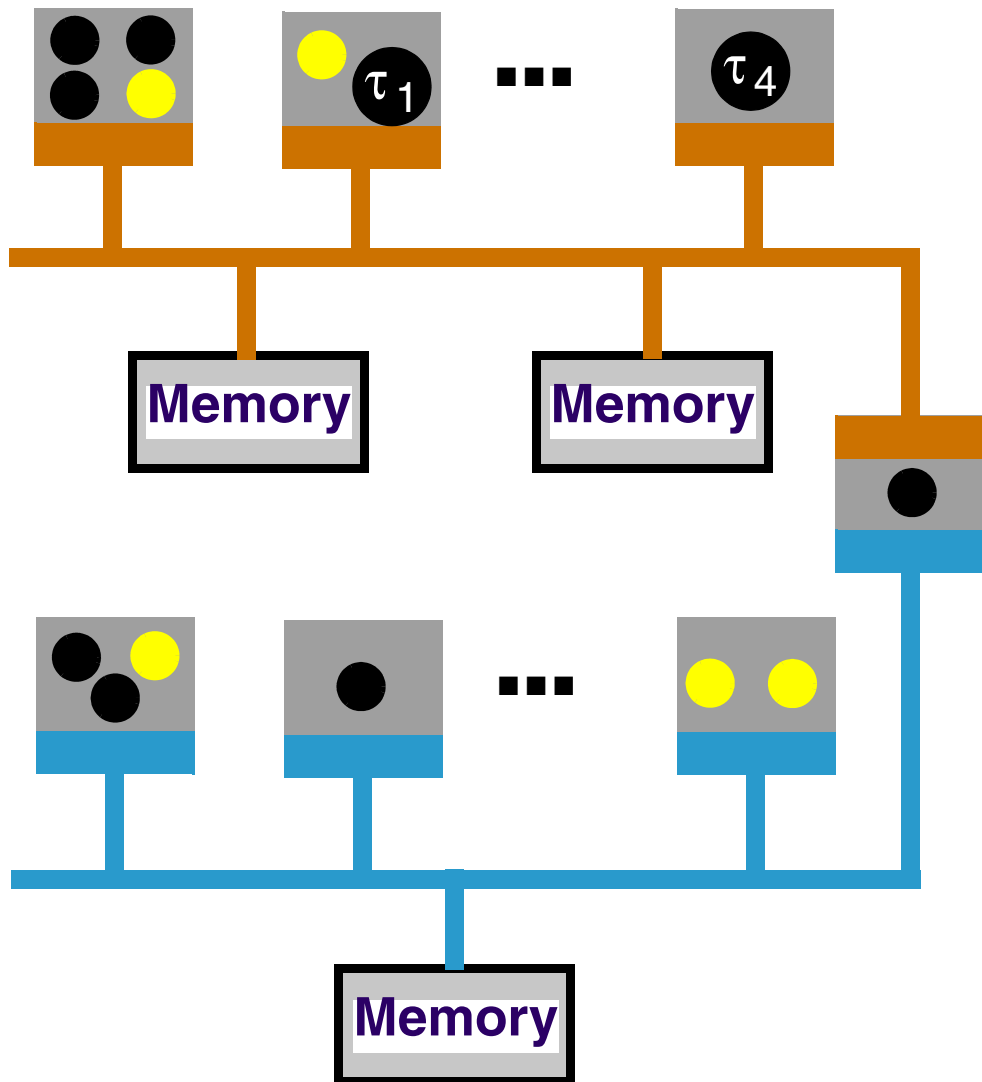


☞ Only message passing between tasks (explicit communication) is going over the shared bus.

☞ Bus sharing has **NO** impact on task WCET.

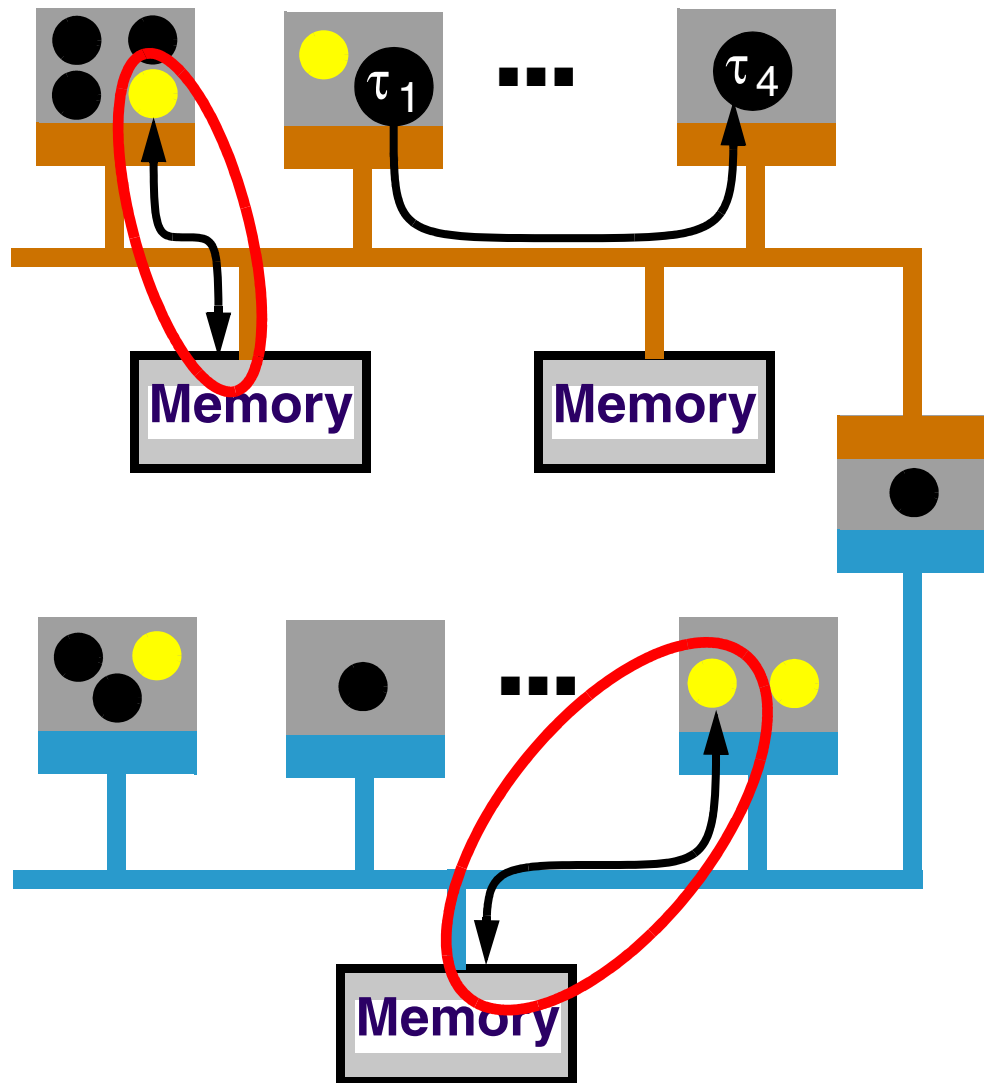


# The MPSoC case





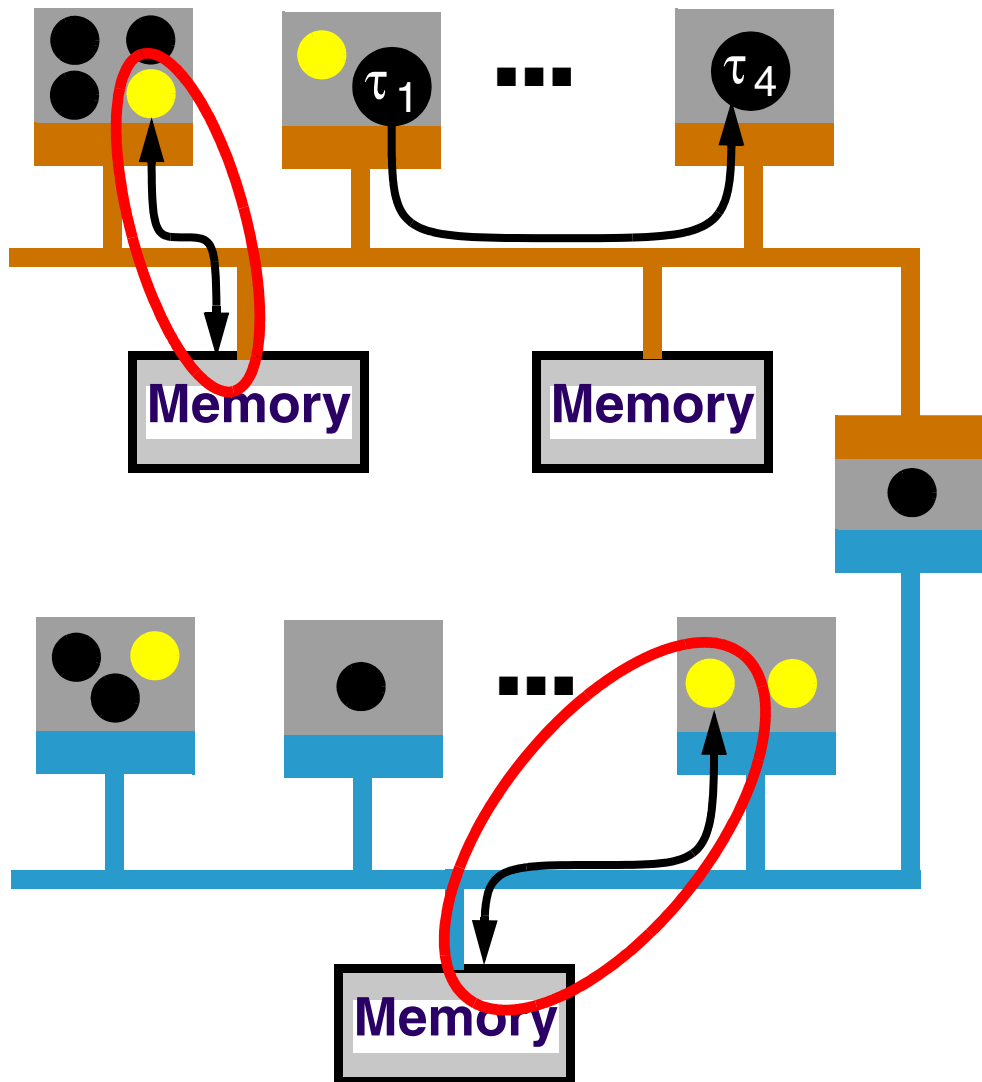
# The MPSoC case



- ➡ Memory accesses (in case of cache miss) are going over the shared bus.
- ➡ **Bus sharing has impact on task WCET!!!**



# The MPSoC case



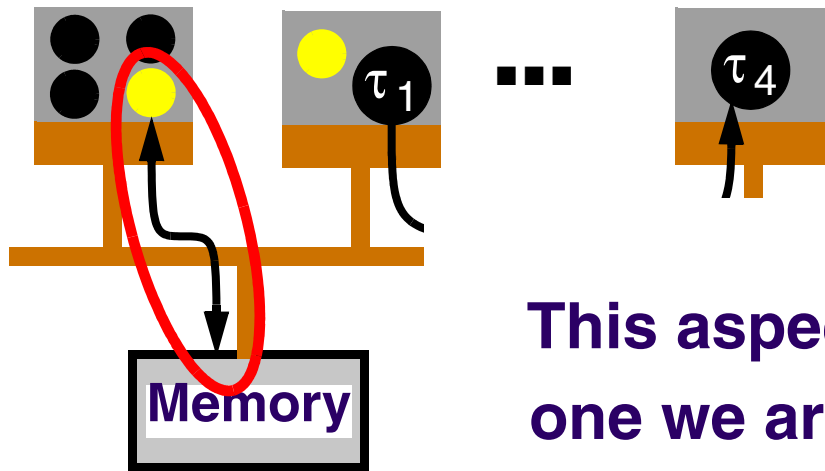
➡ Memory accesses (in case of cache miss) are going over the shared bus.

➡ **Bus sharing has an impact on task WCET!!!**

**You ignore this: Your results are WRONG!**



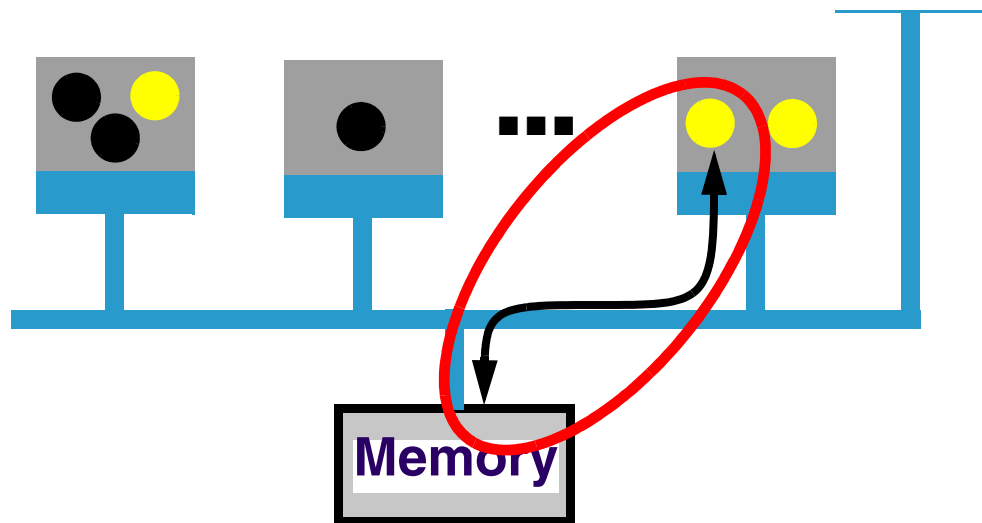
# The MPSoC case



Memory accesses (in case of cache miss) are going over the

This aspect of predictability is the one we are interested in here!

an impact on



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☞ Deriving WCET in the case of a *single processor* is a BIG problem:

- Pipelining
- Cache memory
- Branch prediction
- Out of order execution



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Interference between  
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Execution time depends  
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WCET analysis is

- complex
- potentially pessimistic



☞ Eliminate “problematic” features?



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👉 The player is not allowed to run faster than the referee?!



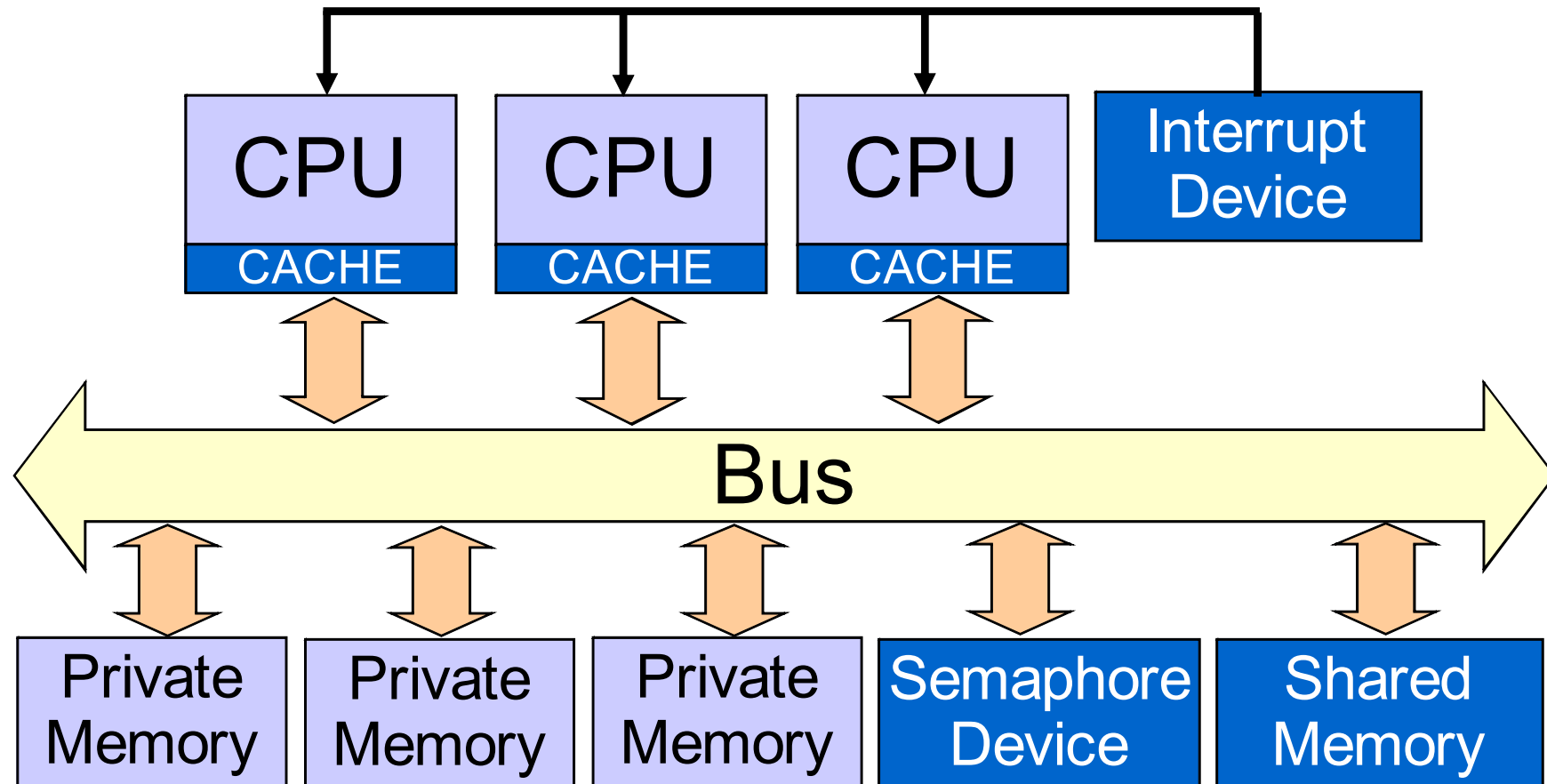




☞ In the case of multiprocessors, on top of all those problems you have:

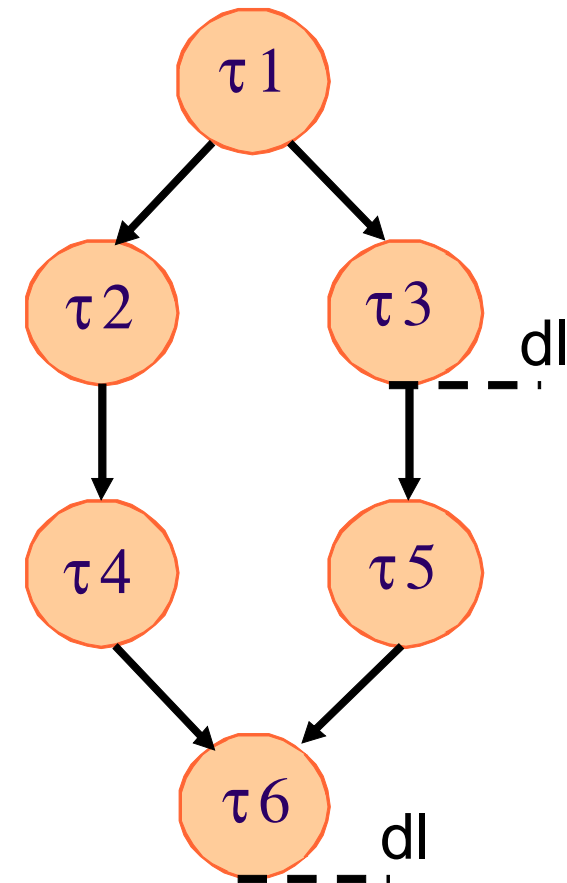
- Interference between active processes
- Additional shared resources (e.g. communication infrastructure)





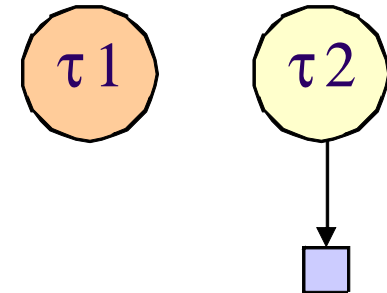
## ■ Task Graph

- Application deadline
- Individual Task deadlines



# An Example

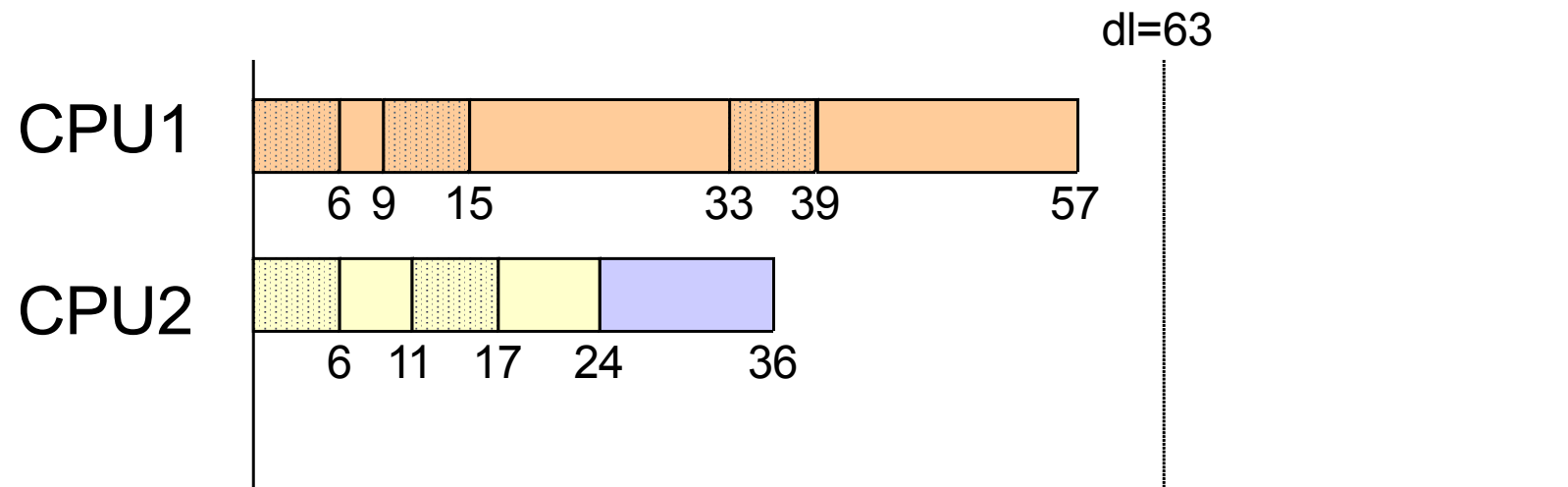
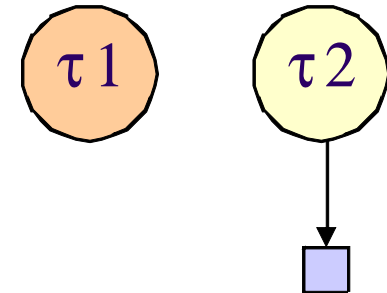
- WCETs - as from “traditional” WCET analysis:
  - $t_1$ : 57
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  - $t_w$ : 12
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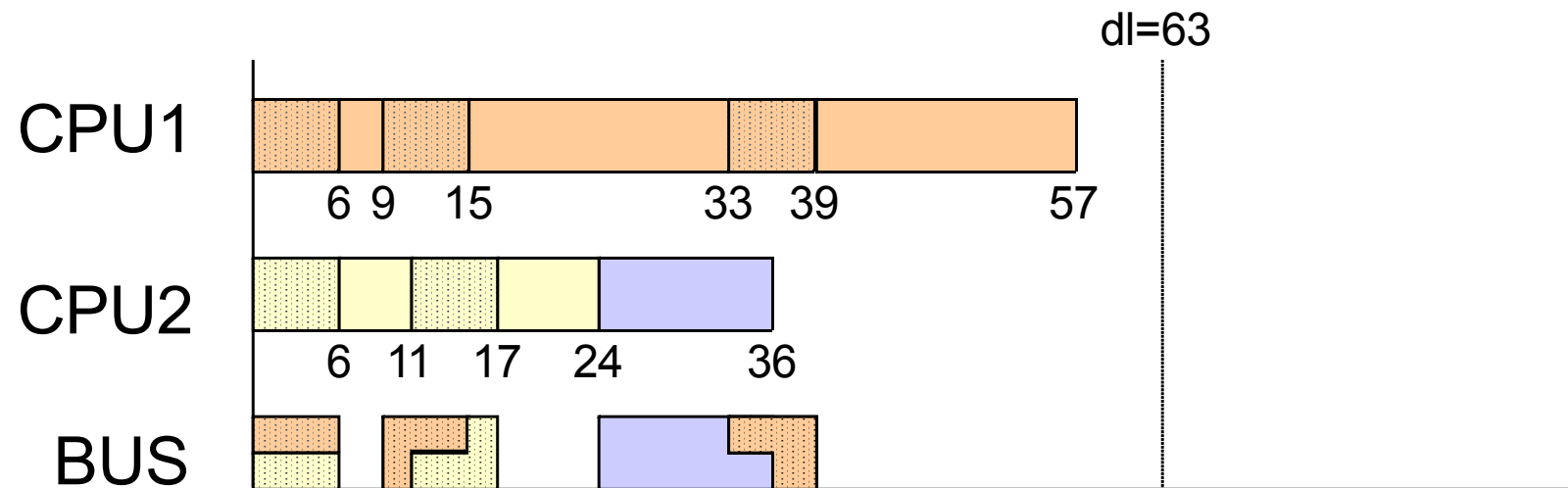
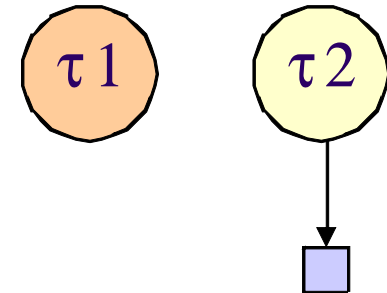
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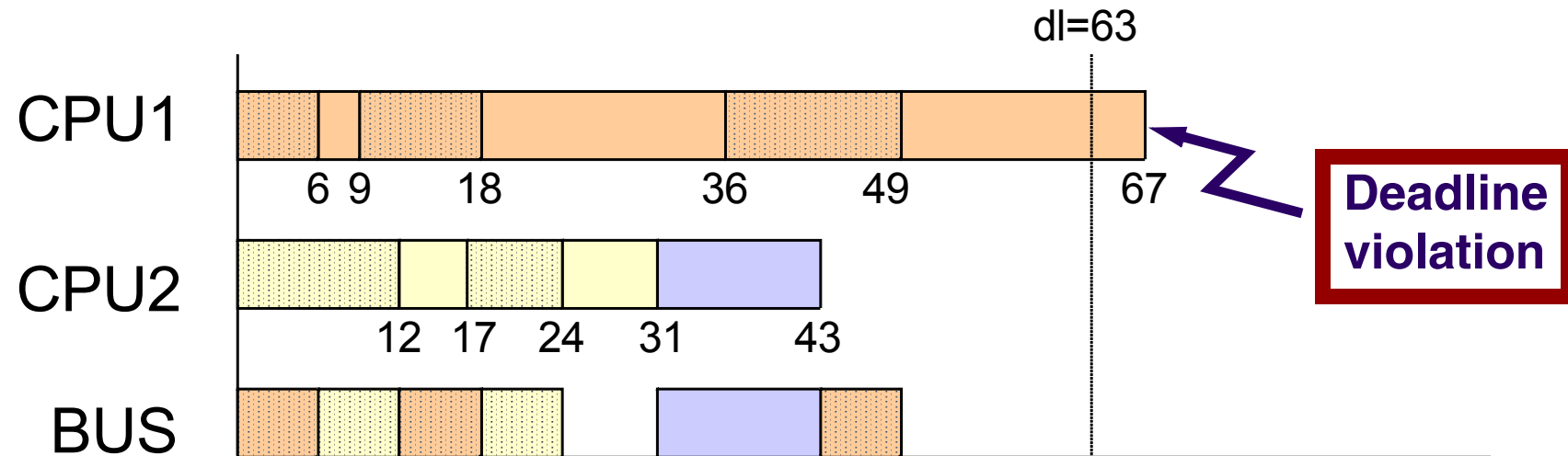
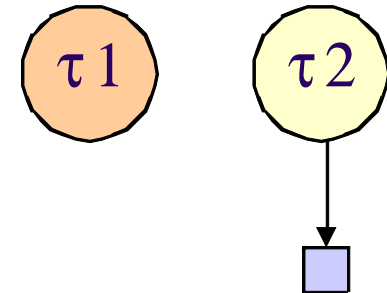
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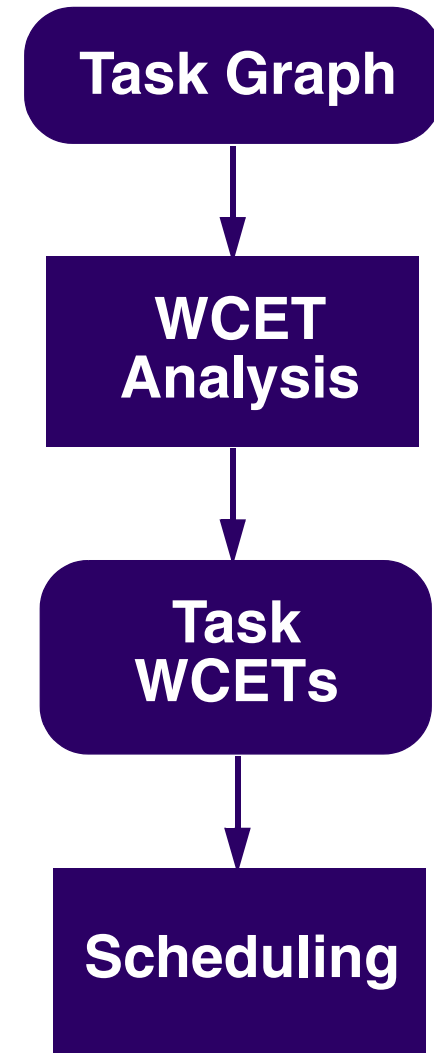
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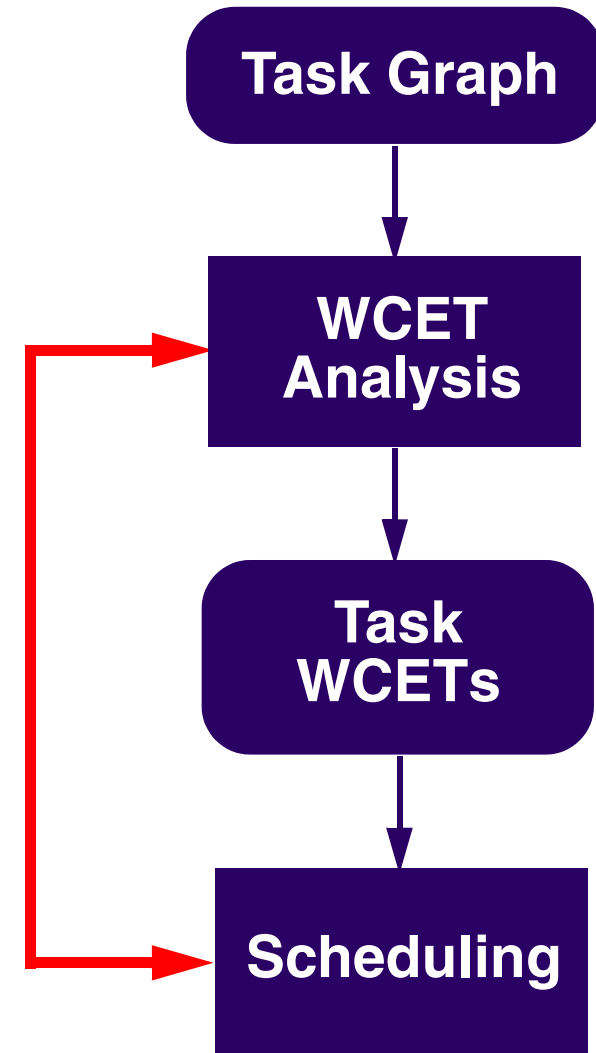
# “Traditional” Approach





# In The Multiprocessor Case

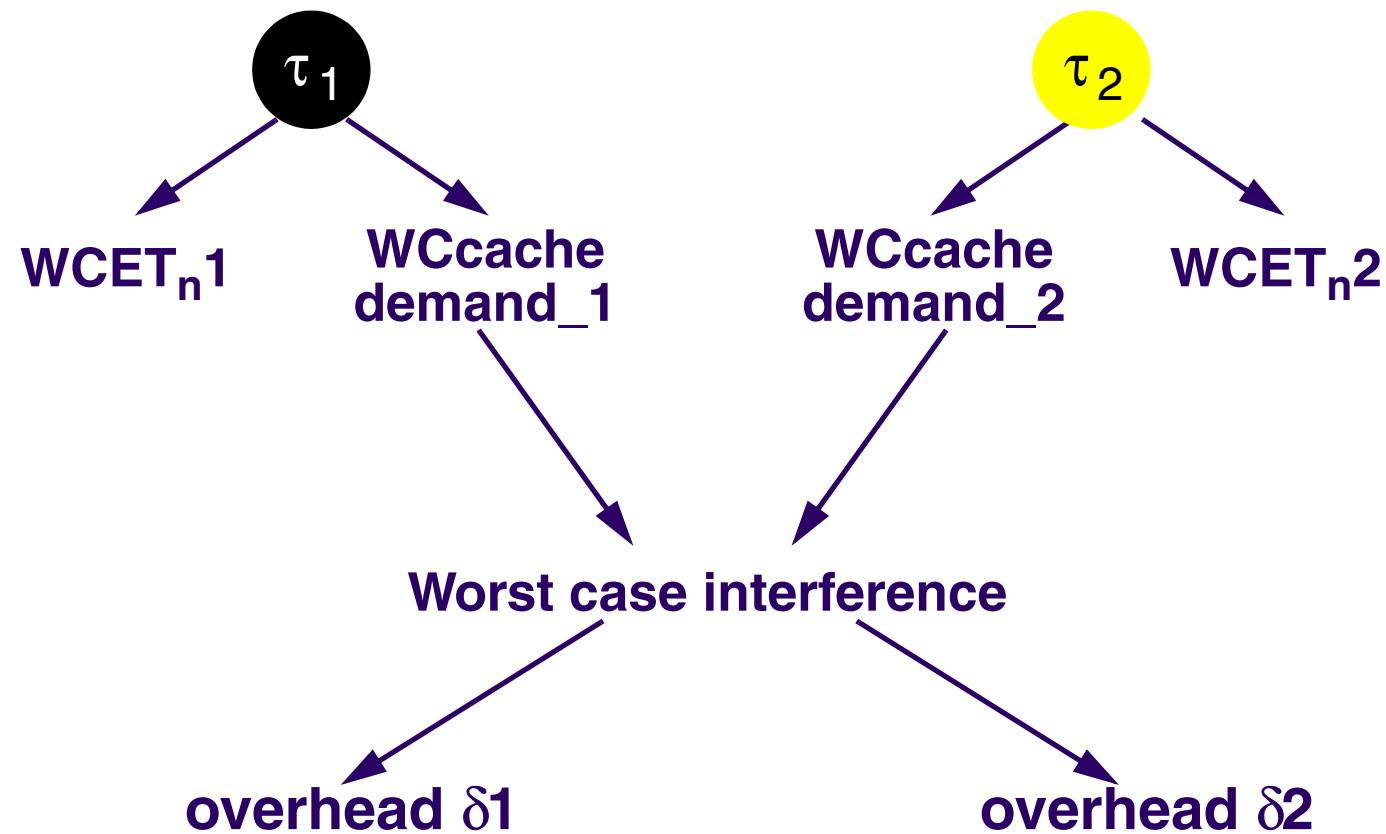
- The WCETs depend on the schedule (interference due to bus conflicts).
- The schedule depends on the WCETs.



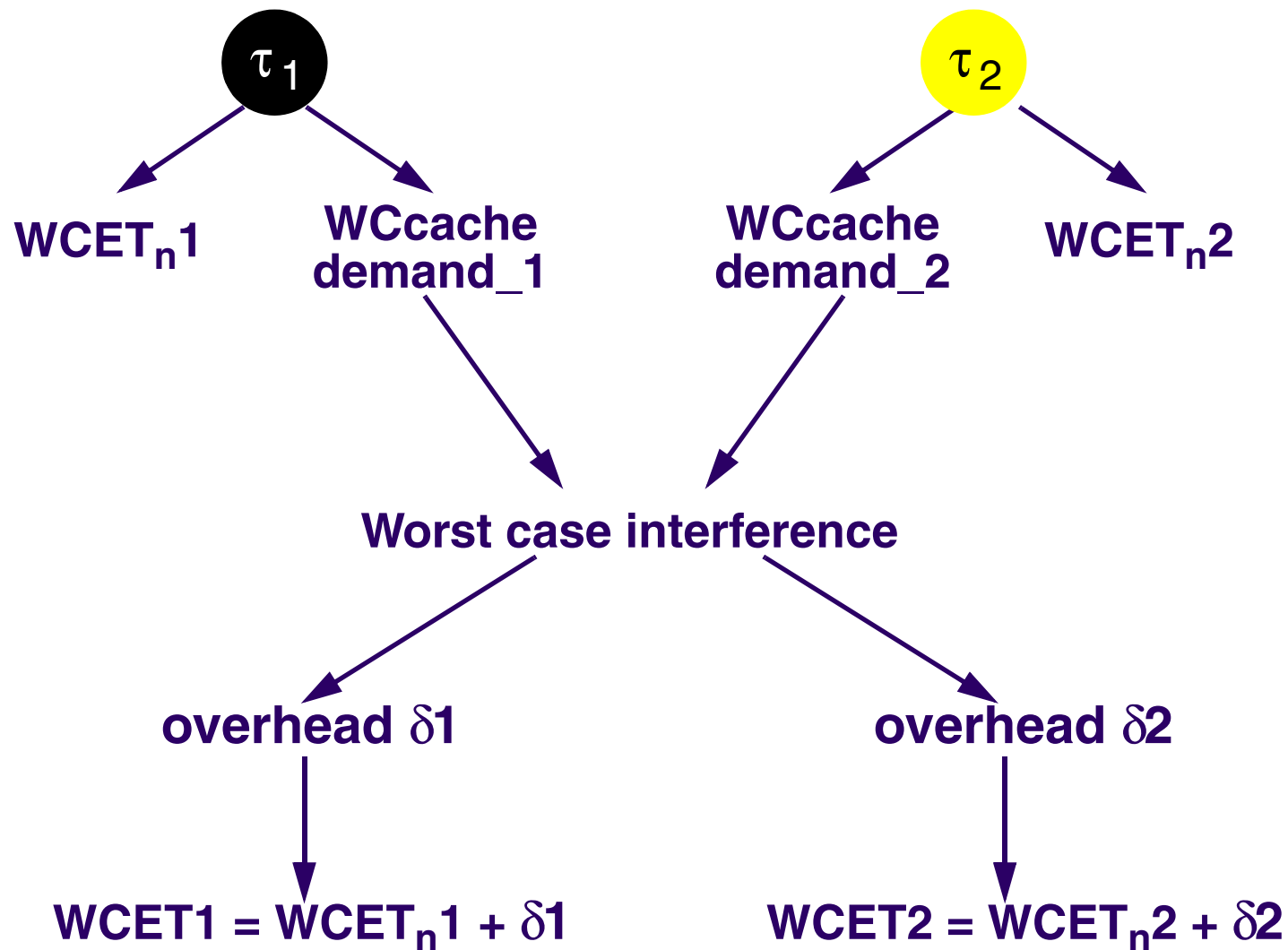
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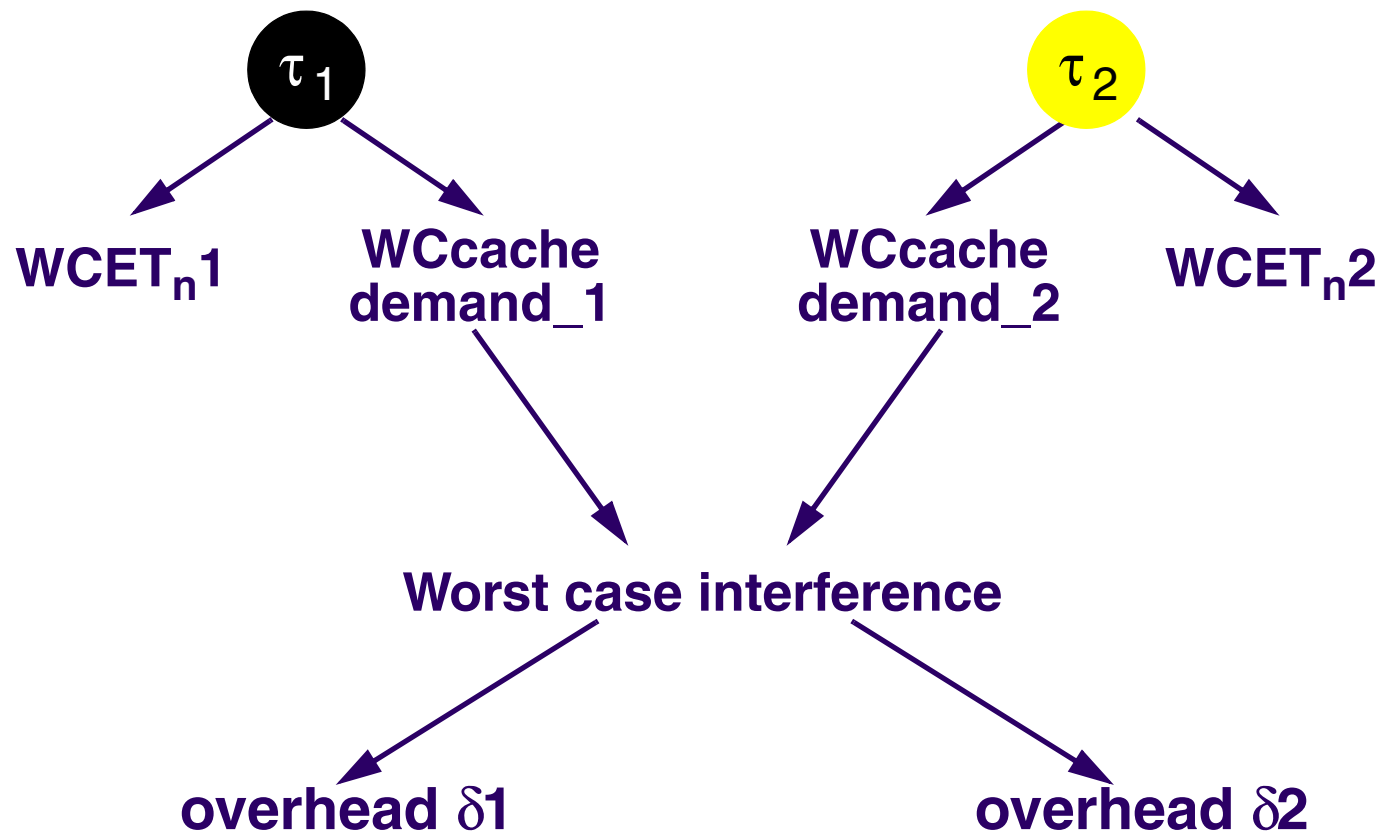
# A Possible Way?



- 👉 **Problem:** What is the WCcache demand and  $WCET_n$ ?
- The longest path is not necessarily the one with the most cache misses.



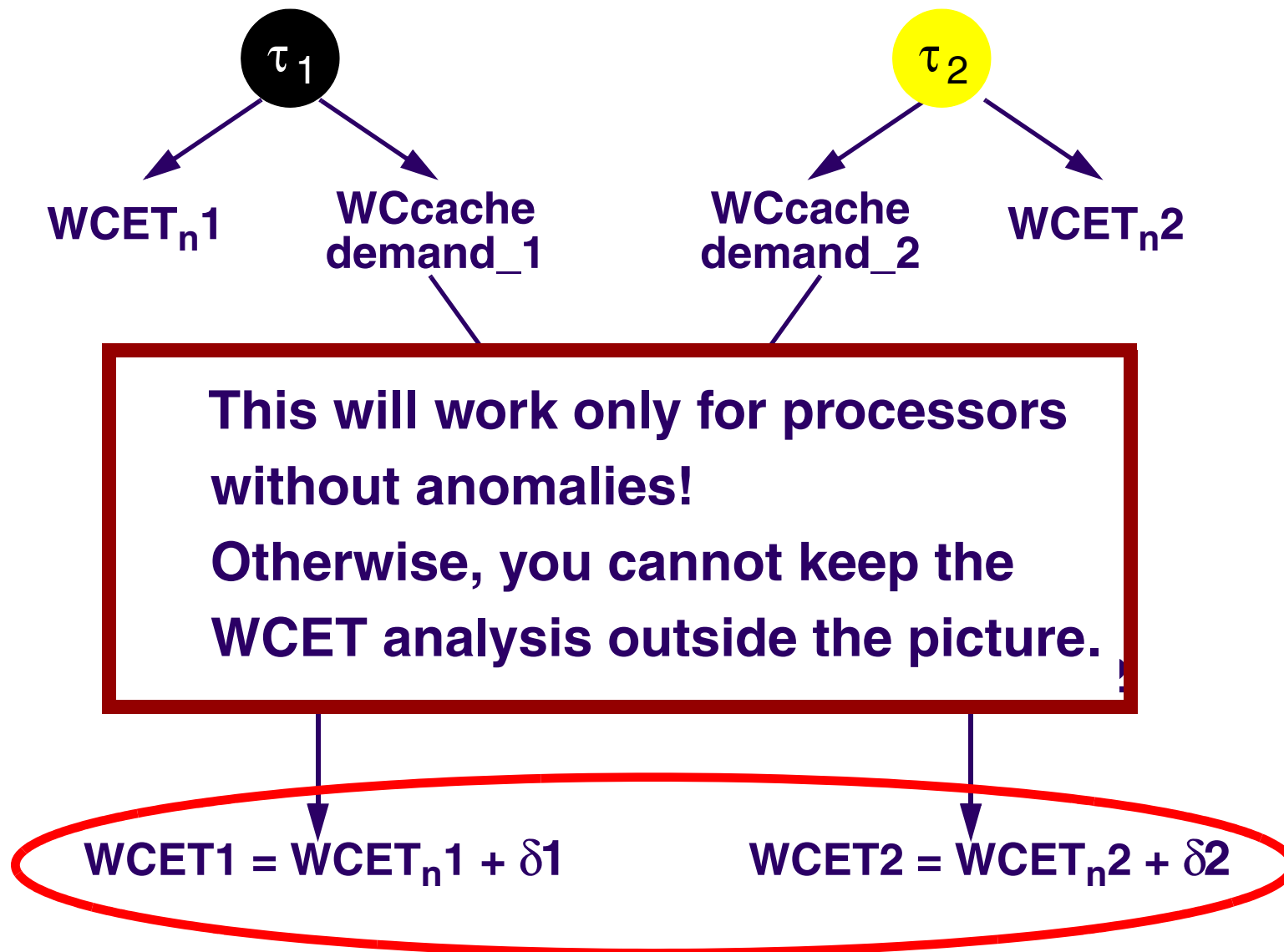
# A Possible Way?



 **Problem:** How to determine the Worst case interference and the related penalty?



# A Possible Way?

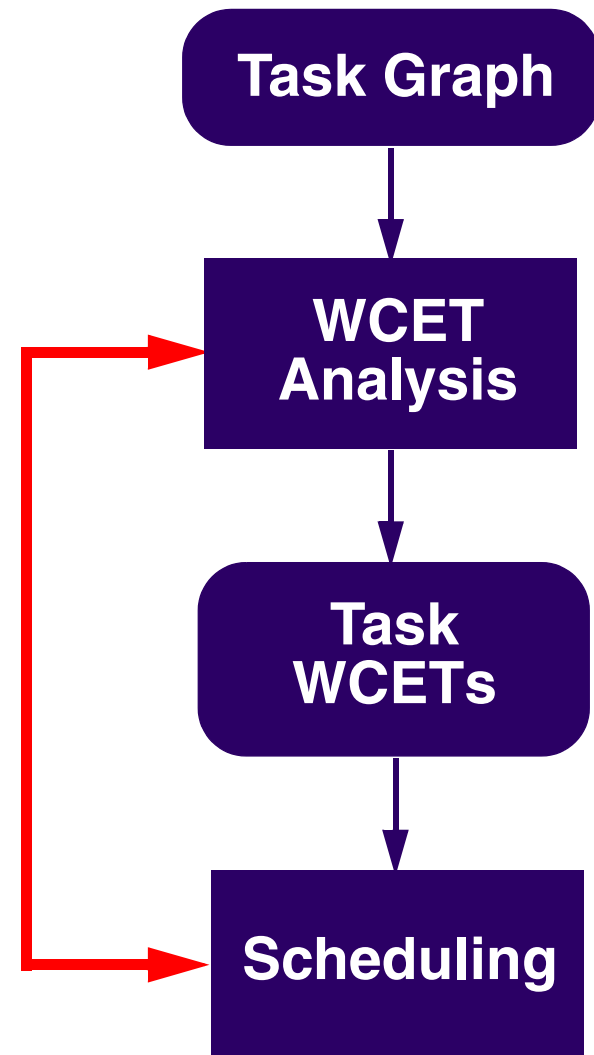


# Proposed Approach

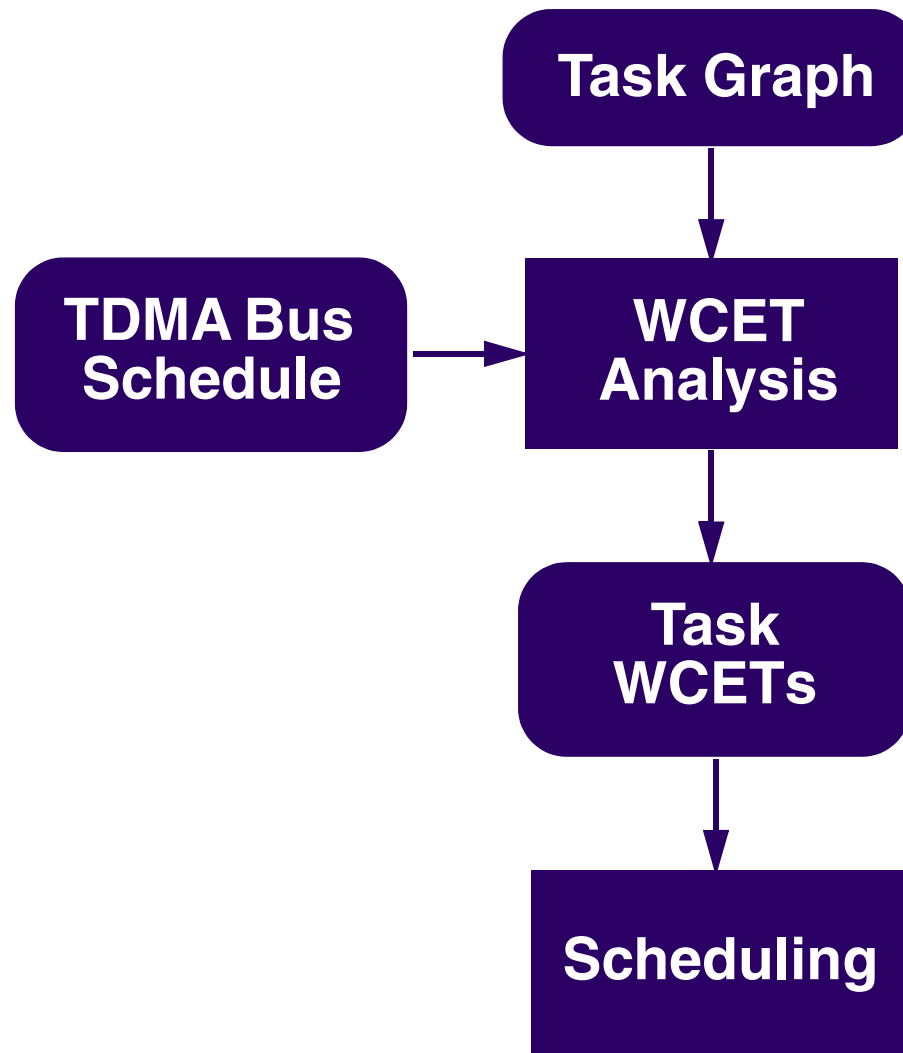
- The WCETs depend on the schedule (due to bus conflicts).
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👉 Solution:

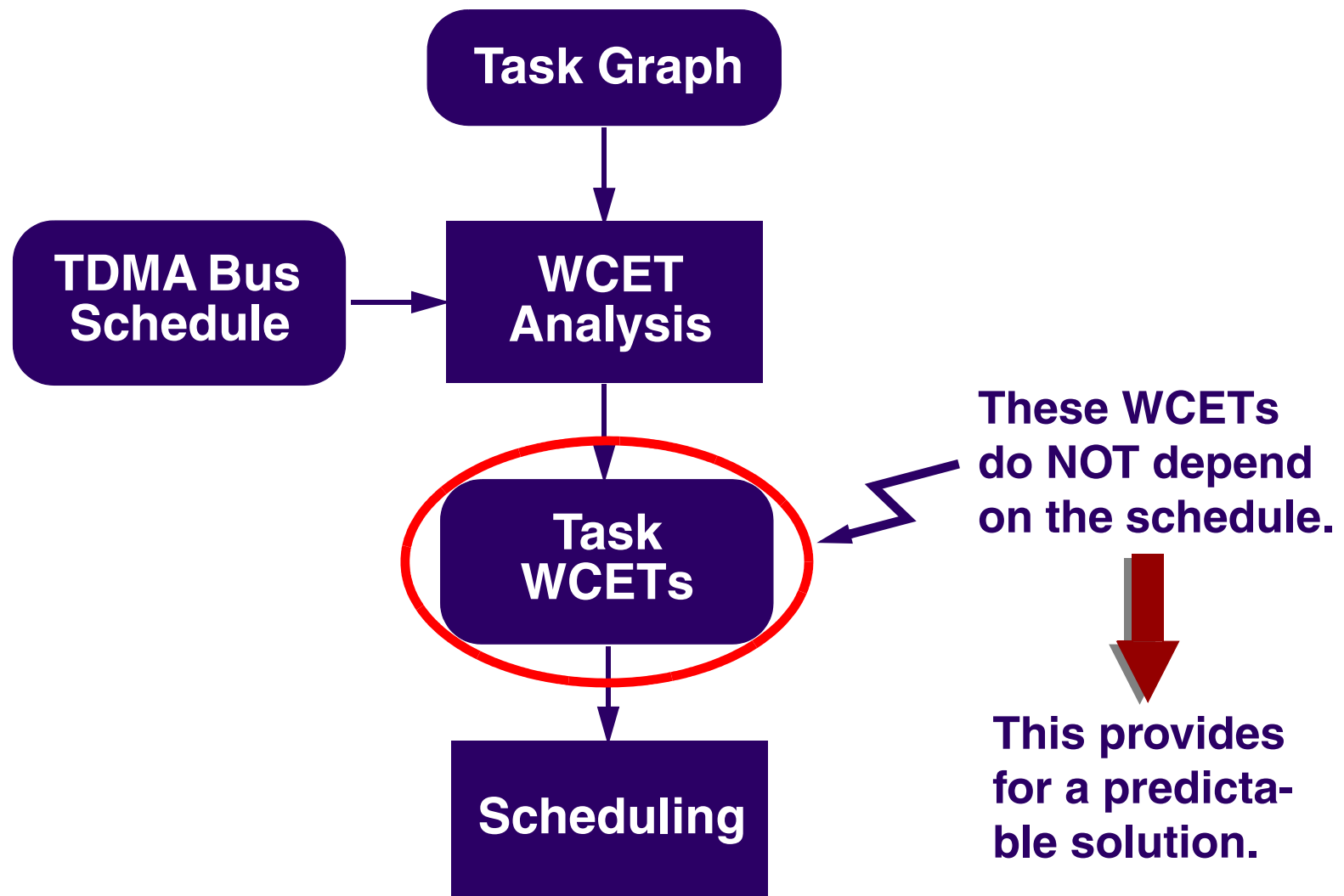
- Cut the circular dependency by using a *TDMA bus schedule*.





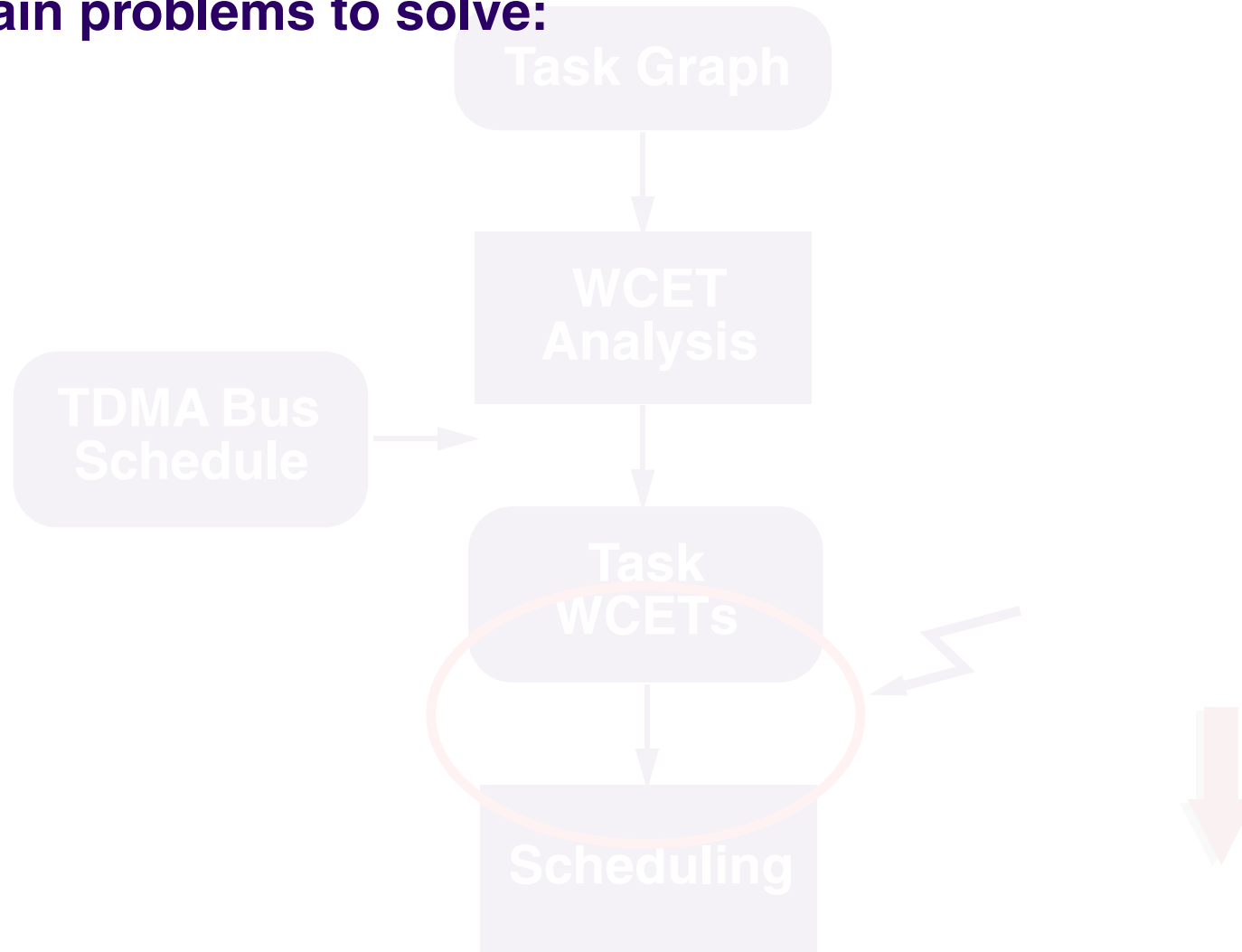


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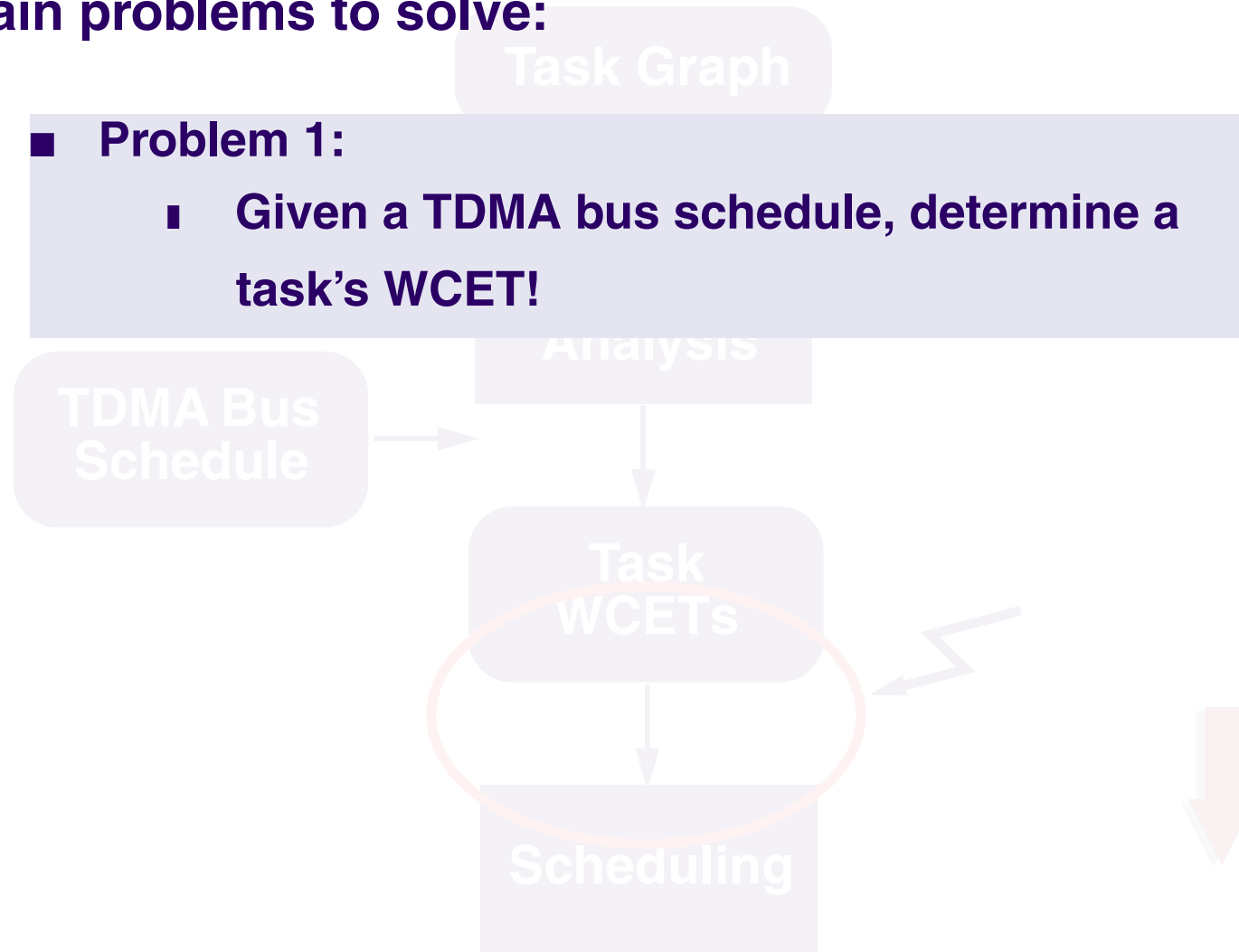
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- Find a “good” TDMA bus schedule!

Task Graph

Analysis

TDMA Bus

Scheduling



## ☞ Three main problems to solve:

### ■ Problem 1:

- Given a TDMA bus schedule, determine a task's WCET!

### ■ Problem 2:

- Find a “good” TDMA bus schedule!

### ■ Problem 3:

- Produce a system schedule!

Task Graph

Analysis

TDMA Bus

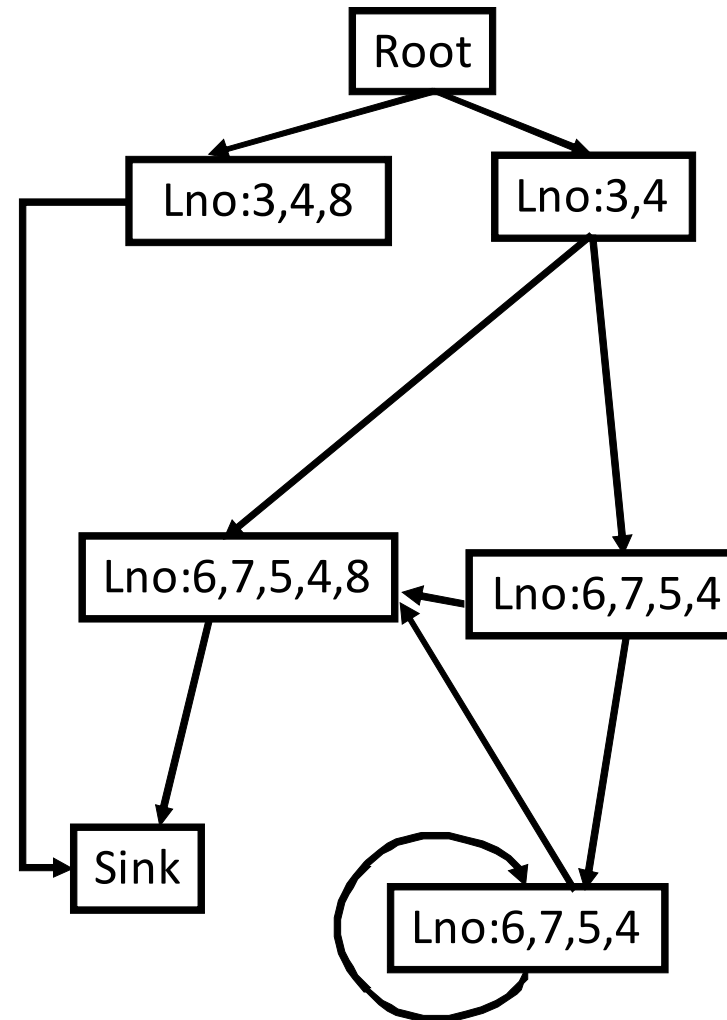


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# The WCET Analysis

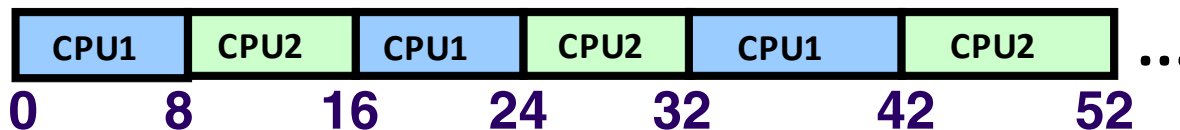
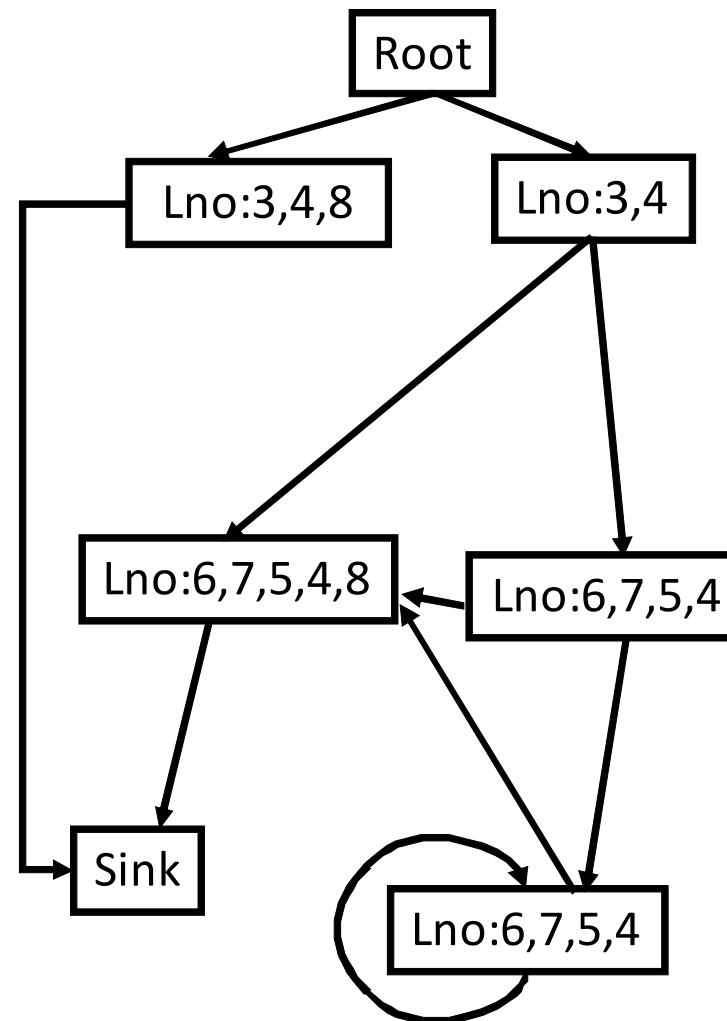
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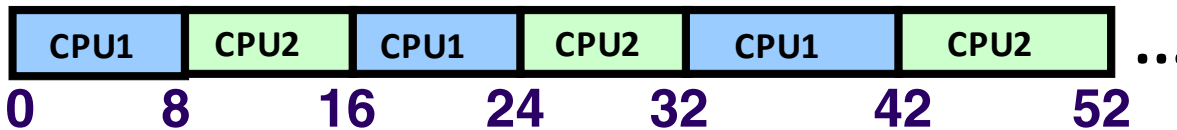
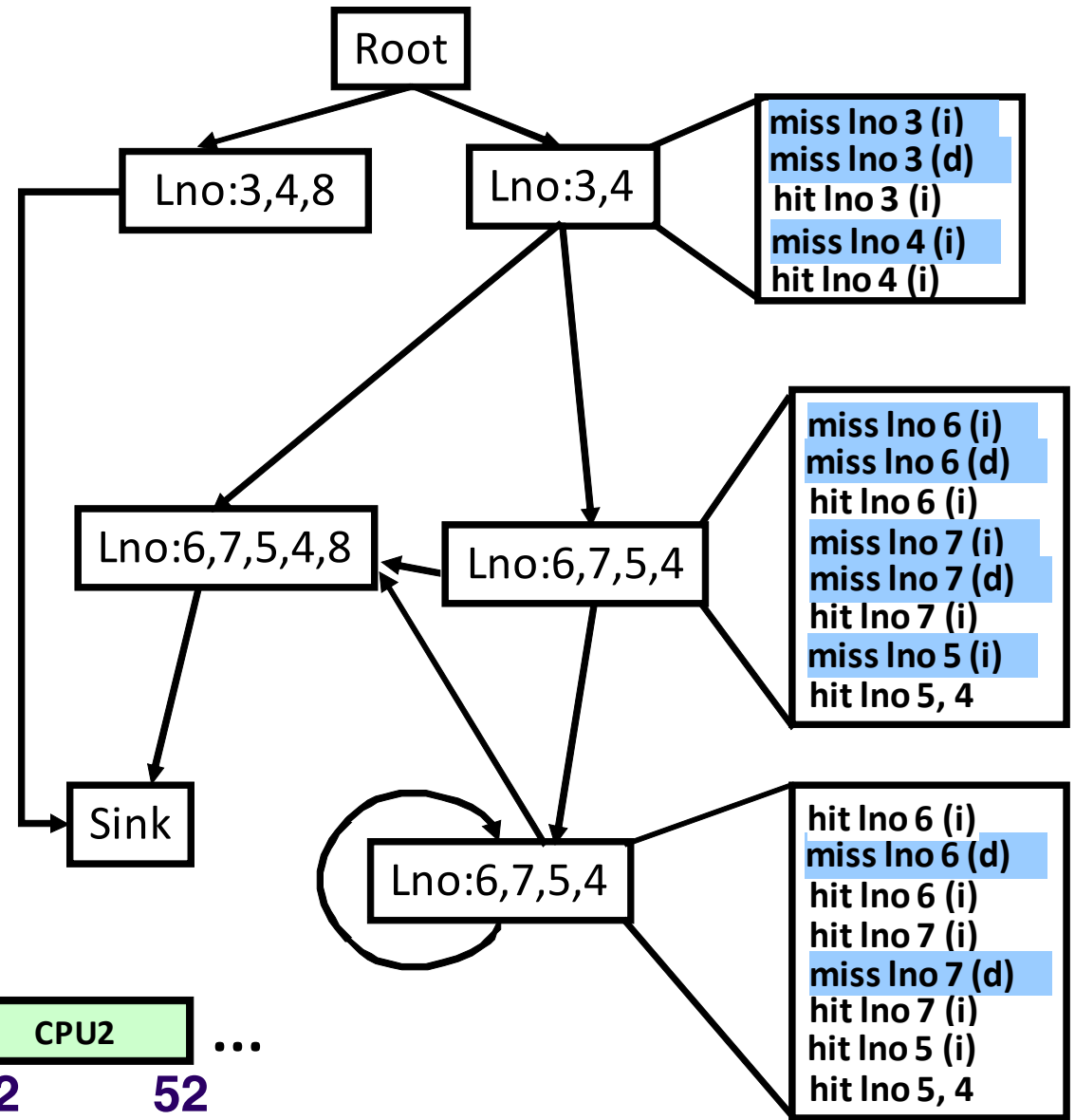
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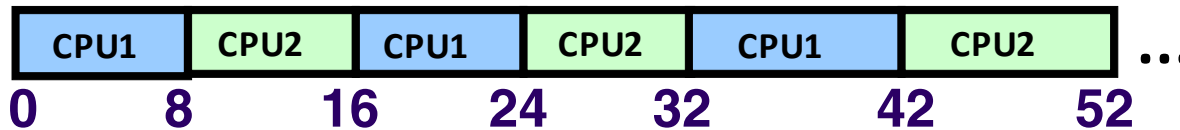
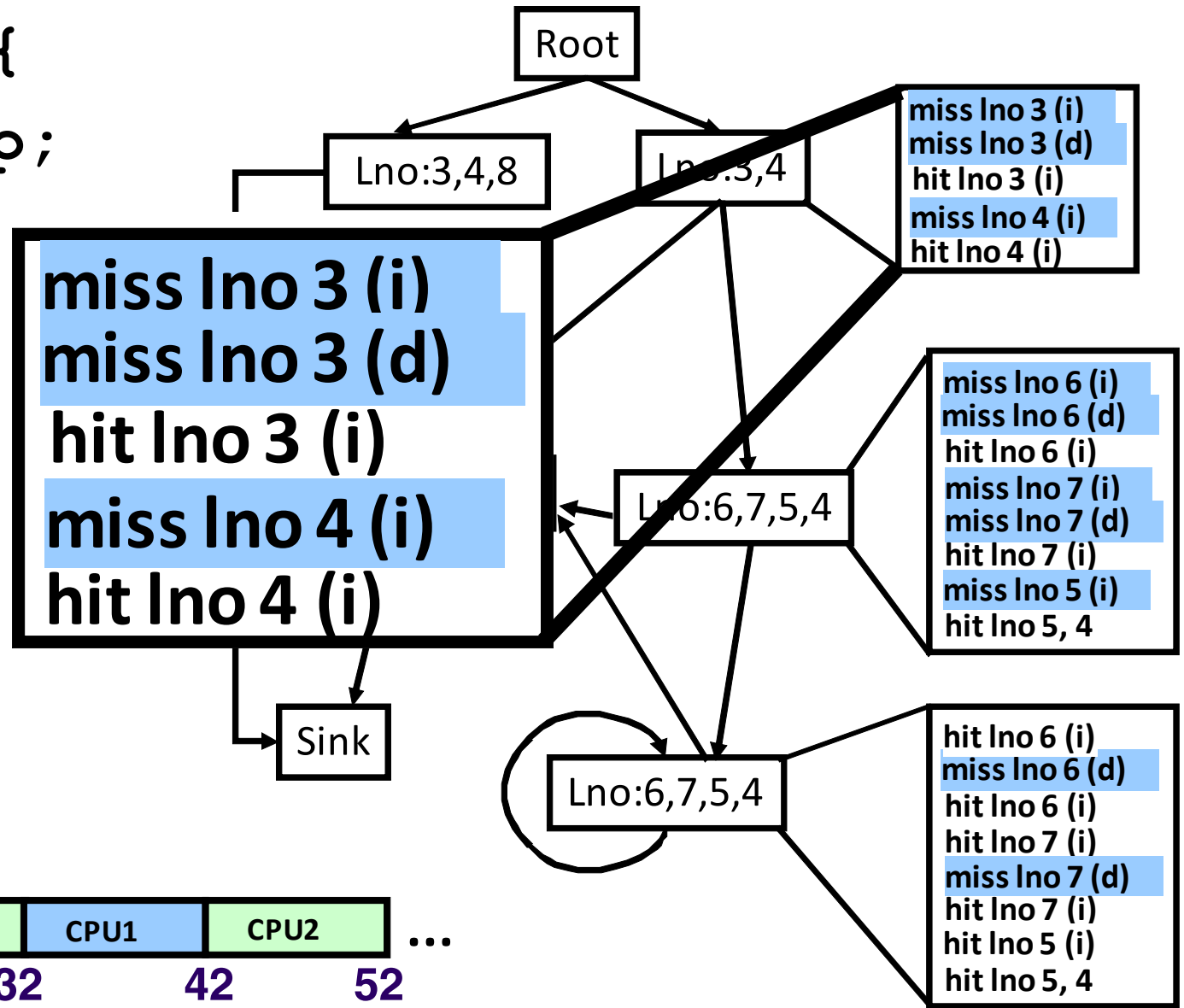
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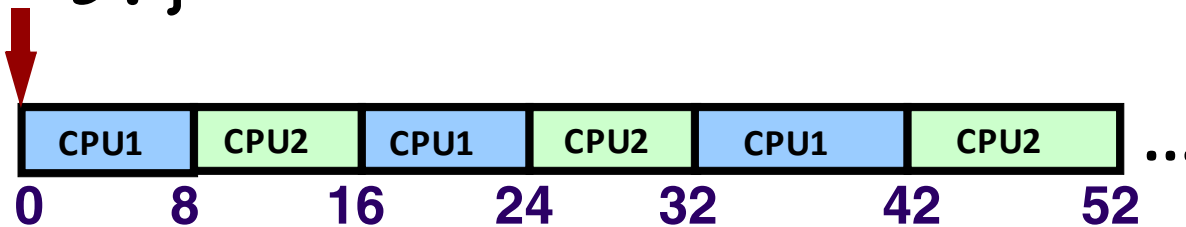
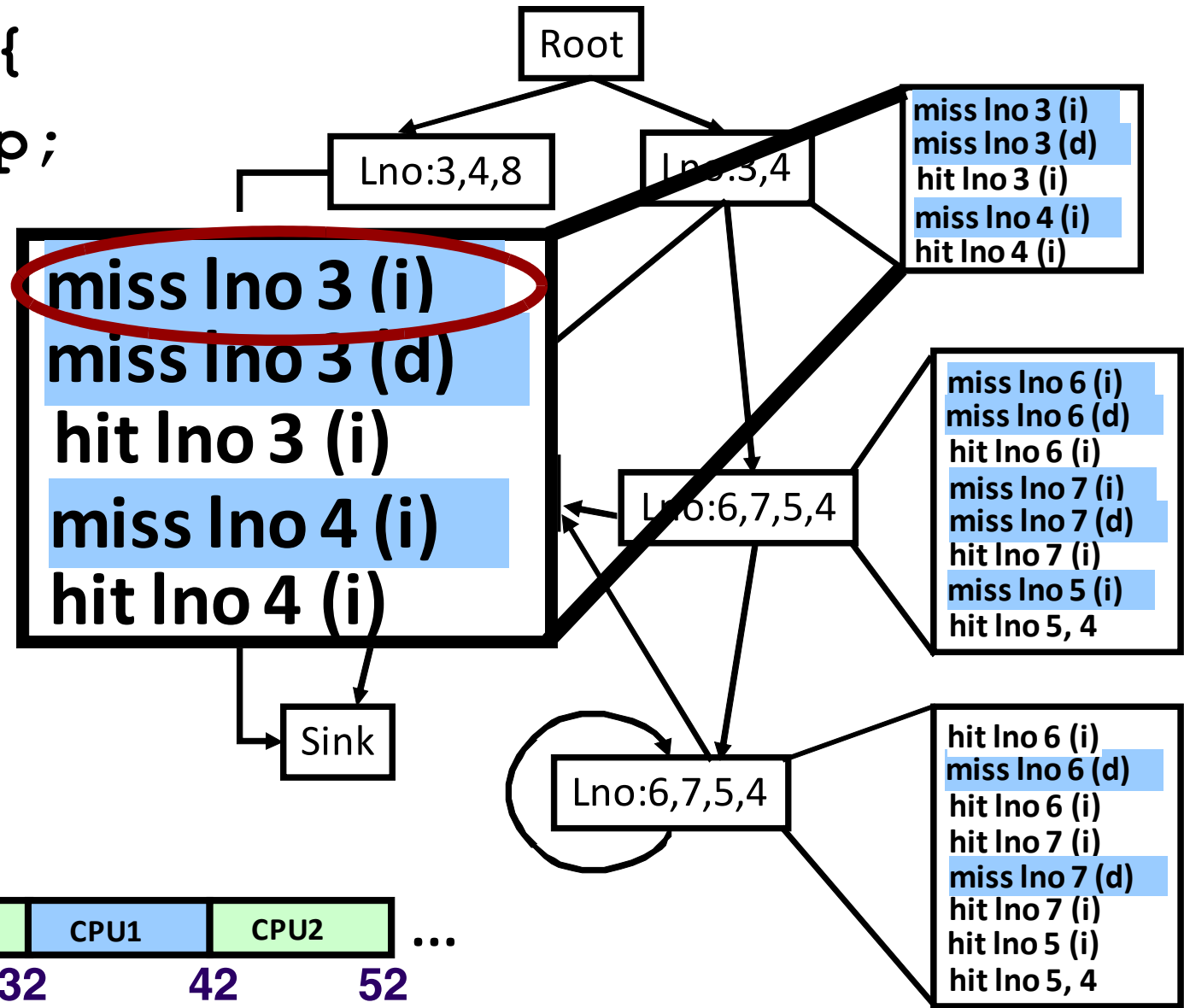
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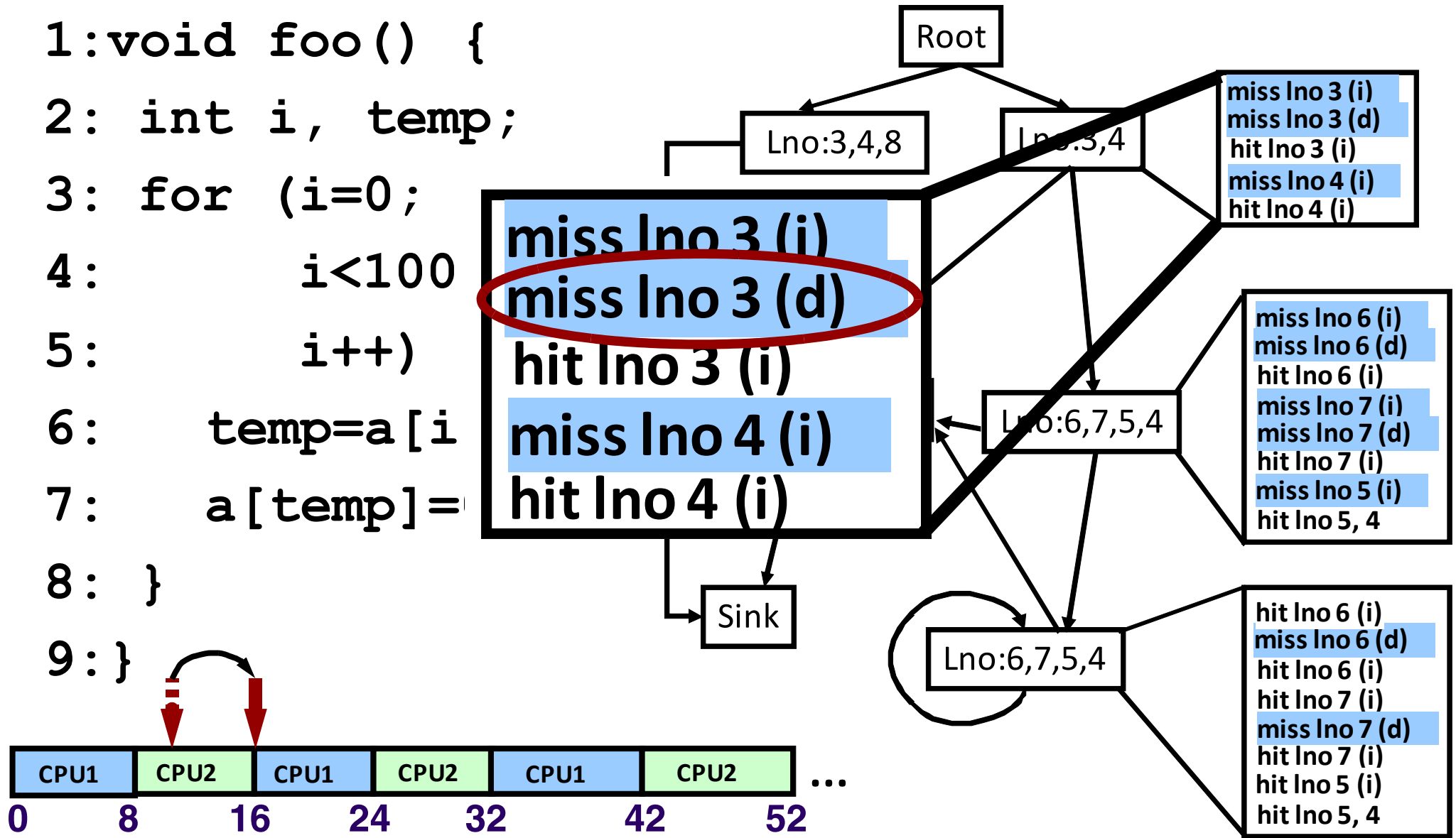
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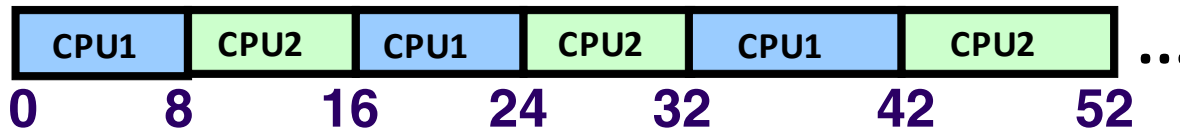
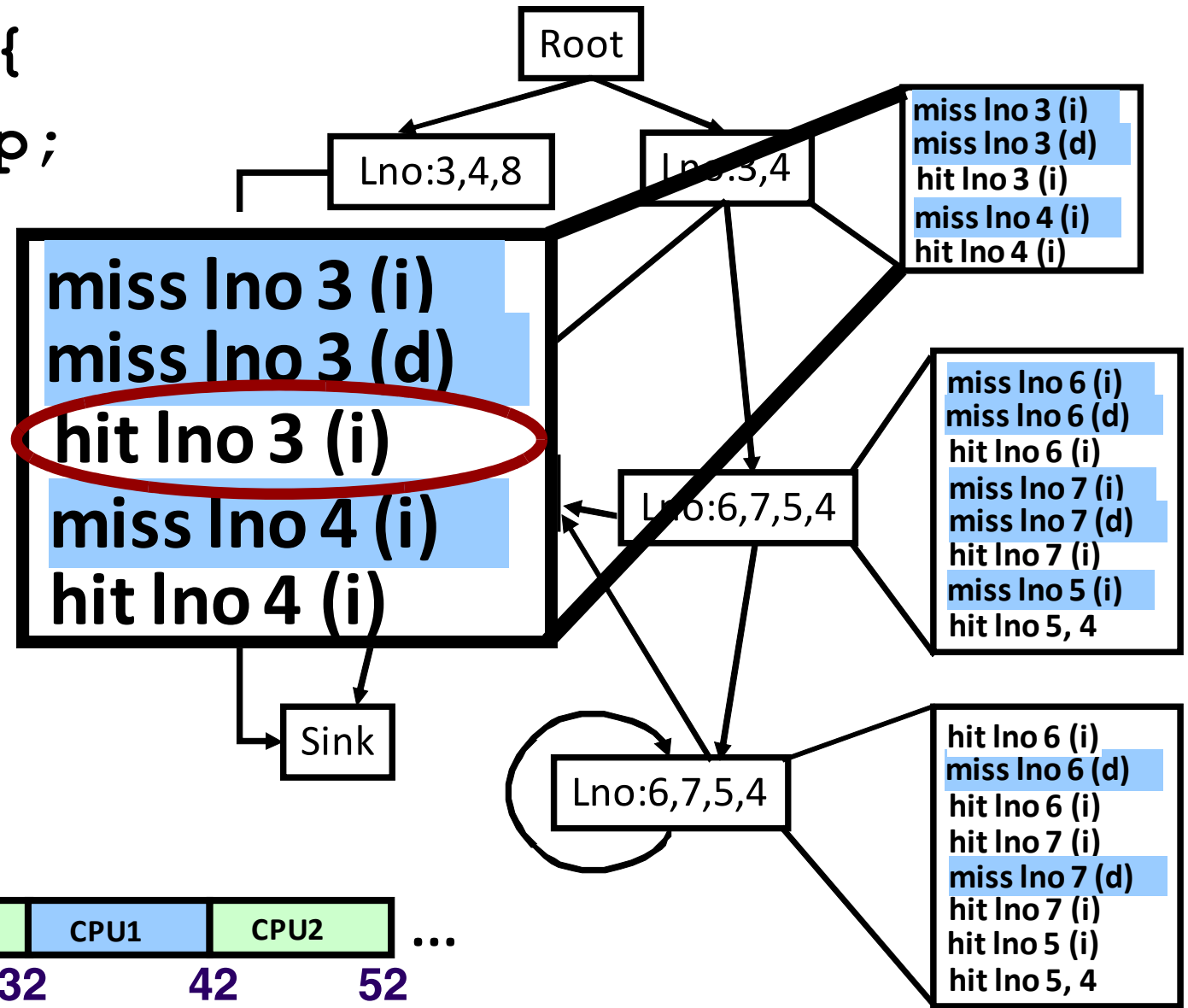
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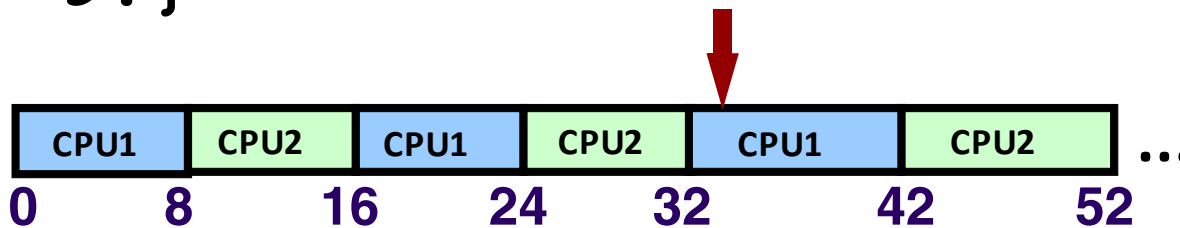
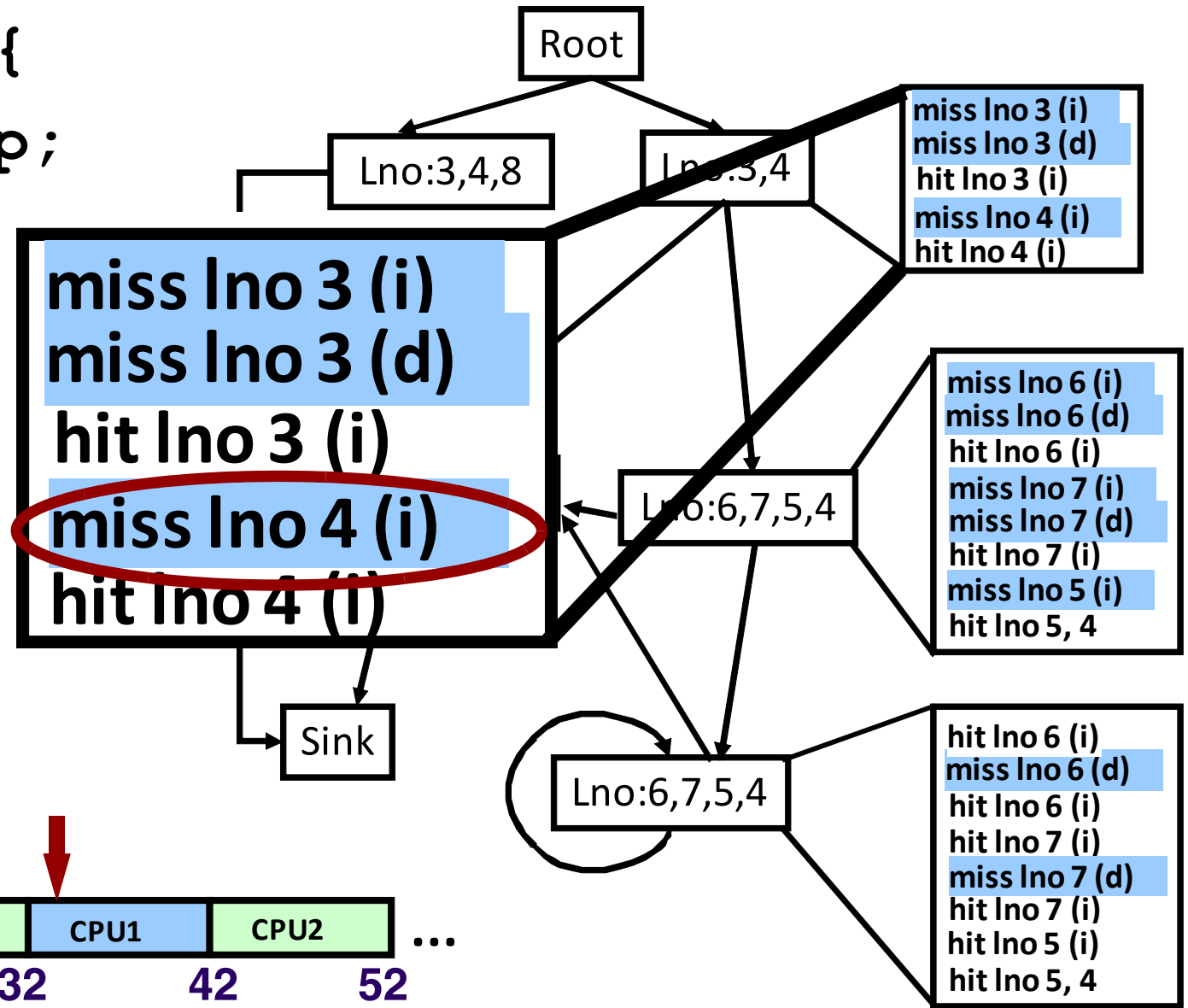
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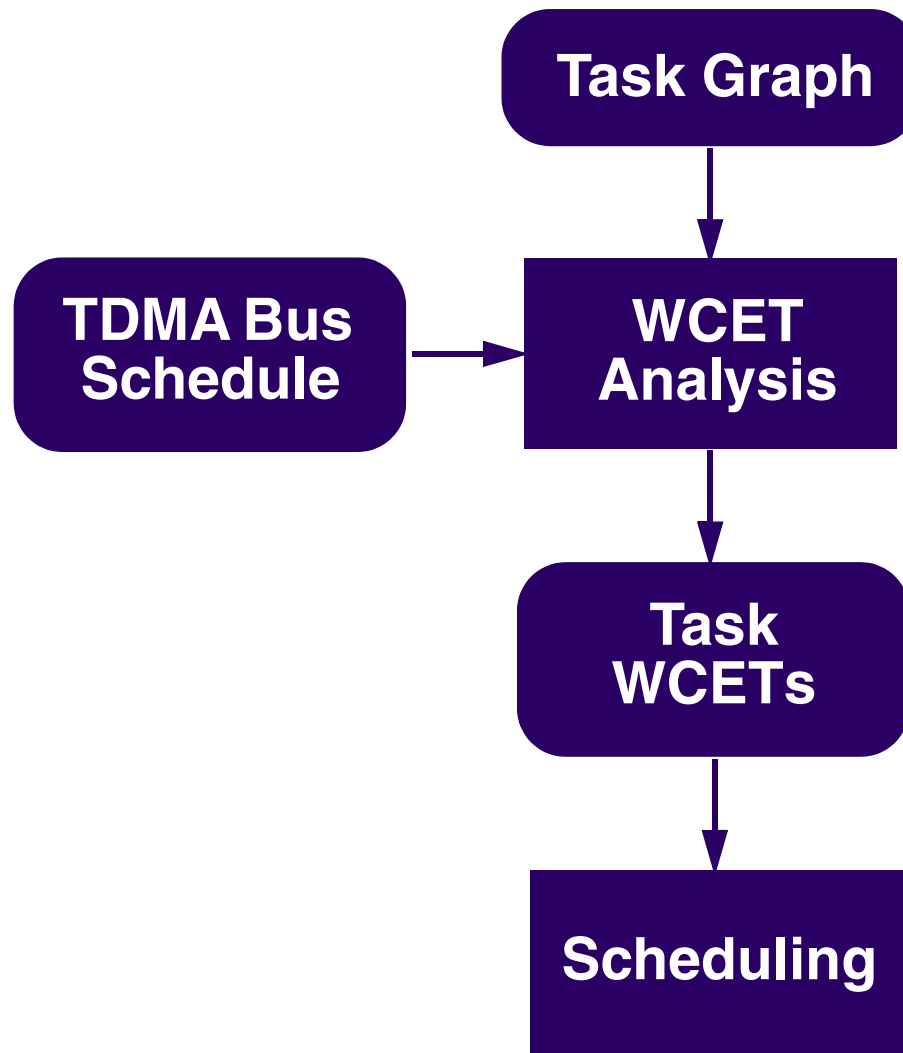


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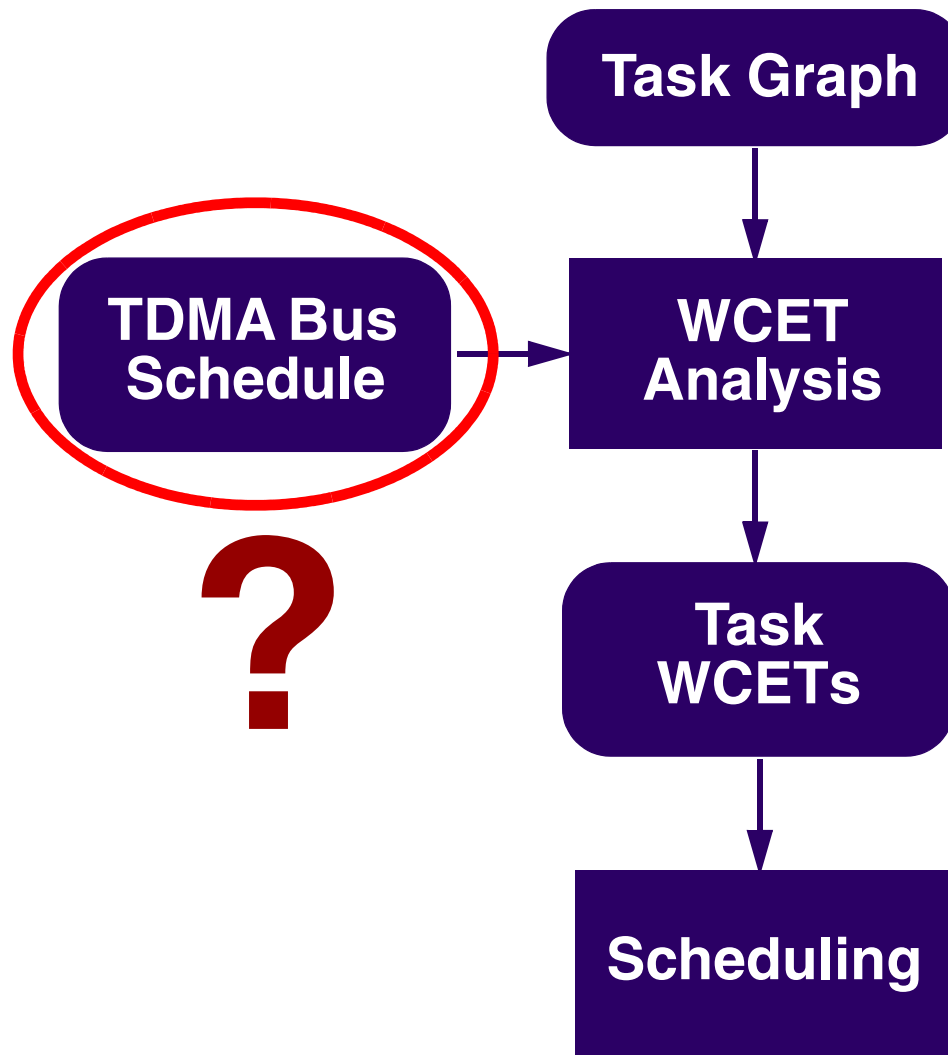


- ➡ Using the WCETs calculated with the given TDMA Bus schedule we can construct a safe system schedule.





# Back To The Big Picture



➡ Using the WCETs calculated with the given TDMA Bus schedule we can construct a safe system schedule.

➡ How to determine the TDMA Bus schedule?

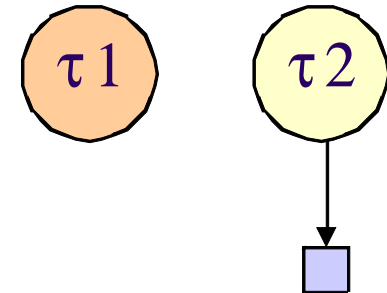


# TDMA Bus Schedule

- WCETs - as from “traditional” WCET analysis:

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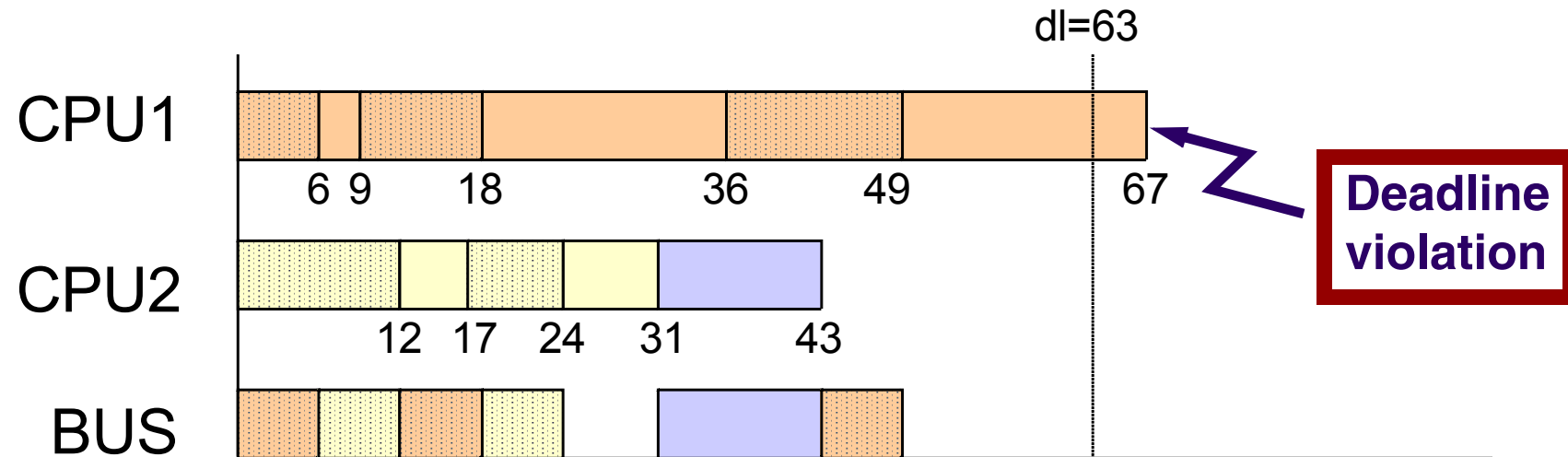
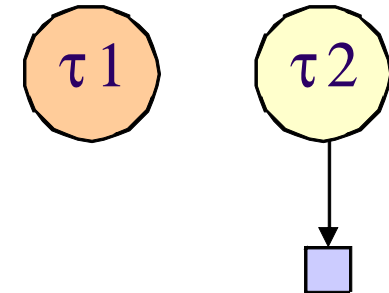
- Deadline: 63



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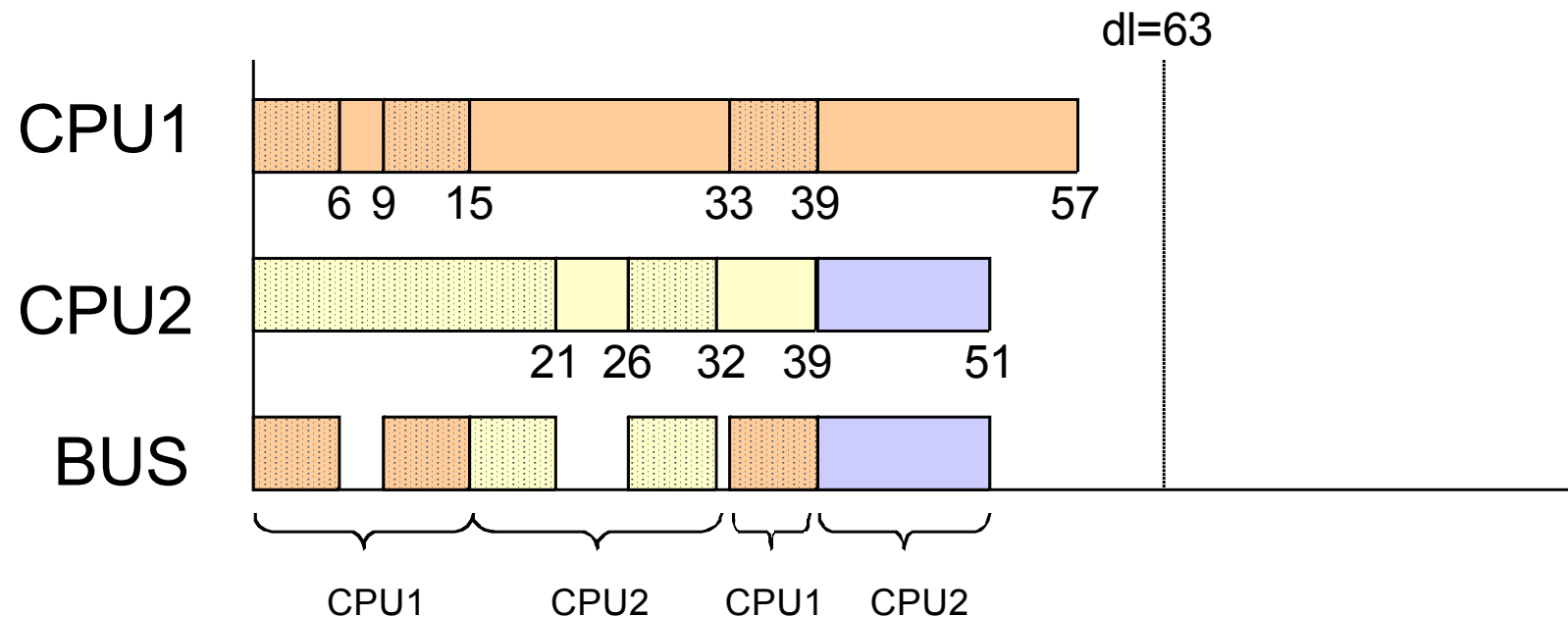
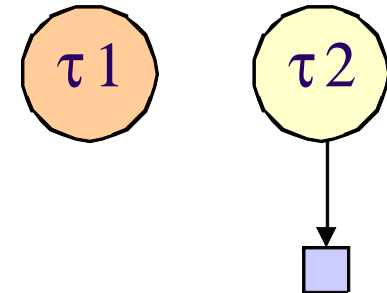
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# TDMA Bus Schedule



- ☞ Any TDMA Bus schedule provides a predictable, safe schedule.
- ☞ The bus schedule matters in terms of worst case schedule length!



# TDMA Bus Schedule



☞ Any TDMA Bus schedule provides a predictable, safe schedule.

☞ The bus schedule matters in terms of worst case schedule length!

## ■ Problem:

- Find a TDMA bus schedule which minimises the worst case schedule length!



# TDMA Bus Schedule



☞ An ideal bus schedule would serve each miss as fast as possible.



☞ Adapt the bus schedule to the distribution of the cache misses as detected by the WCET analysis!



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# TDMA Bus Schedule

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☞ Adapt the bus schedule to the distribution of the cache misses as detected by the WCET analysis!



☞ Tasks which are simultaneously active have bus access requirements that are conflicting.



☞ Cache misses are distributed irregularly.



☞ A bus schedule following this irregularity would consume very much memory in the bus controller.



# TDMA Bus Schedule Approaches



## ■ Four TDMA Bus Schedule Approaches:

■ BSA1    ■ BSA2    ■ BSA3    ■ BSA4

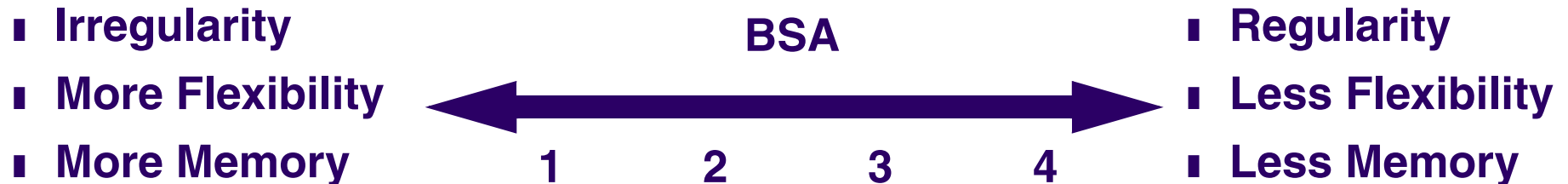


# TDMA Bus Schedule Approaches

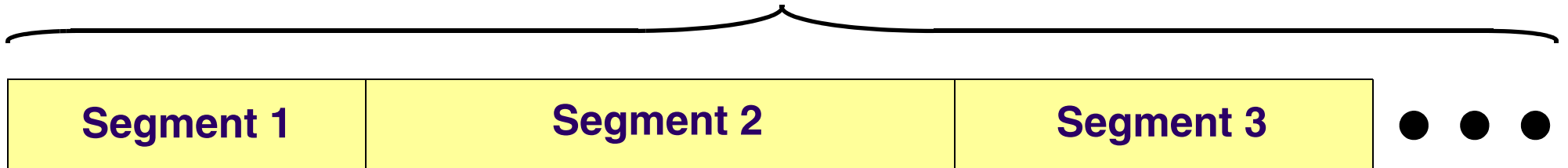


## ■ Four TDMA Bus Schedule Approaches:

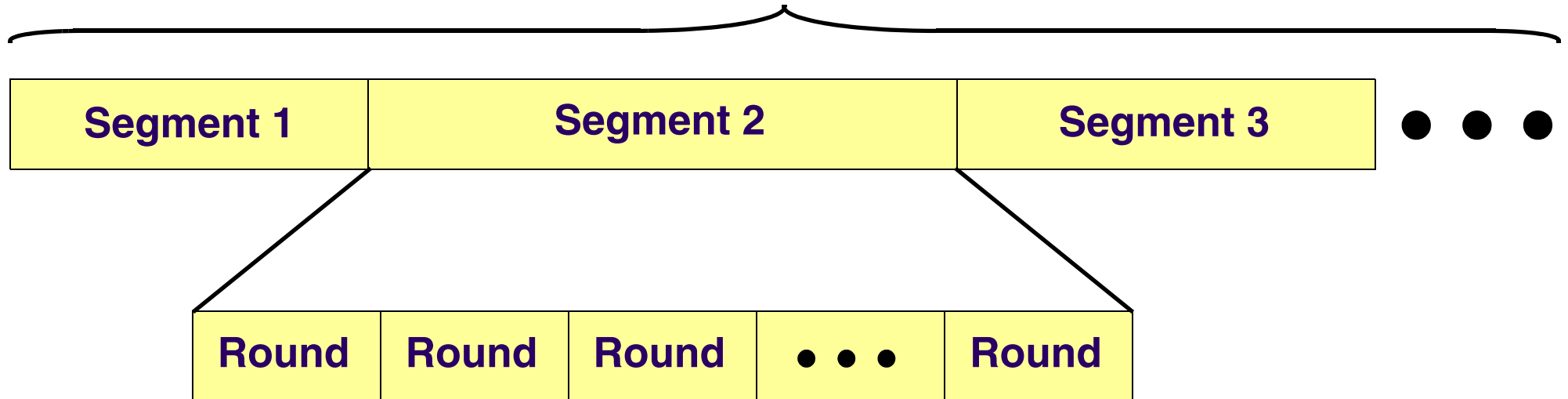
- You have to pay for predictability:
  - Performance
  - Hardware overhead



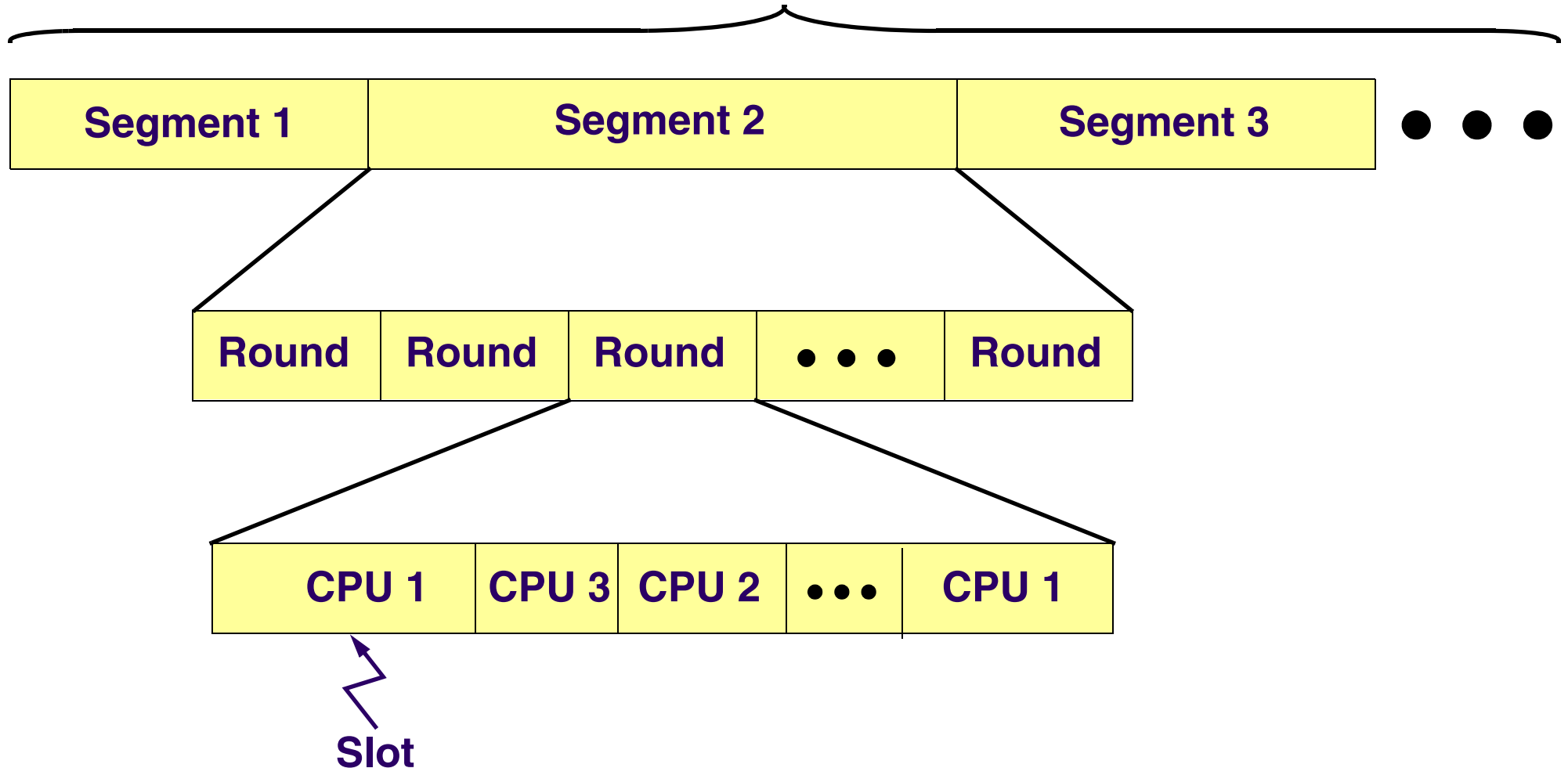
**Bus Schedule: over a period**



## Bus Schedule: over a period

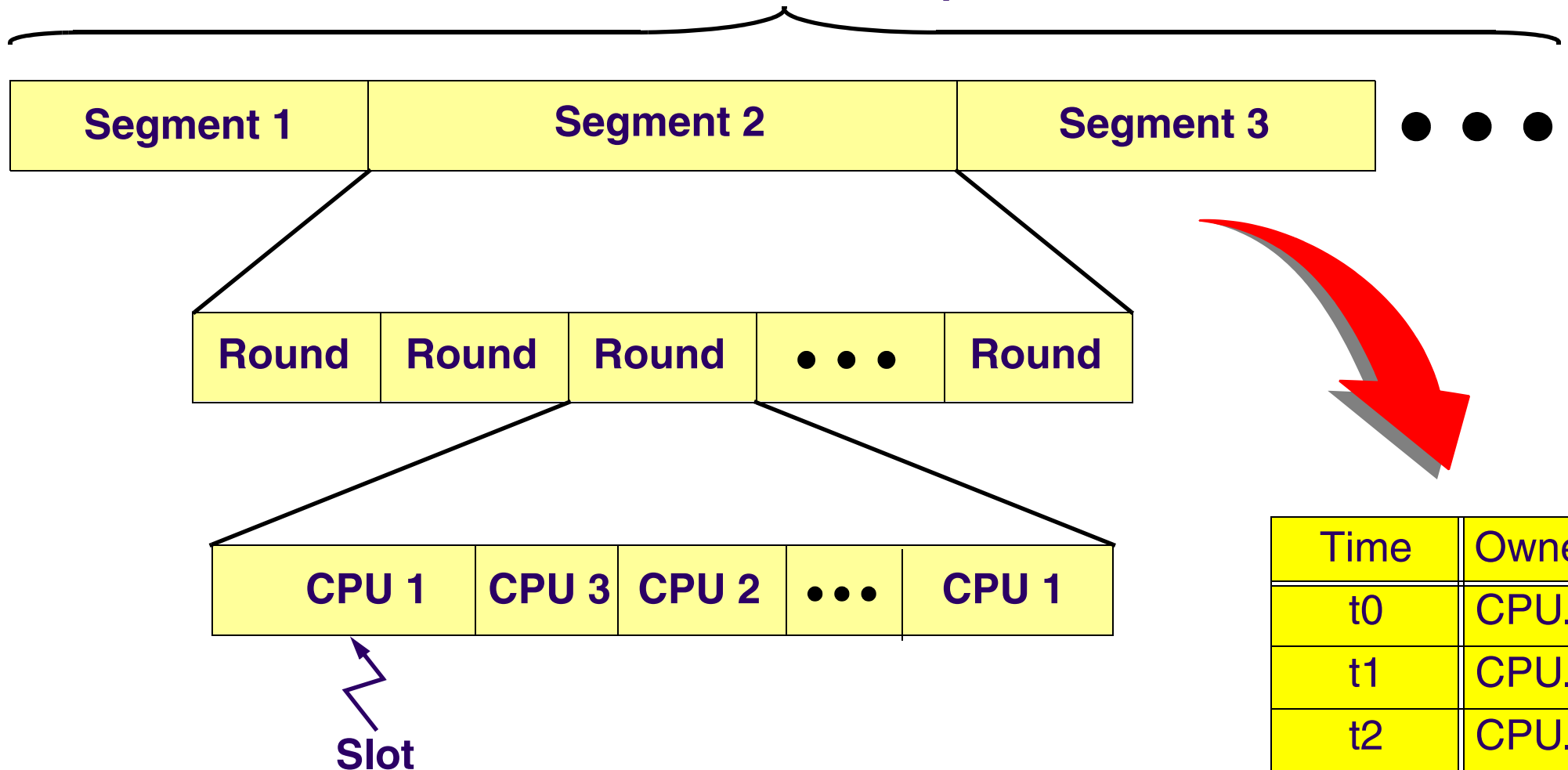


## Bus Schedule: over a period



# Bus Schedule

## Bus Schedule: over a period



☞ The most general, unrestricted, bus schedule:

- Composed of one single segment
  - Consisting of one single round
    - Consisting of an arbitrary sequence of slots of arbitrary size.





☞ The most general, unrestricted, bus schedule:

- Composed of one single segment

- Consisting of one single round

- Consisting of an arbitrary sequence of slots of arbitrary size.

☞ Can, potentially, be very well customised to the actual cache miss profile.

☞ Huge memory requirements!



☞ Not realistic but a good reference for comparison





## ■ Restriction:

- Each processor has maximum one slot in a round.

👉 Slot sizes in a round and their order are arbitrary.

👉 Rounds belonging to different segments are different.





## ■ Restriction:

- Each processor has maximum one slot in a round (BSA2).
- All slots in a round must have the same size.

👉 Rounds belonging to different segments are different.





## ■ Restriction:

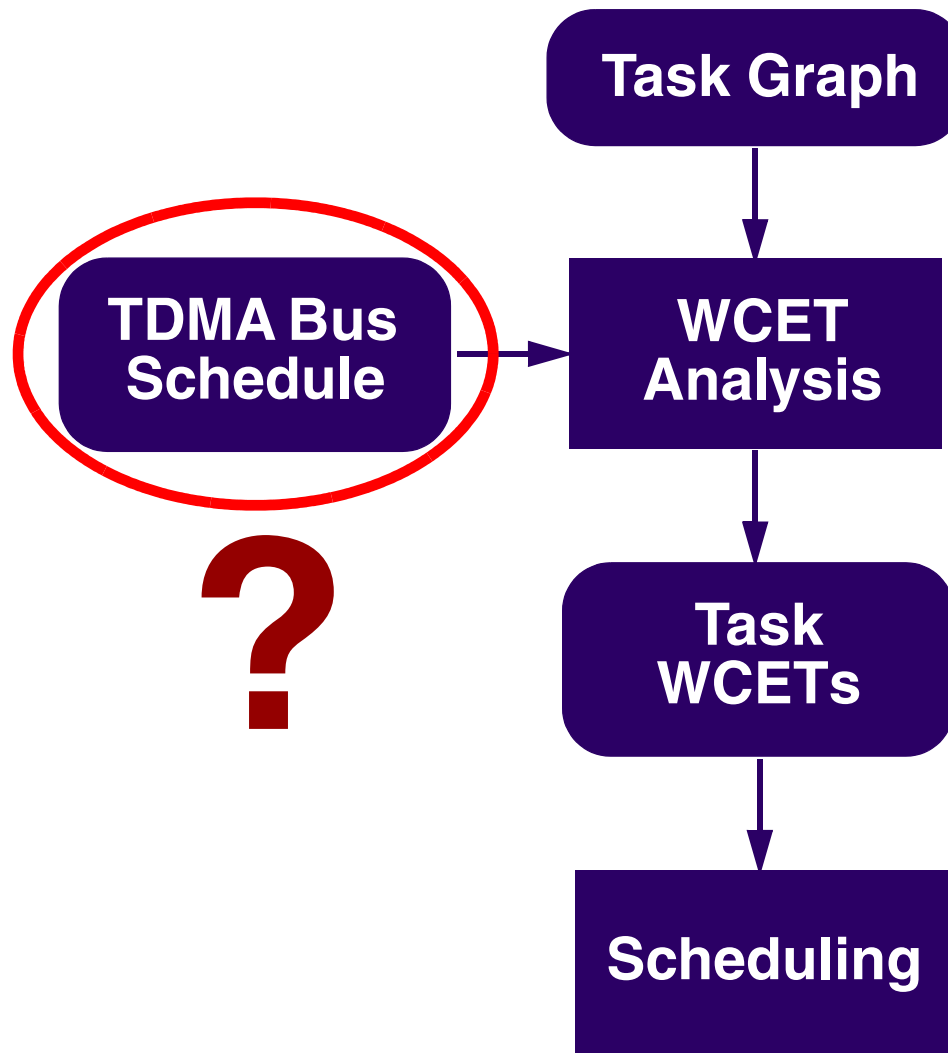
- Each processor has maximum one slot in a round (BSA2).
- All slots in a round must have the same size (BSA3).
- All rounds, in all segments, are identical.

☞ The same round repeats over the whole bus schedule.

☞ This is an *extremely* constrained approach!



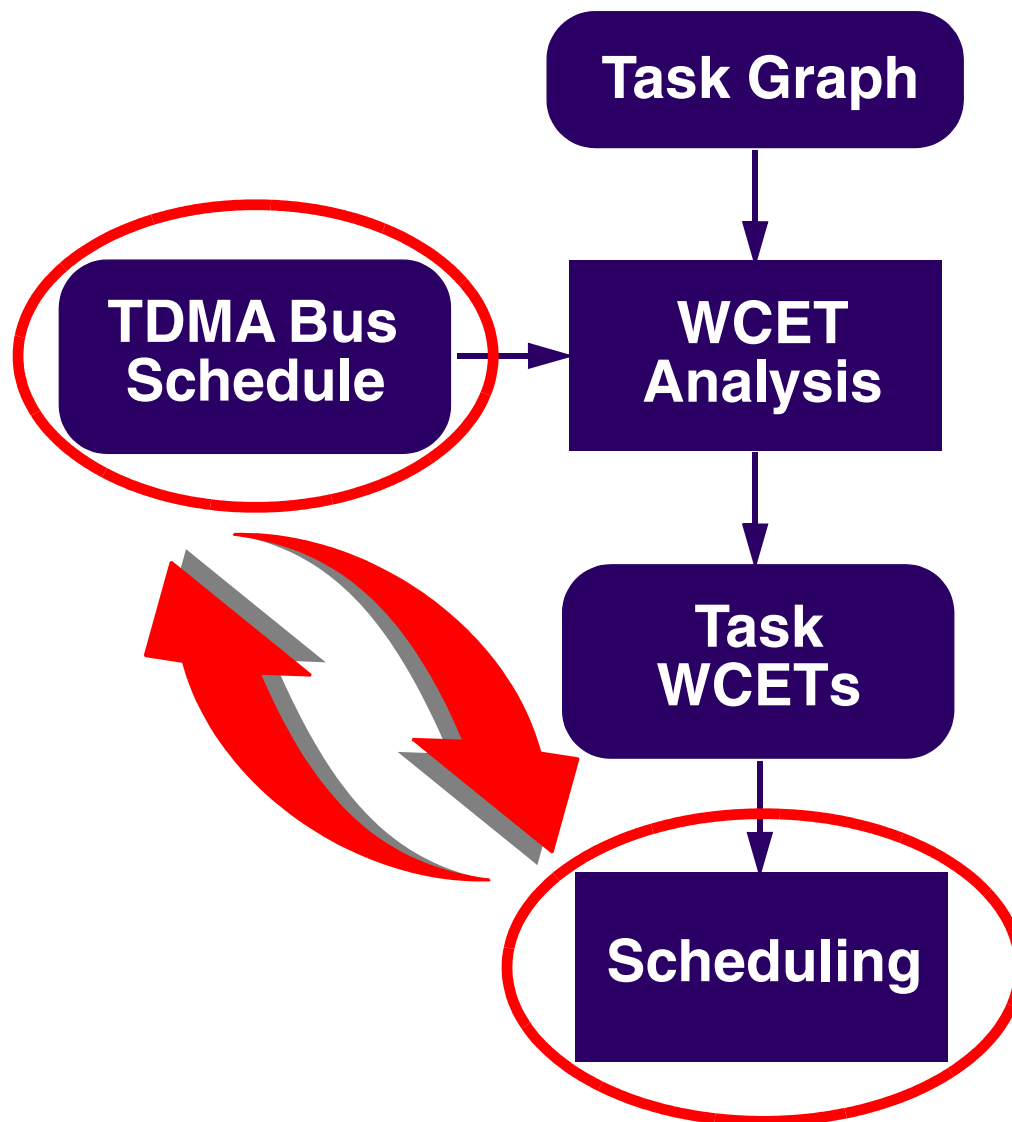
# Back To The Big Picture



- ➡ Using the WCETs calculated with the given TDMA Bus schedule we can construct a safe system schedule.
- ➡ How to determine the TDMA Bus schedule?



# Back To The Big Picture



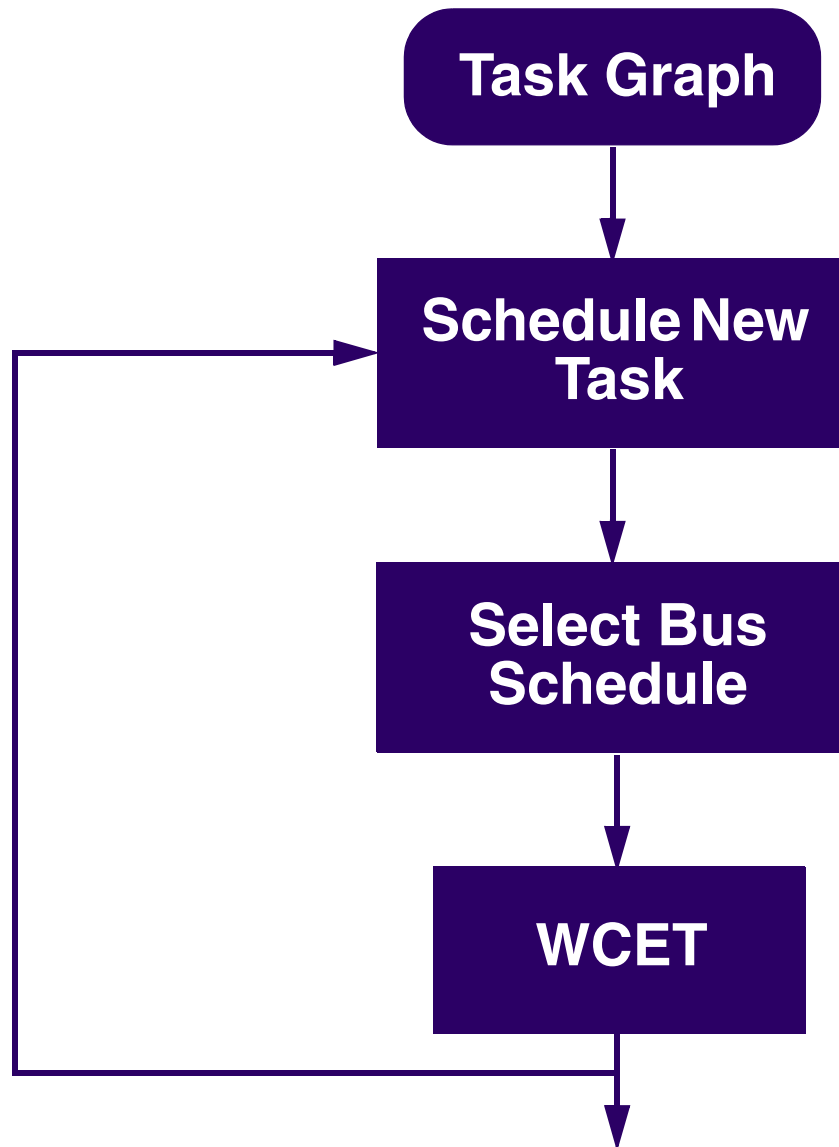
➡ Using the WCETs calculated with the given TDMA Bus schedule we can construct a safe system schedule.

➡ How to determine the TDMA Bus schedule?

➡ The bus schedule is determined simultaneously with the task graph scheduling.



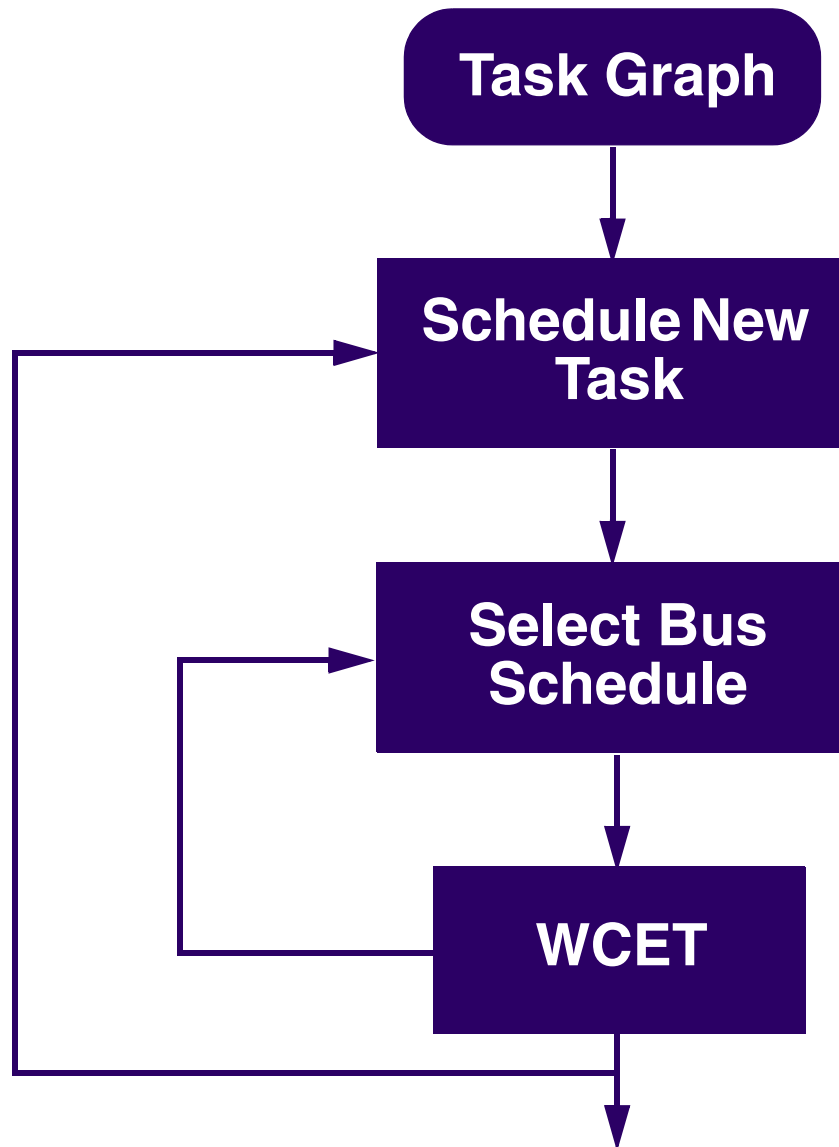
# Back To The Big Picture



👉 The bus schedule is determined simultaneously with the task graph scheduling.



# Back To The Big Picture

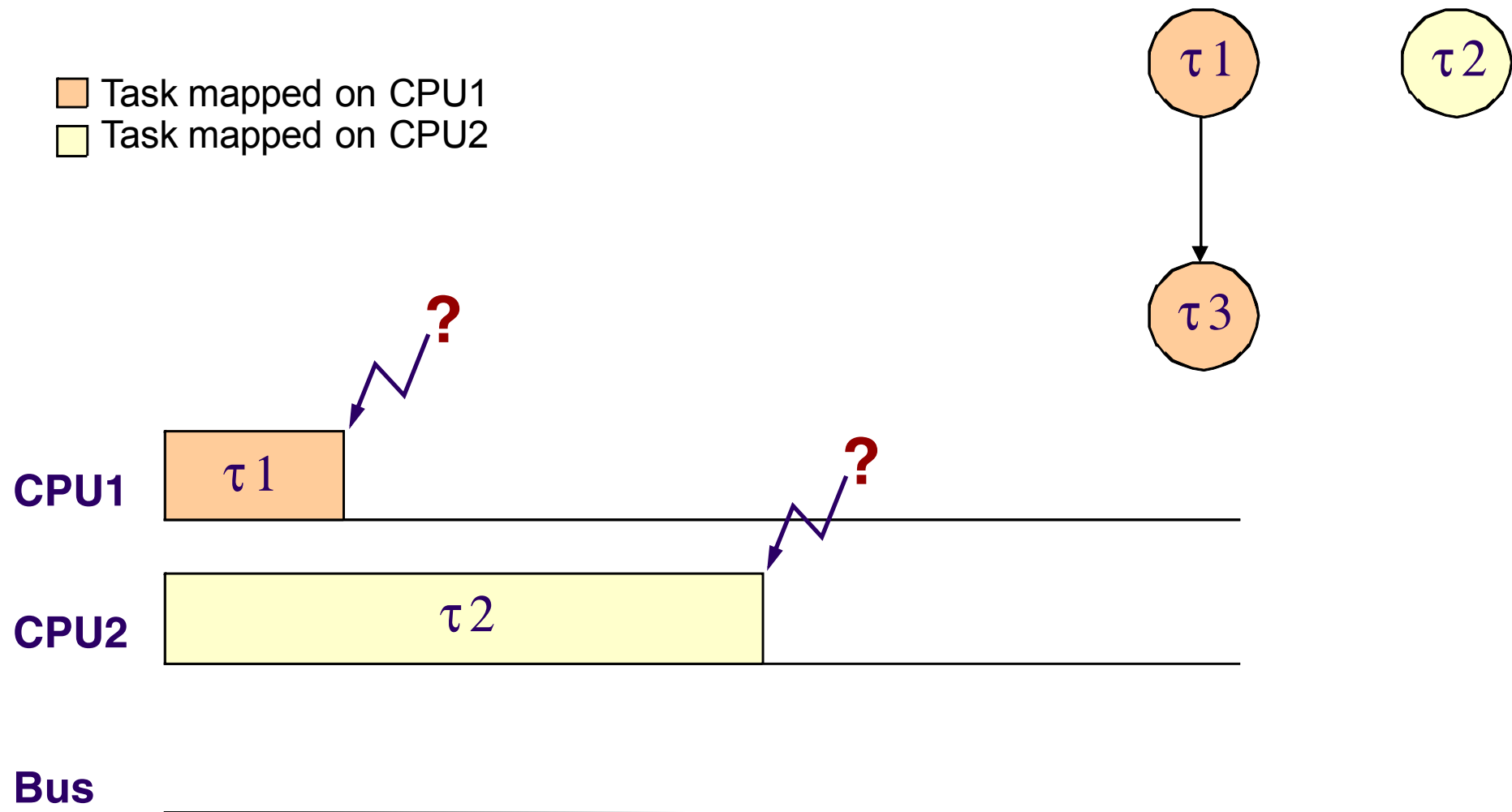


👉 The bus schedule is determined simultaneously with the task graph scheduling.

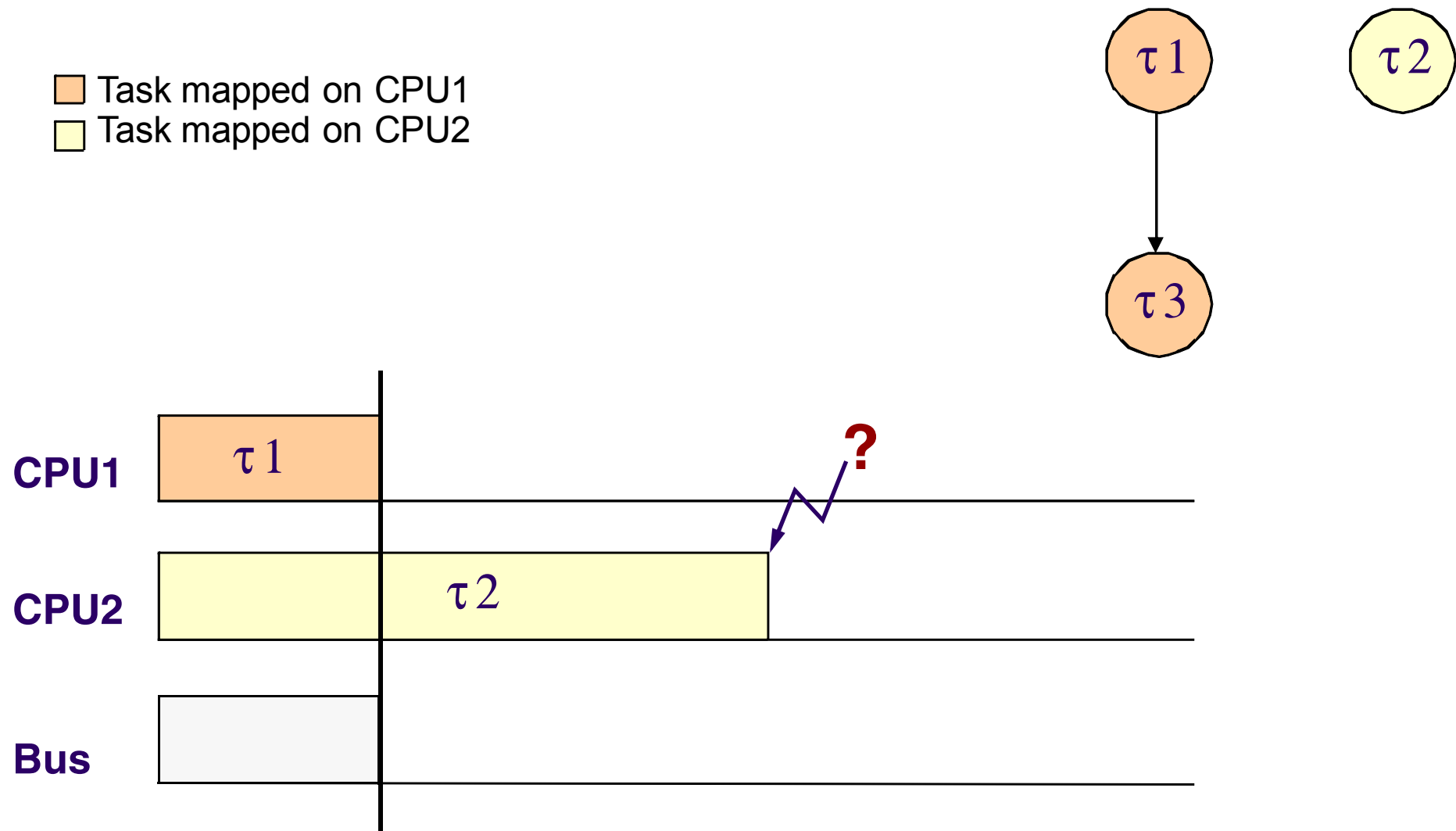




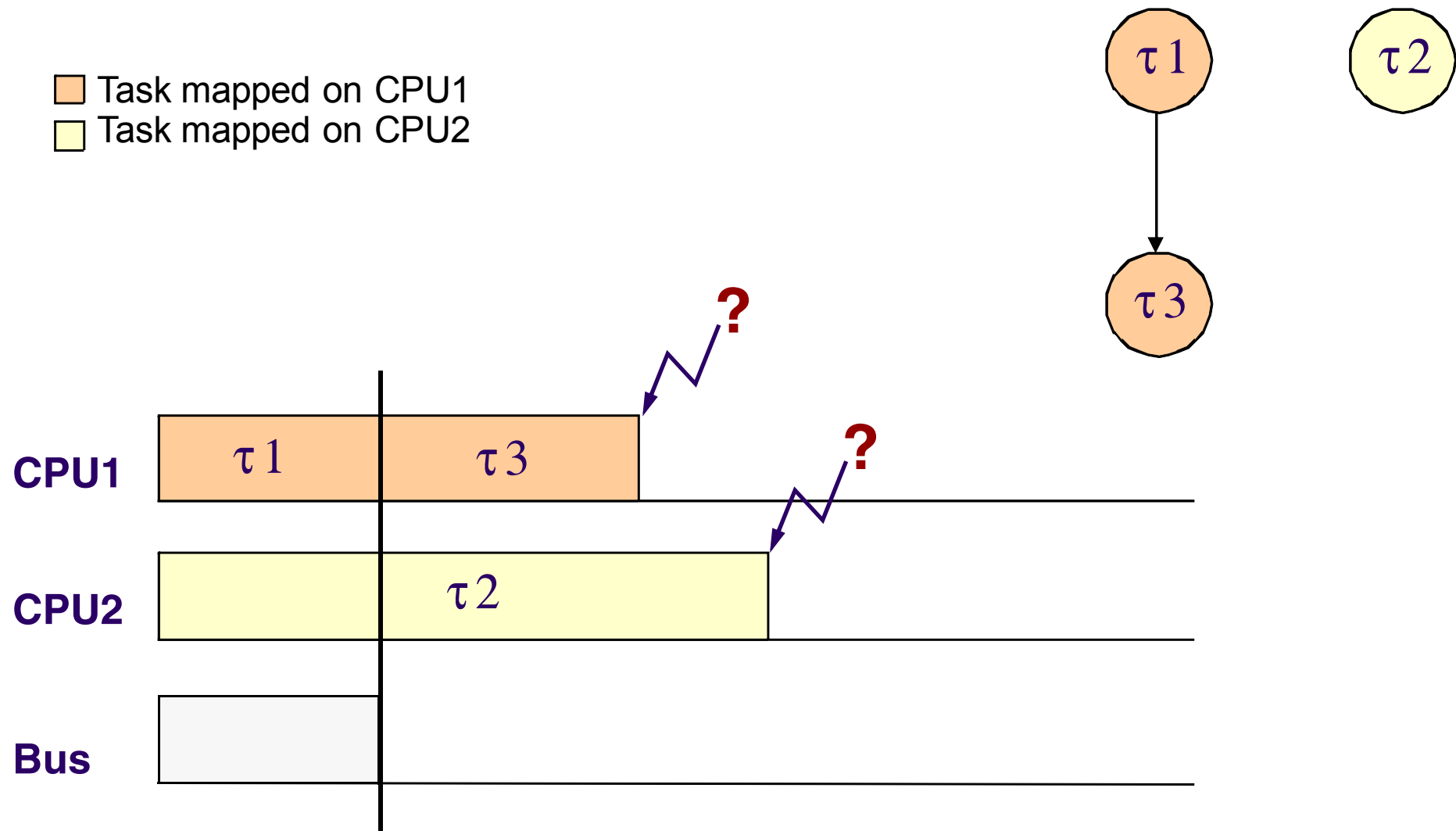
# The Big Picture: Example



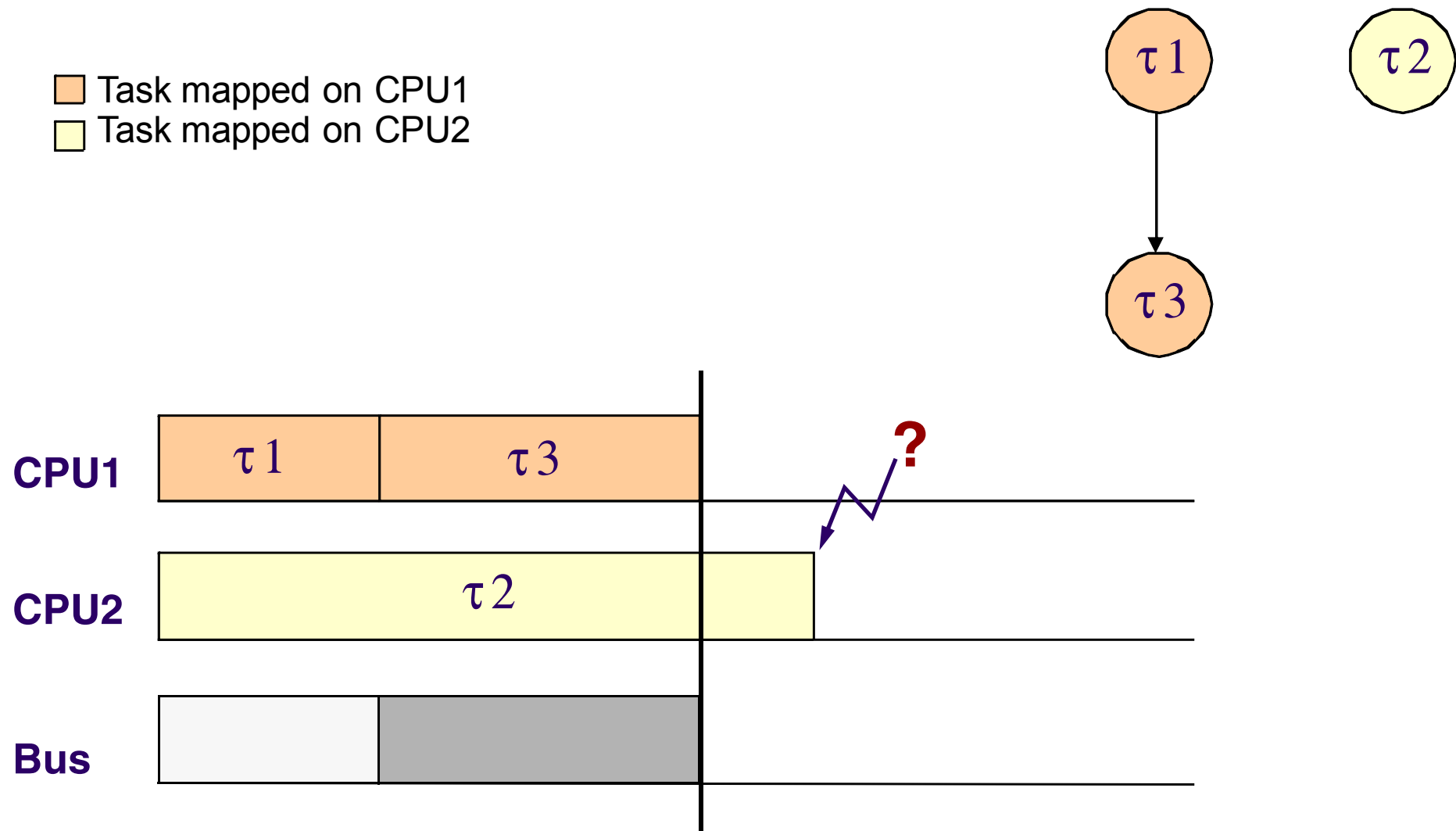
# The Big Picture: Example



# The Big Picture: Example



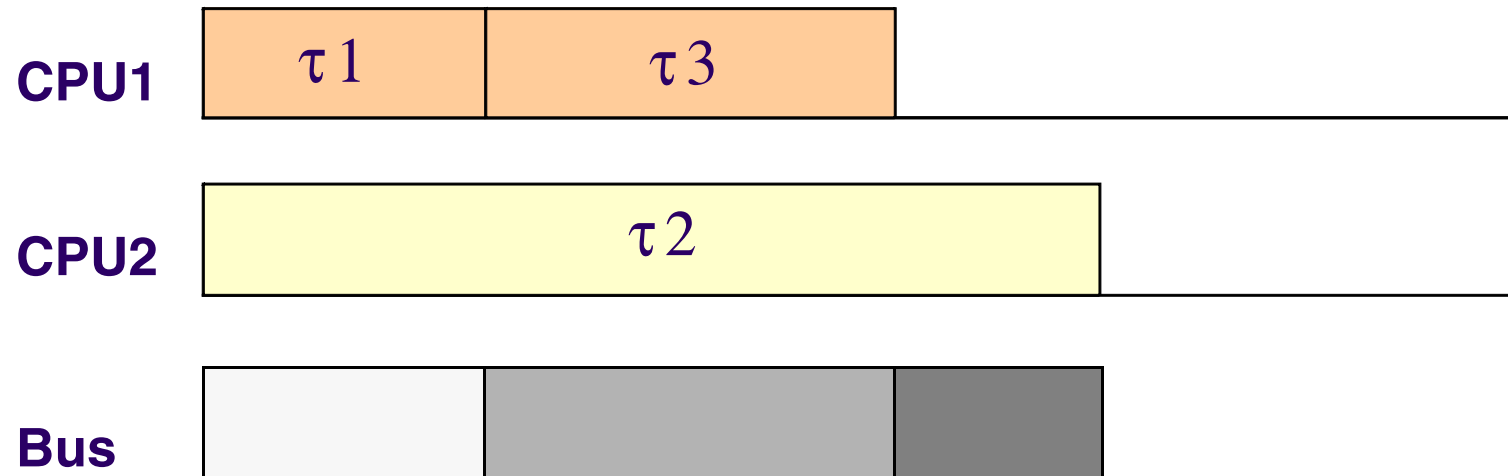
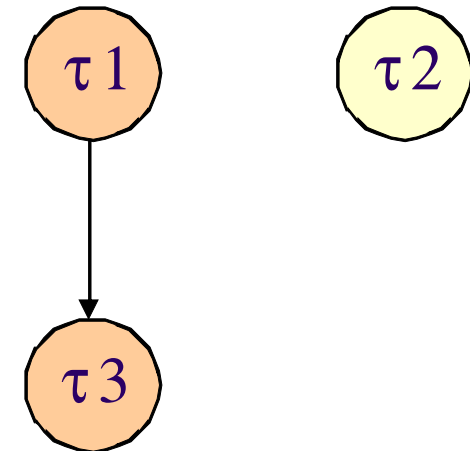
# The Big Picture: Example



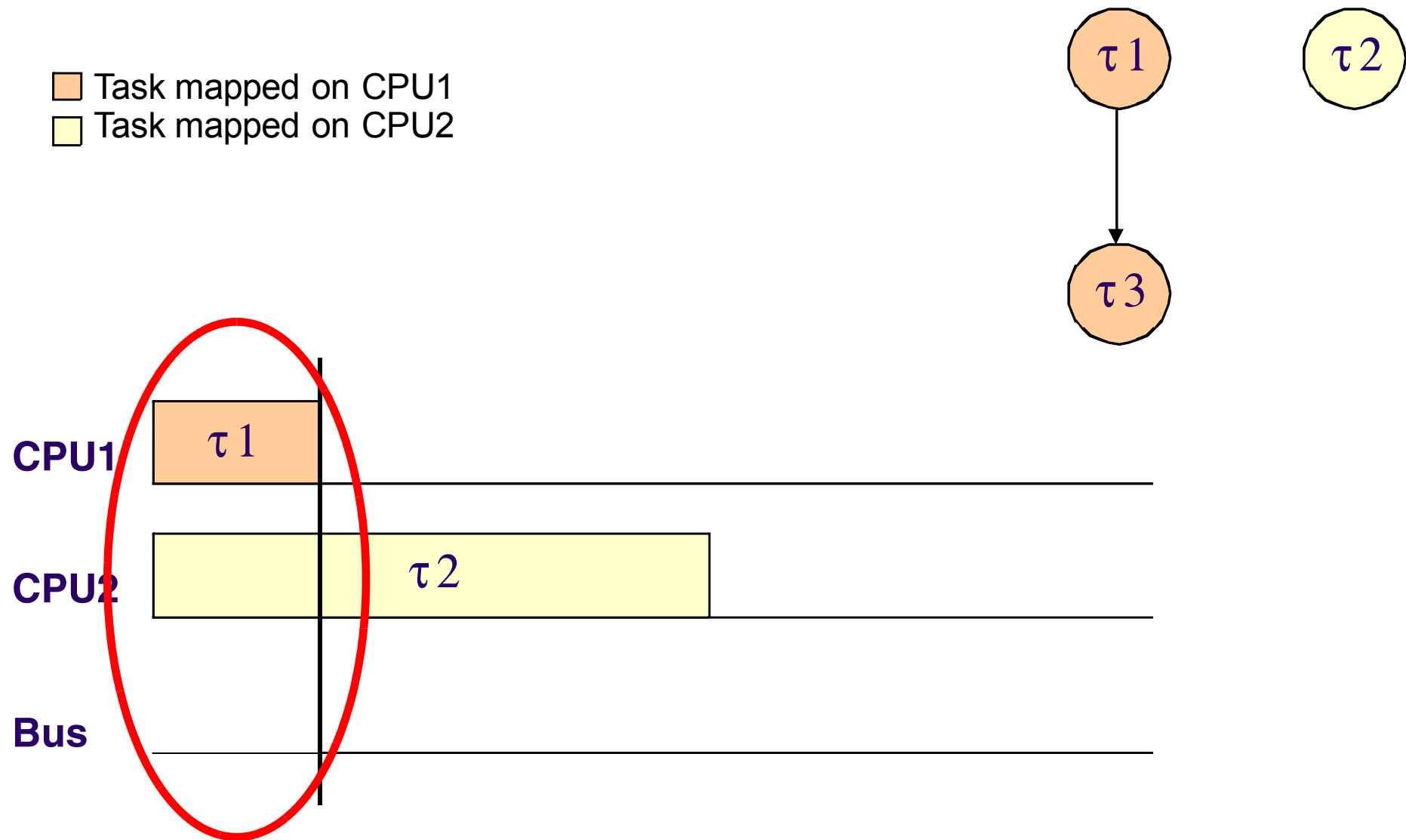
# The Big Picture: Example

- Task mapped on CPU1
- Task mapped on CPU2

**The final Bus and Task schedule**



# Bus Schedule Generation

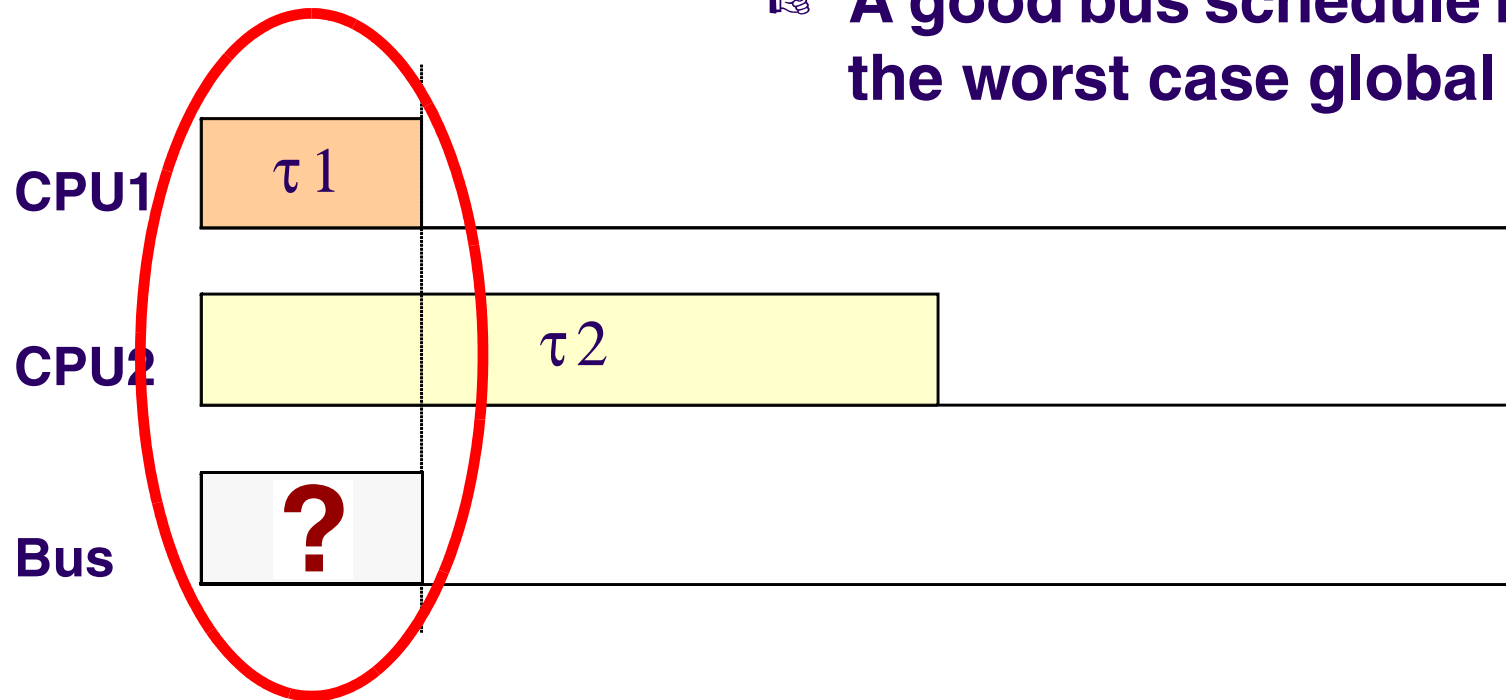


# Bus Schedule Generation

- Task mapped on CPU1
- Task mapped on CPU2

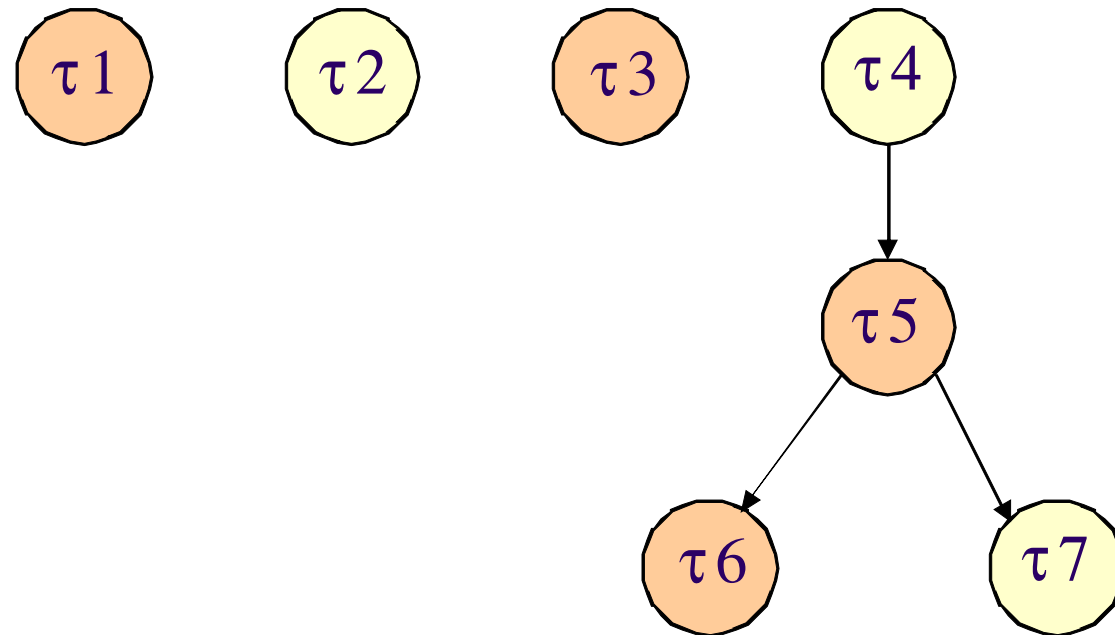
How do we find that “good” segment of bus schedule?

A good bus schedule minimizes the worst case global delay!



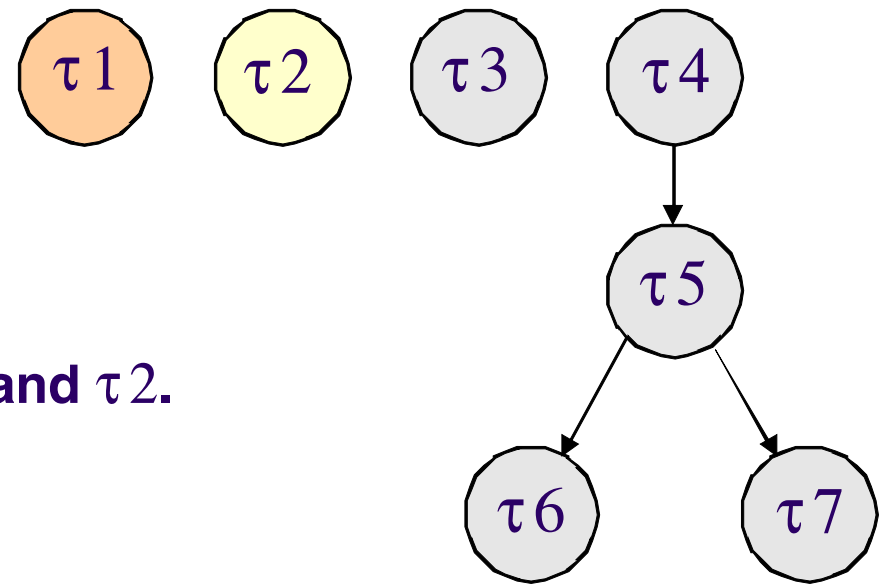
# Bus Schedule Generation

- Task mapped on CPU1
- Task mapped on CPU2



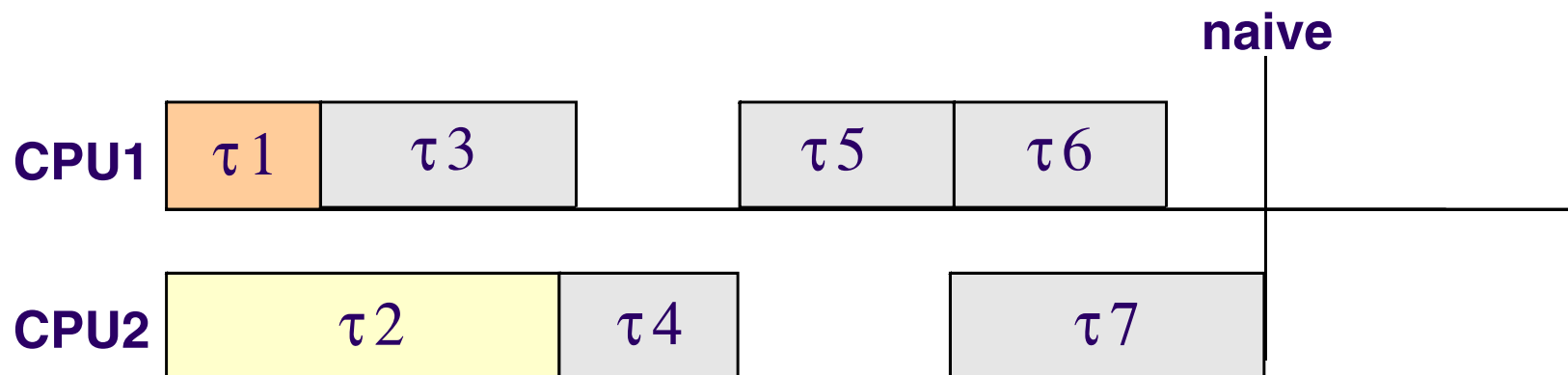


# Bus Schedule Generation

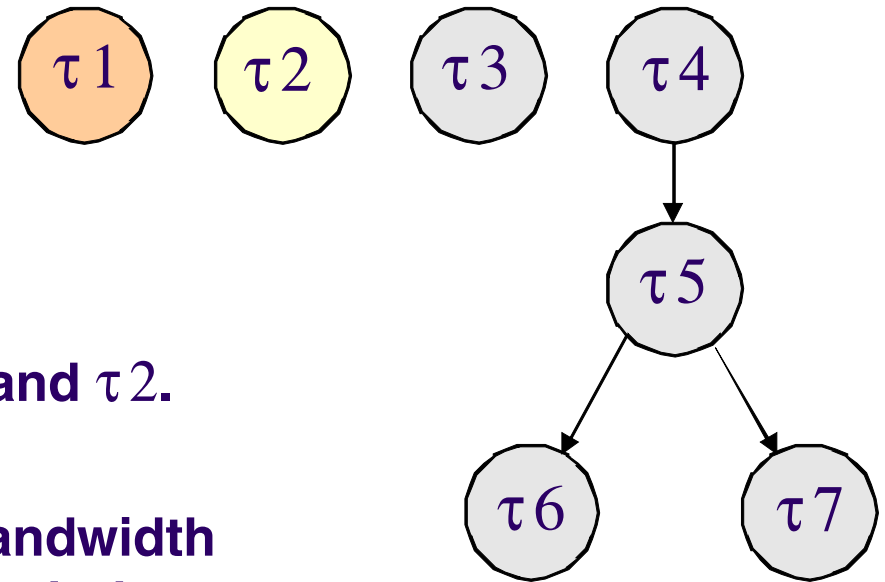


- Task being processed on CPU1
- Task being processed on CPU2
- Task not yet analyzed

☞ We are looking at tasks  $\tau_1$  and  $\tau_2$ .



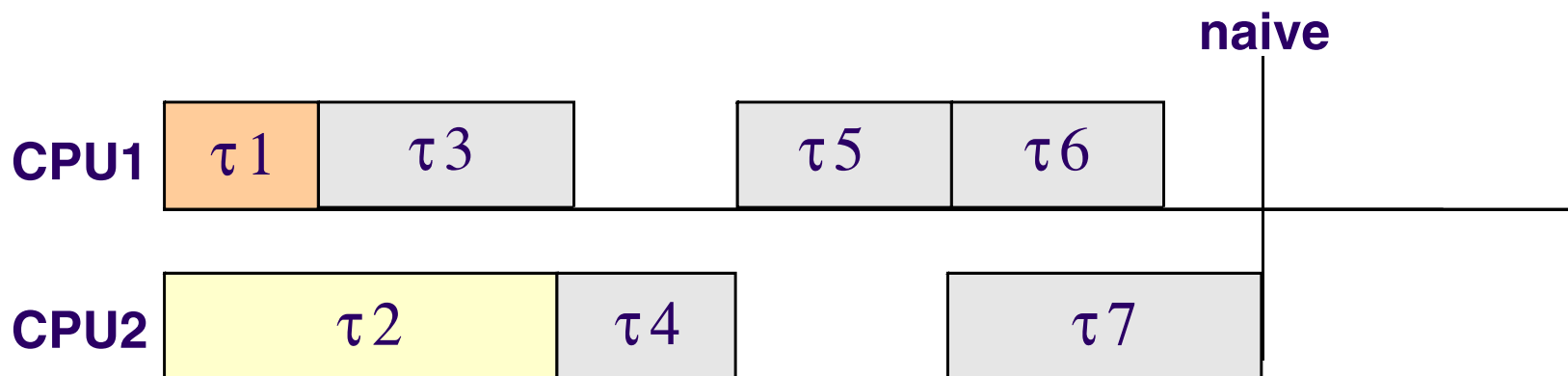
# Bus Schedule Generation



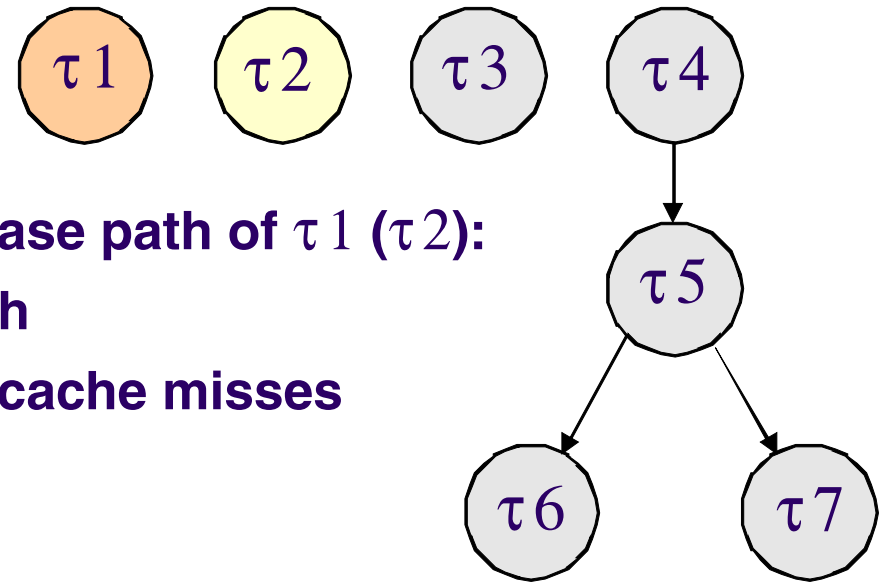
- Task being processed on CPU1
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☞ We are looking at tasks  $\tau_1$  and  $\tau_2$ .

☞ Question:  
How to distribute the bus bandwidth  
between CPU1 and CPU2 such that  
the global delay is reduced?

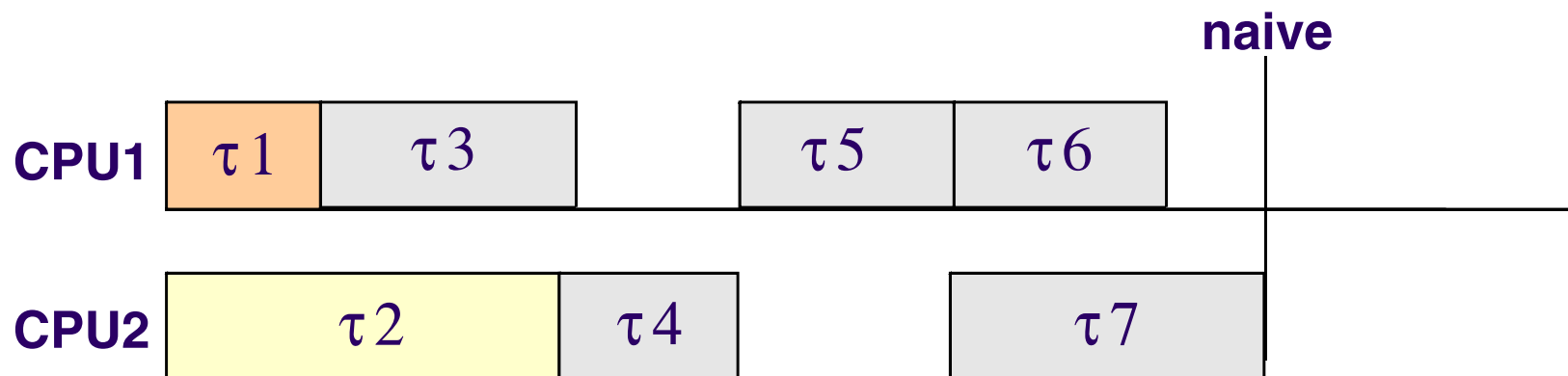


# Bus Schedule Generation

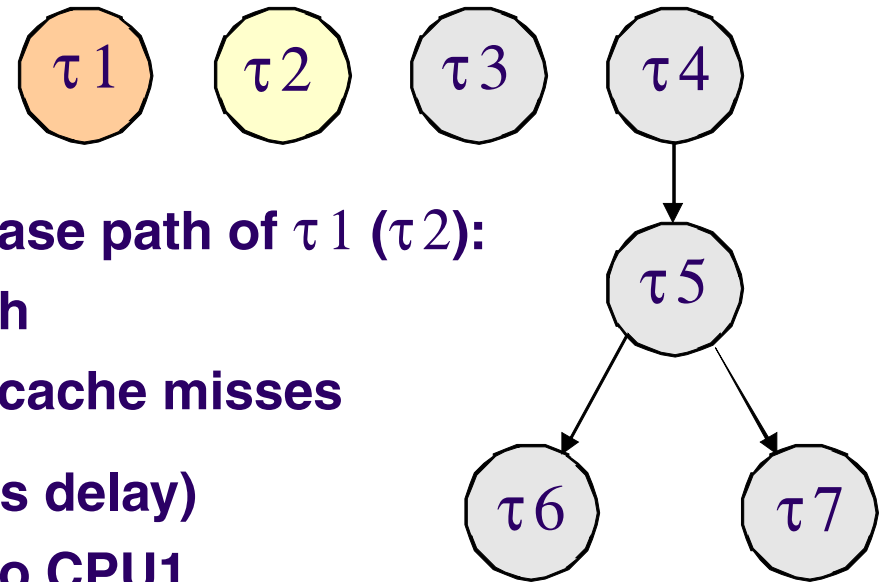


👉 **Traditional WCET analysis detects a worst case path of  $\tau_1$  ( $\tau_2$ ):**

- **$m1$ :** number of cash misses on this path
- **$l1$ :** total time spent on this path *except* cache misses



# Bus Schedule Generation



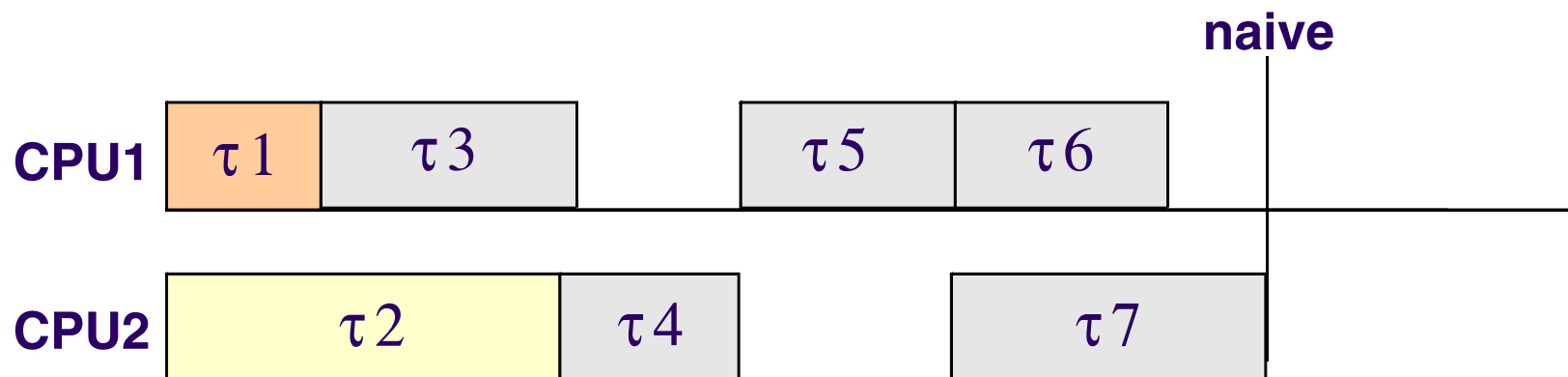
❏ **Traditional WCET analysis detects a worst case path of  $\tau_1$  ( $\tau_2$ ):**

- **$m_1$ : number of cache misses on this path**

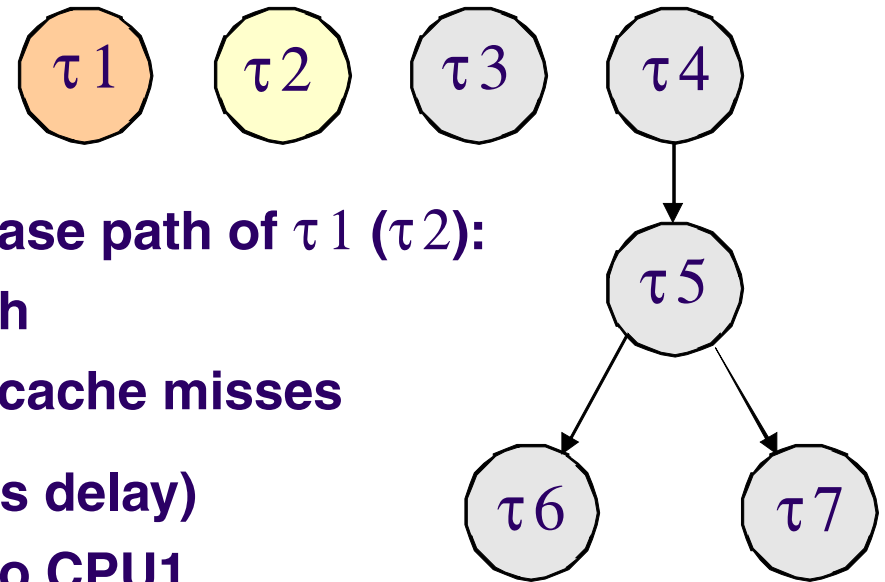
- **$l_1$ : total time spent on this path *except* cache misses**

- **$k$ : time needed to solve a cache miss (no bus delay)**

- **$p_1$ : percentage of bus bandwidth allocated to CPU1**



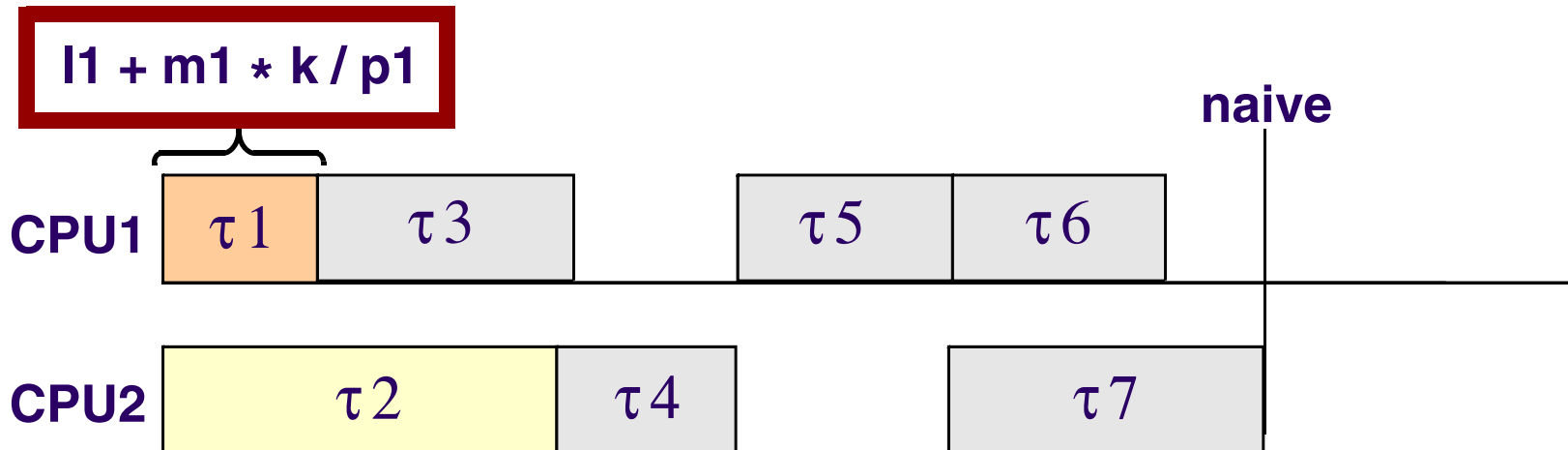
# Bus Schedule Generation



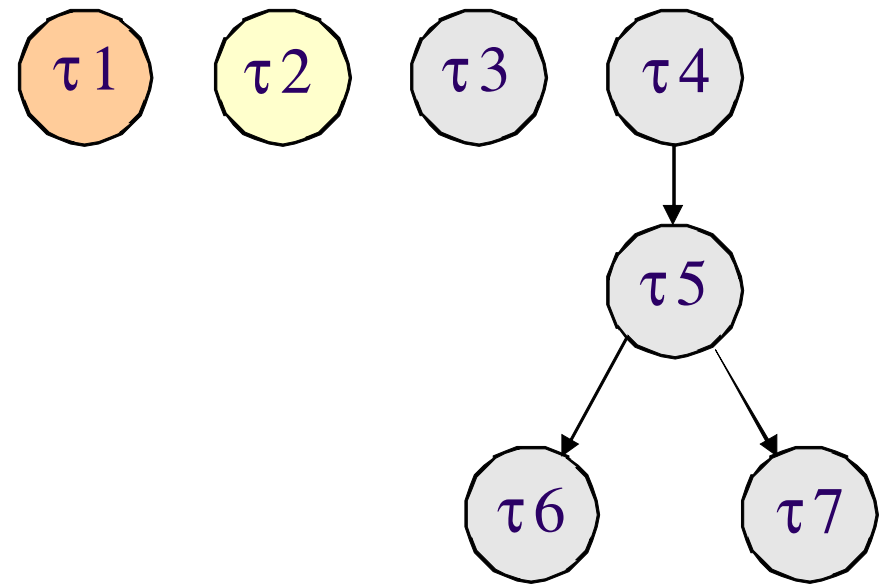
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- $p_1$ : percentage of bus bandwidth allocated to CPU1

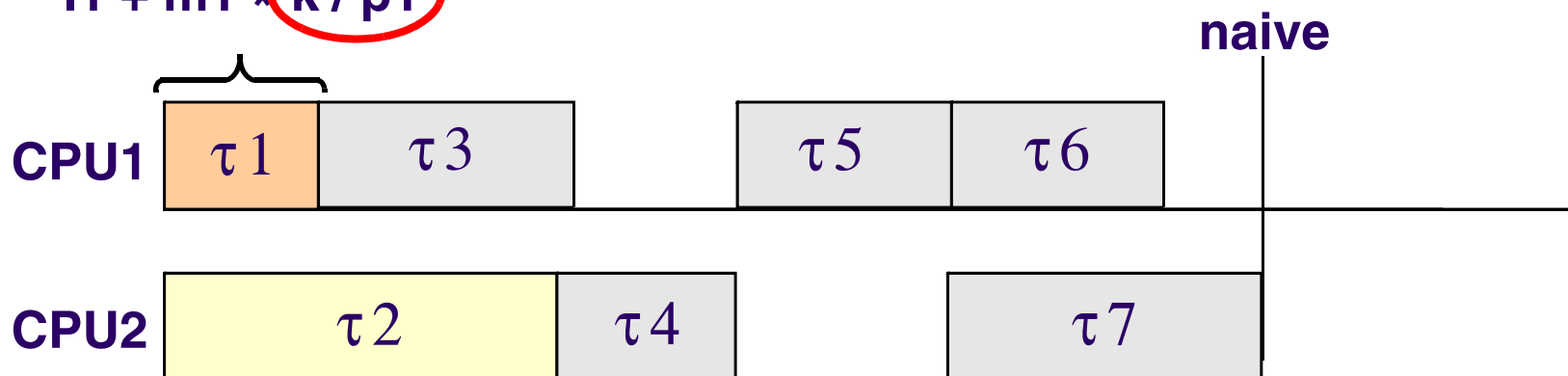


# Bus Schedule Generation

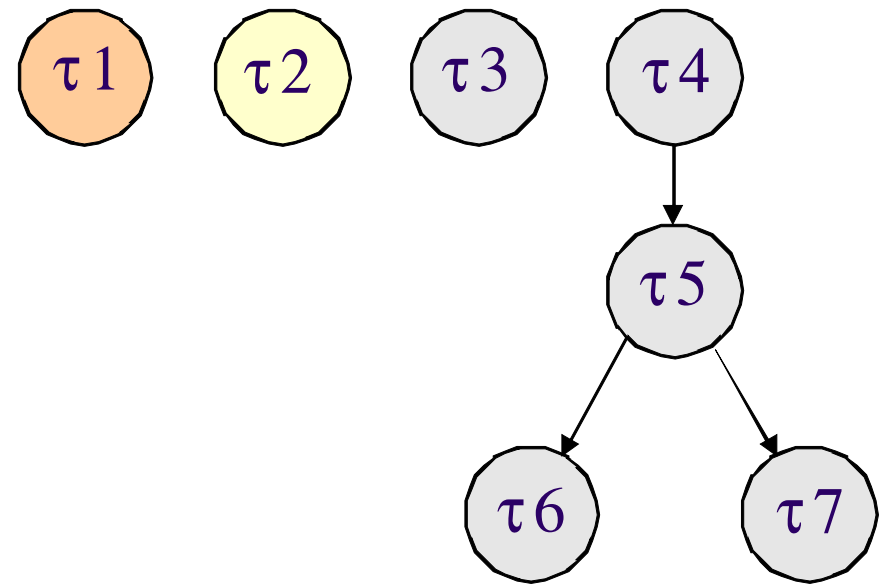


Average time to solve a cache miss

$$l1 + m1 * k / p1$$

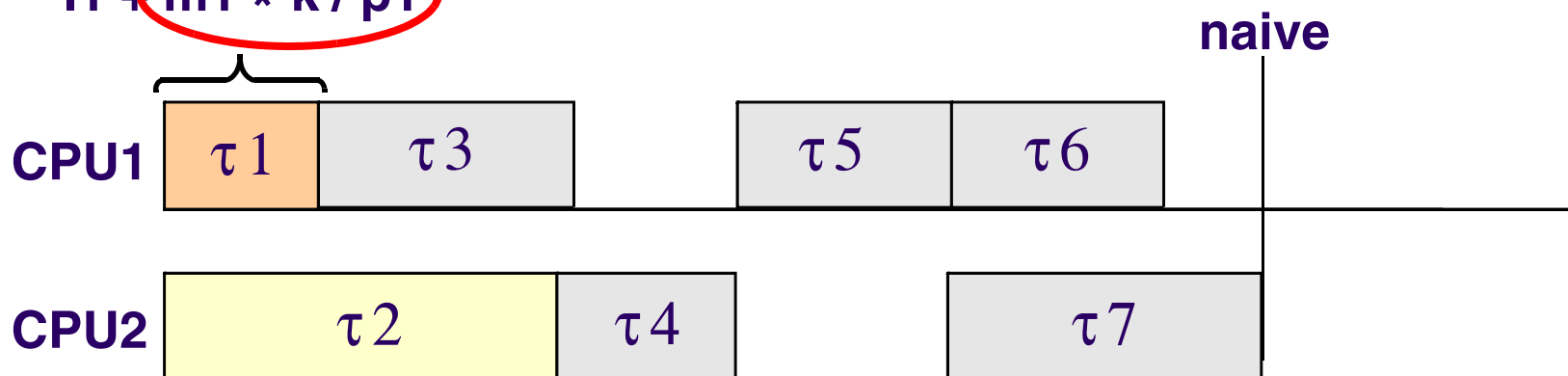


# Bus Schedule Generation

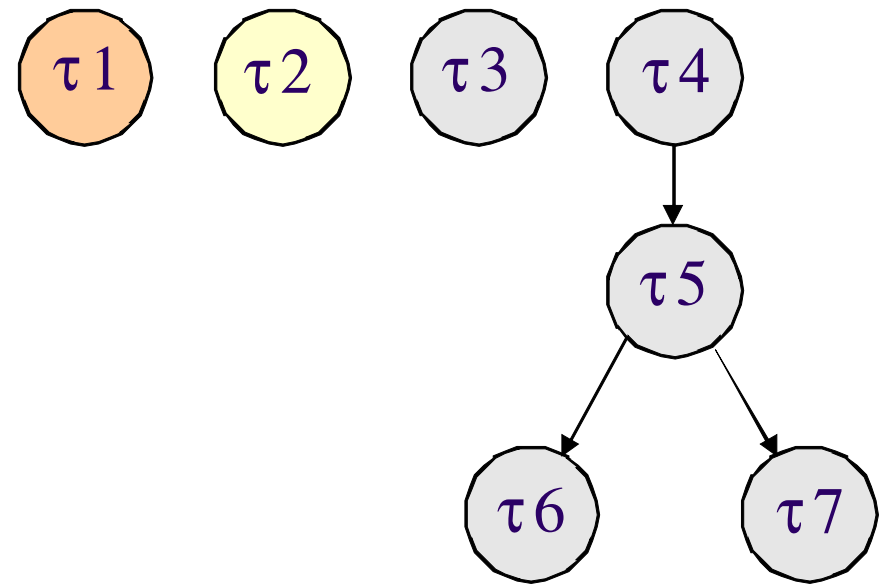


Total time to solve  
cache misses

$$l1 + m1 * k / p1$$

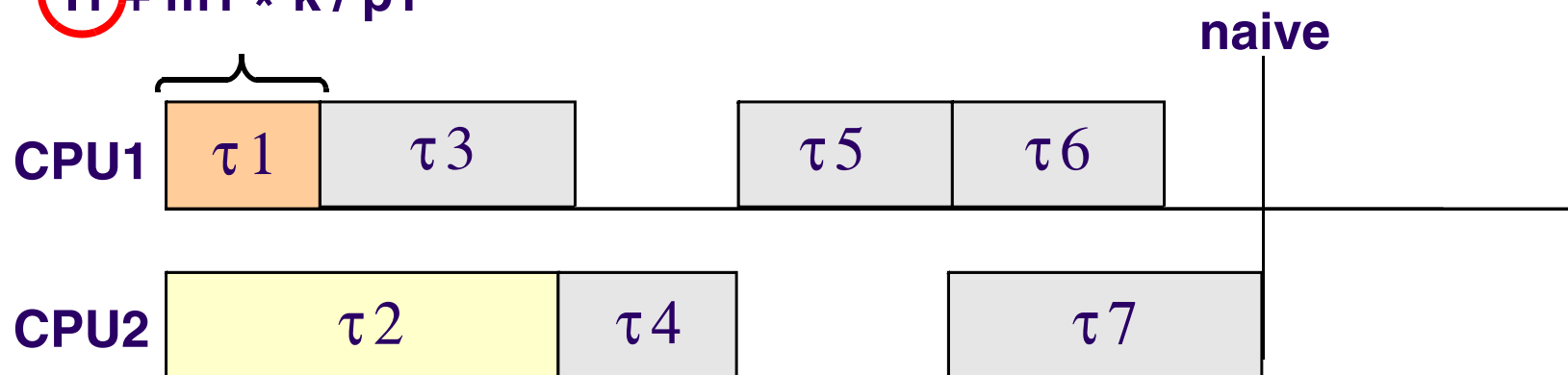


# Bus Schedule Generation



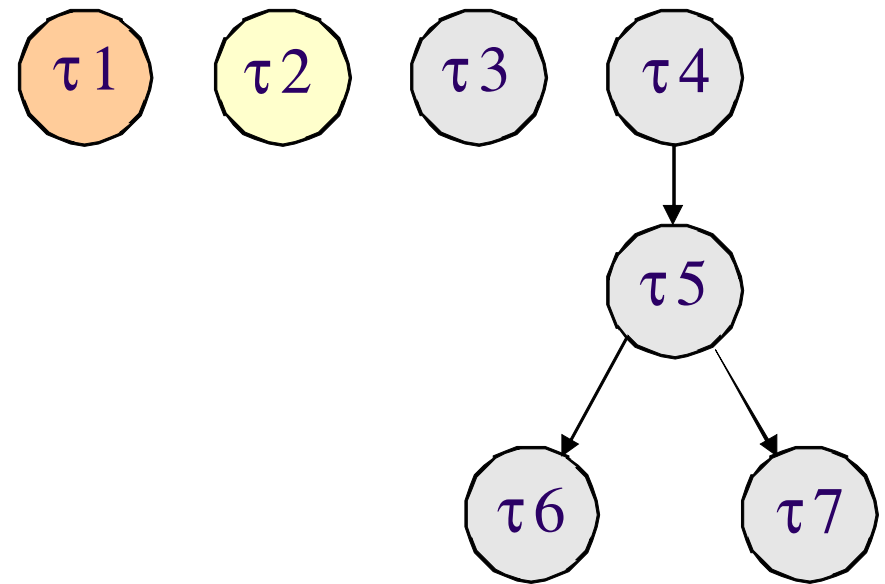
Ex. time, except  
cache misses

$\textcircled{l1} + m1 * k / p1$



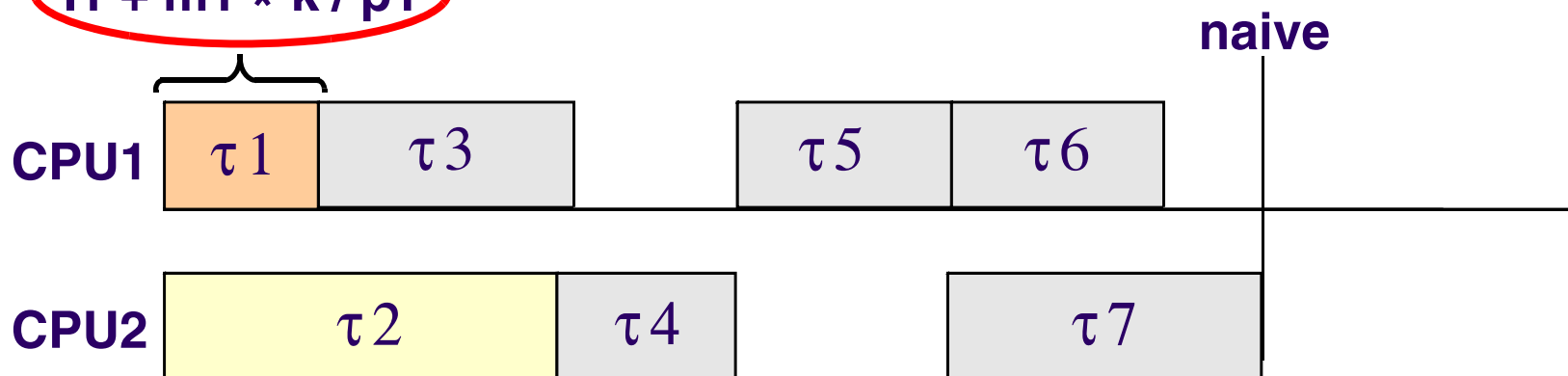


# Bus Schedule Generation



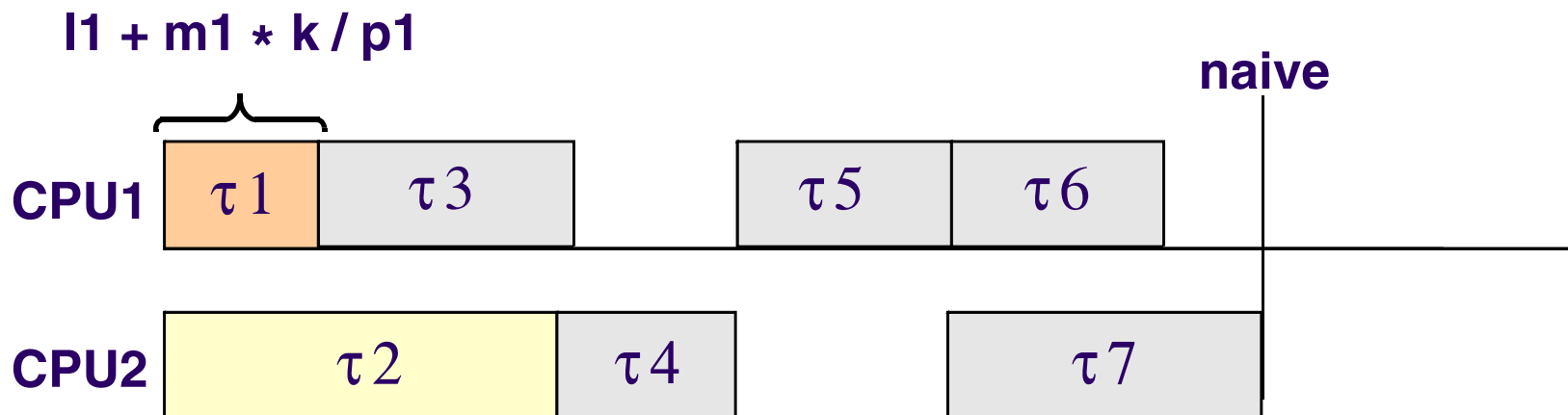
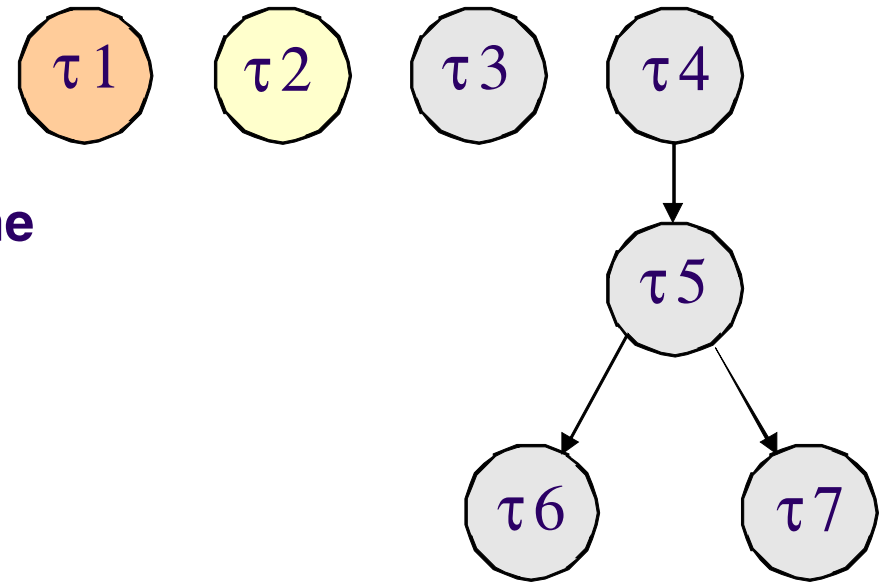
Estimated  
length of  $\tau_1$

$$l_1 + m_1 * k / p_1$$

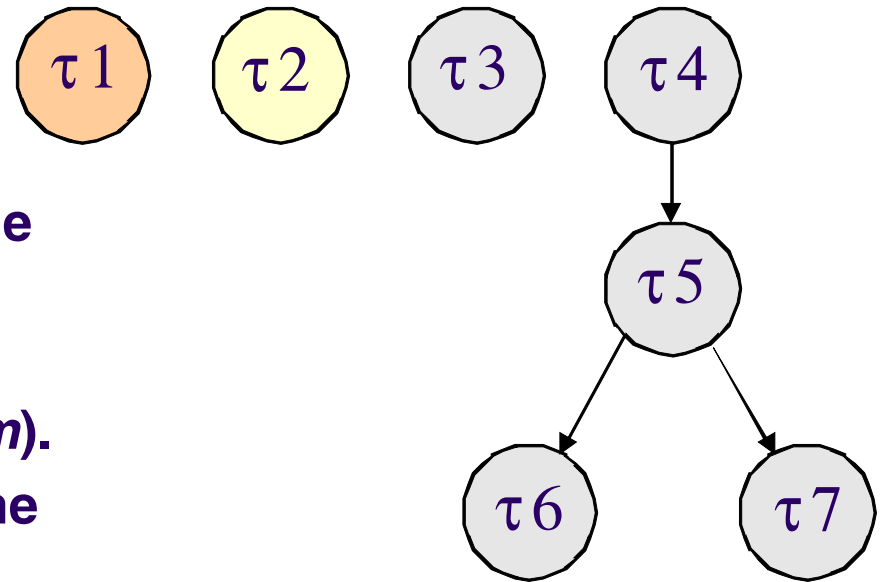


# Bus Schedule Generation

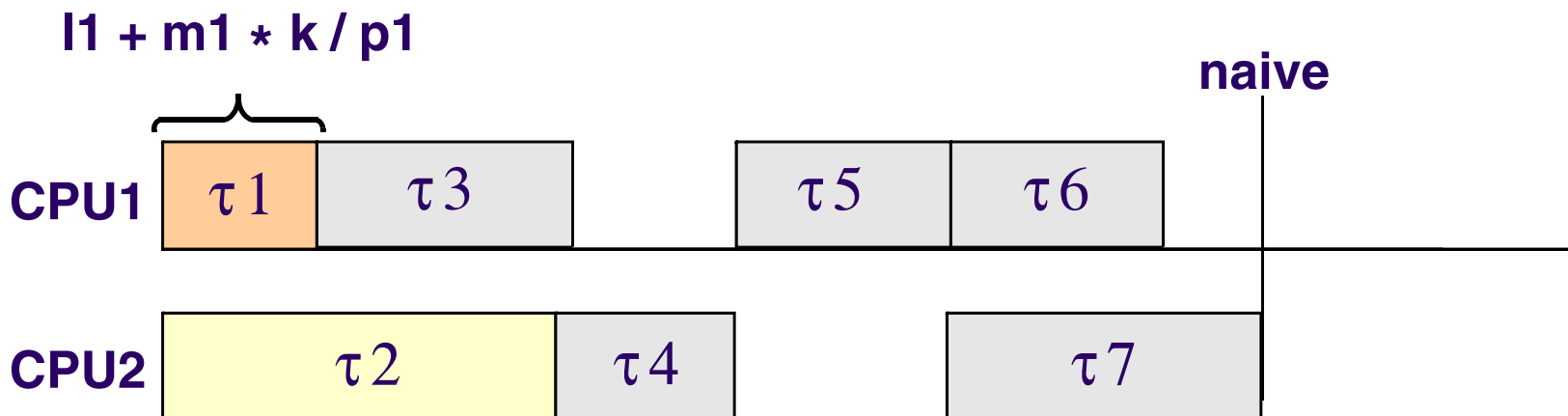
👉 **Question:**  
How to fix  $p1$  and  $p2$  such that the global delay is reduced?



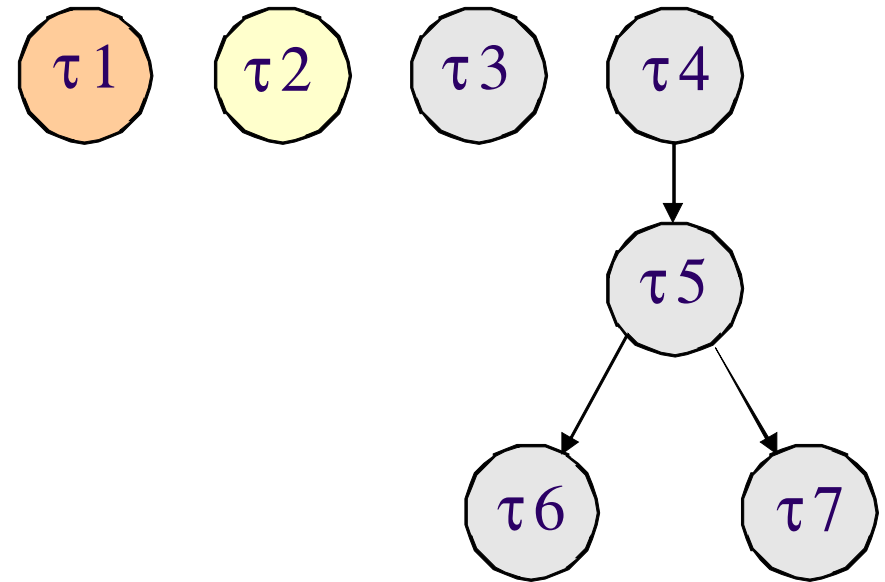
# Bus Schedule Generation



- 👉 **Question:**  
How to fix  $p1$  and  $p2$  such that the global delay is reduced?
- Give more bandwidth to the task with more cache misses (larger  $m$ ).
  - Tasks have different impact on the global delay!

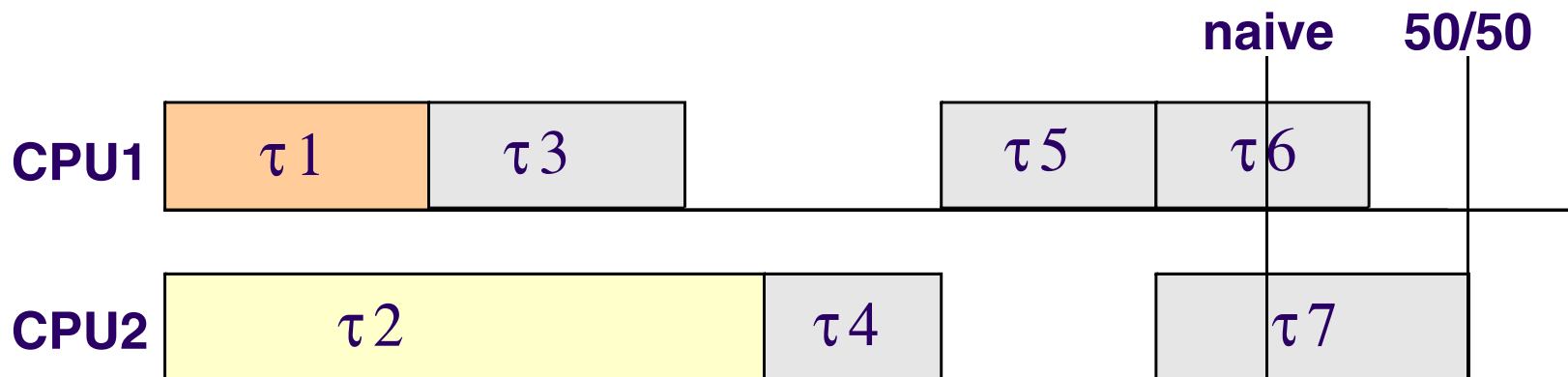
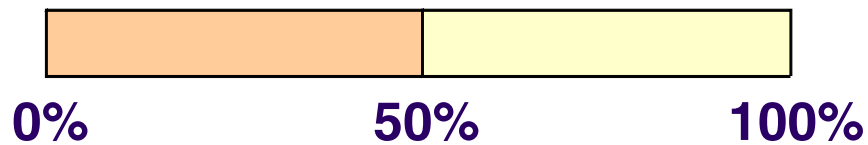


# Bus Schedule Generation

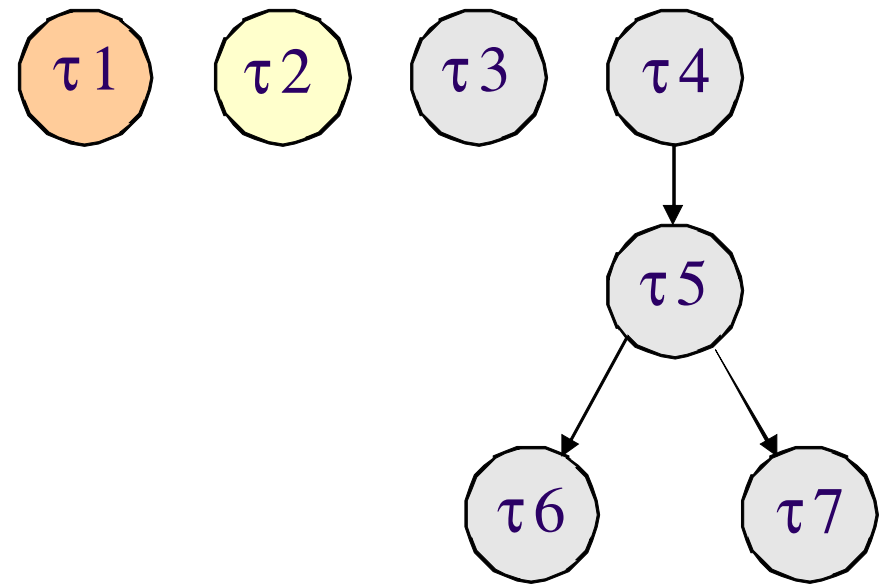


- Task being processed on CPU1
- Task being processed on CPU2
- Task not yet analyzed

## Bandwidth Distribution

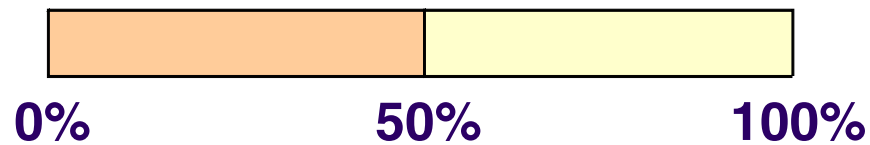


# Bus Schedule Generation

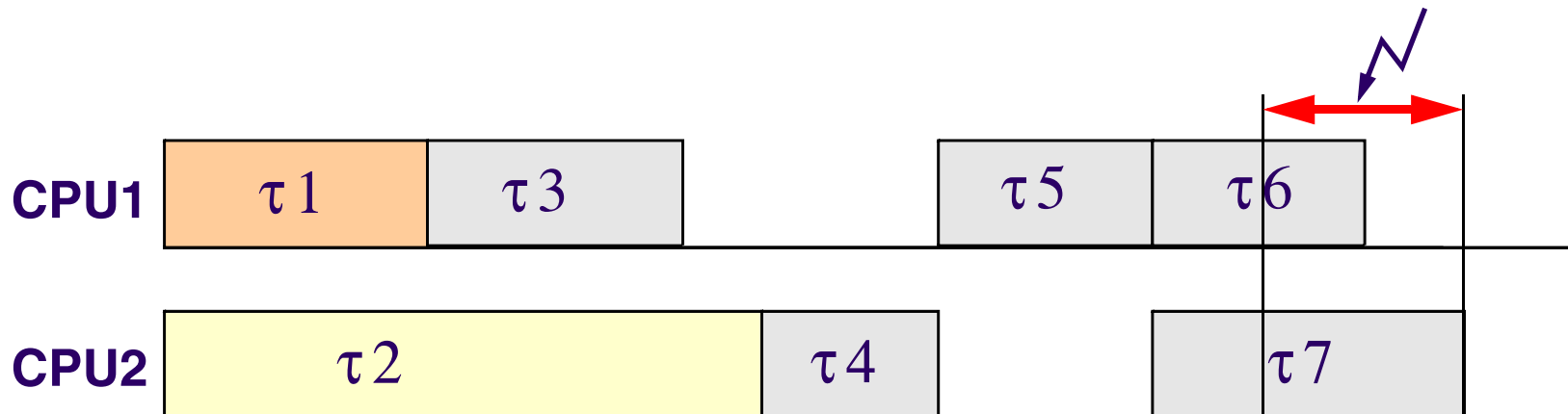


- Task being processed on CPU1
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- Task not yet analyzed

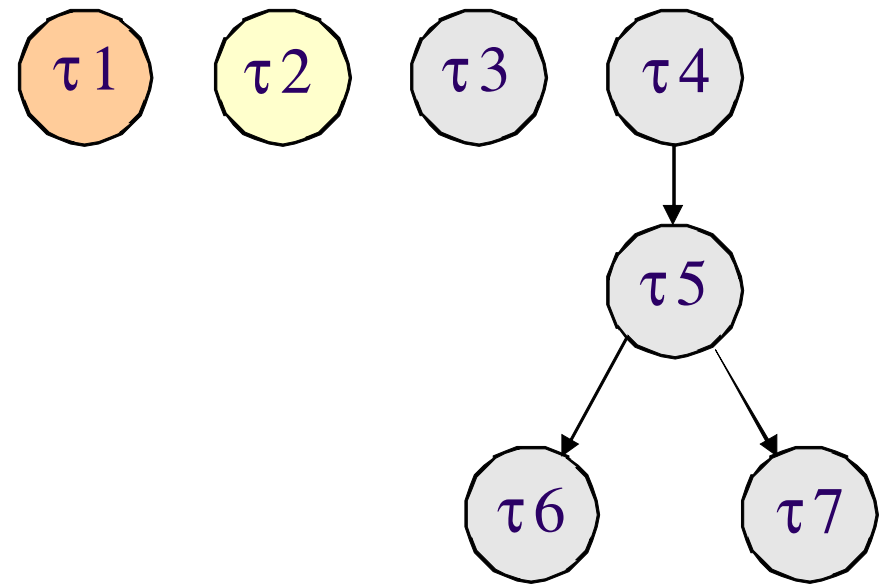
## Bandwidth Distribution



This has to be minimized

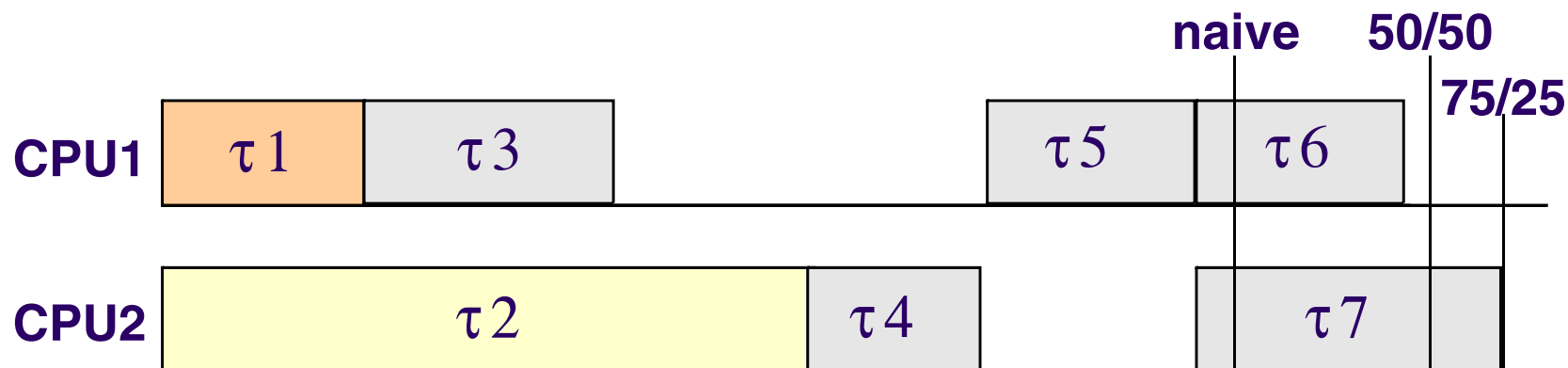


# Bus Schedule Generation

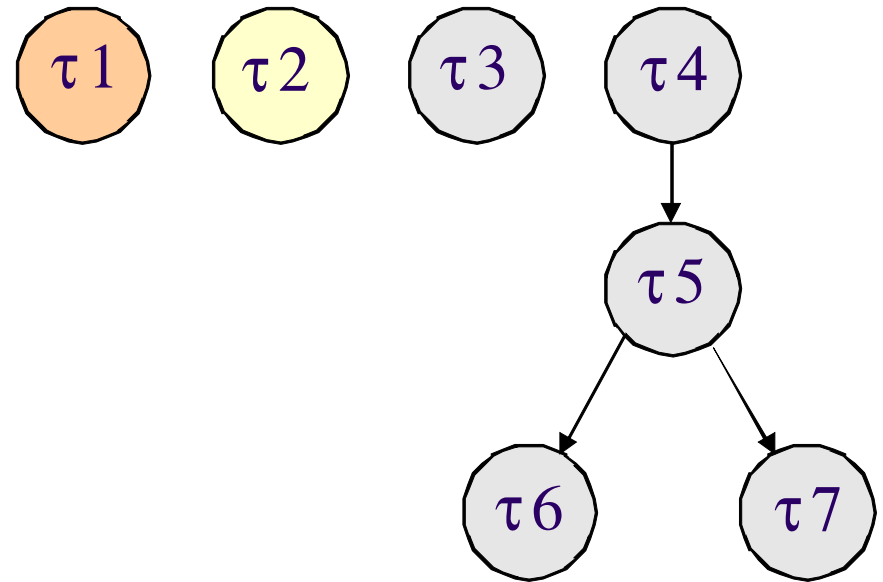


- Task being processed on CPU1
- Task being processed on CPU2
- Task not yet analyzed

## Bandwidth Distribution

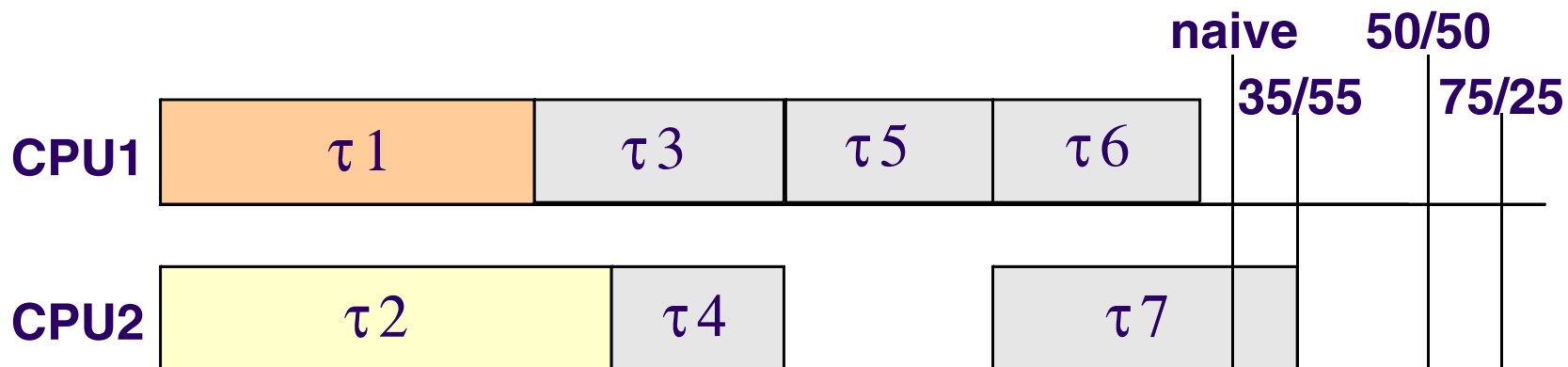
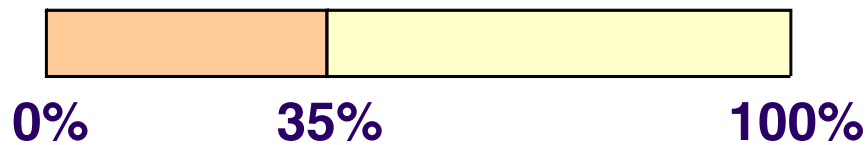


# Bus Schedule Generation

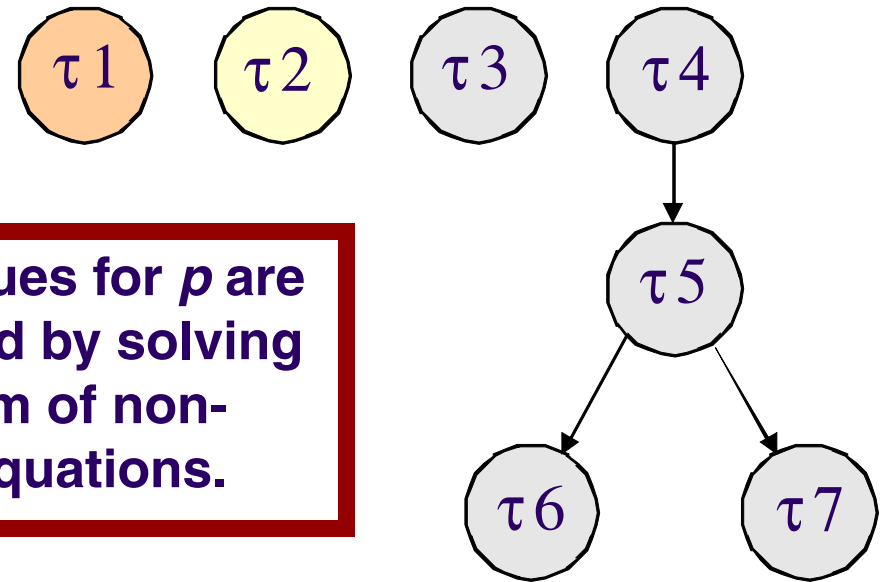


- Task being processed on CPU1
- Task being processed on CPU2
- Task not yet analyzed

## Bandwidth Distribution



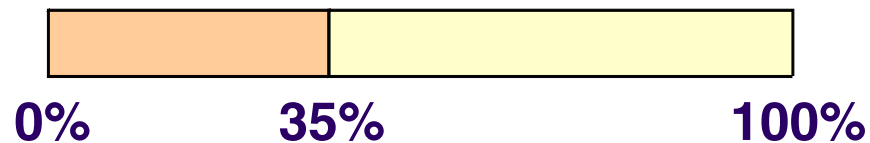
# Bus Schedule Generation



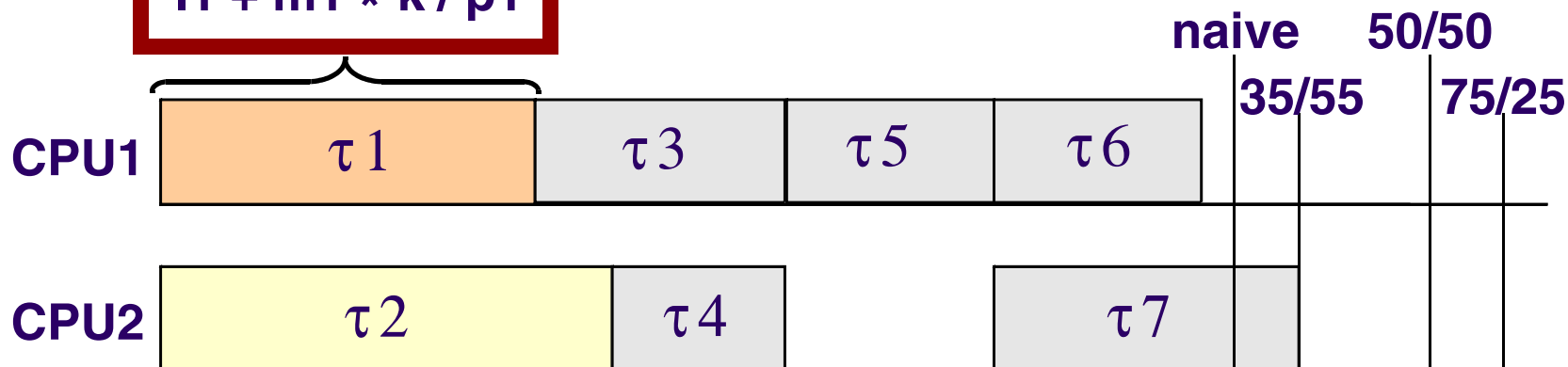
- Task being processed on CPU1
- Task being processed on CPU2
- Task not yet analyzed

The values for  $p$  are obtained by solving a system of non-linear equations.

## Bandwidth Distribution

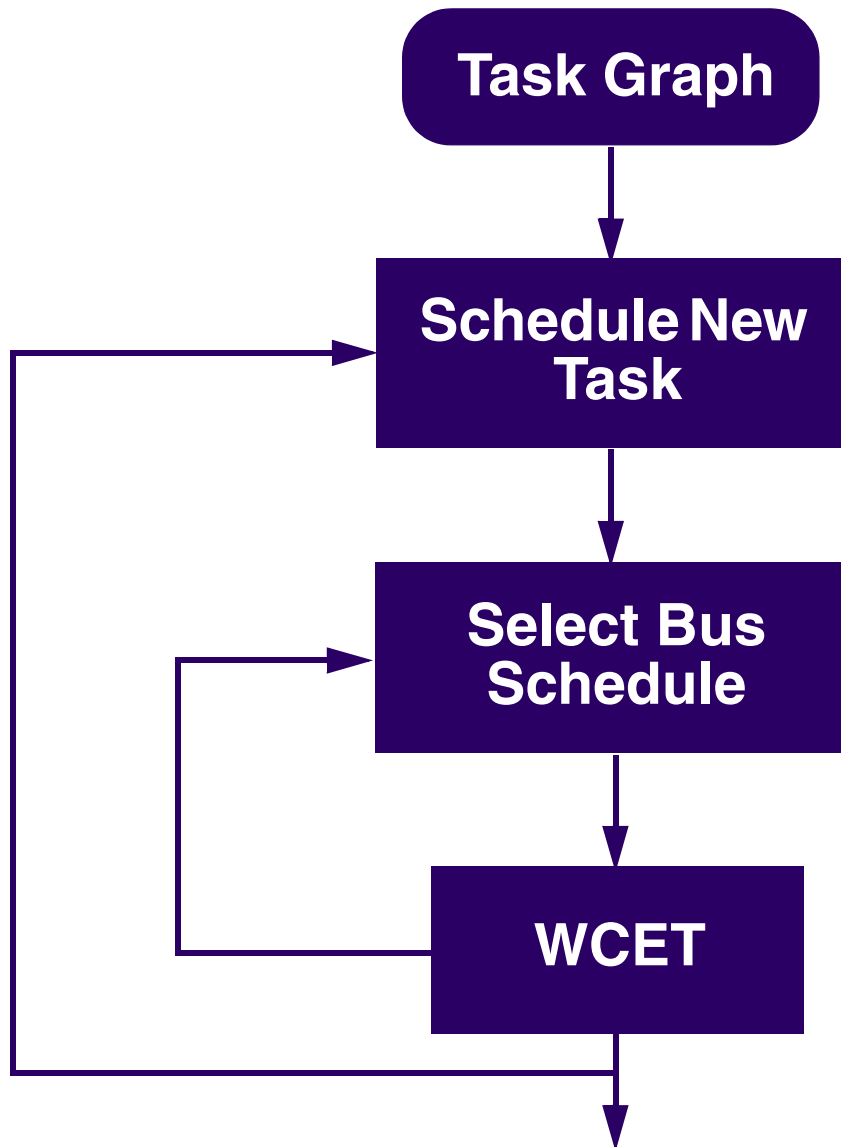


$$l1 + m1 * k / p1$$





# Bus Schedule Generation

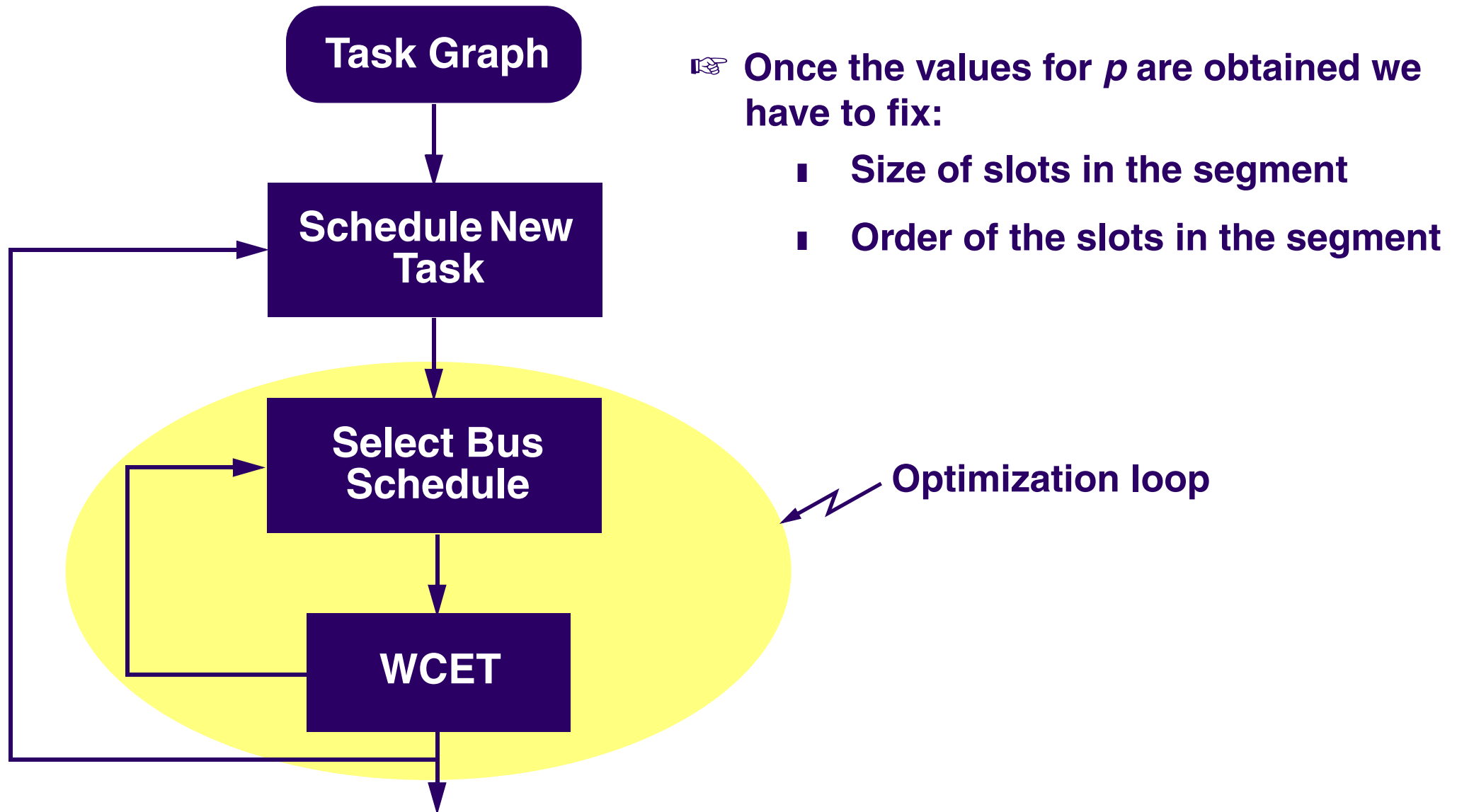


☞ Once the values for  $p$  are obtained we have to fix:

- Size of slots
- Order of the slots



# Bus Schedule Generation





- When calculating the bandwidth distributions  $p$  we have assumed that misses are uniformly distributed throughout the task's critical path.

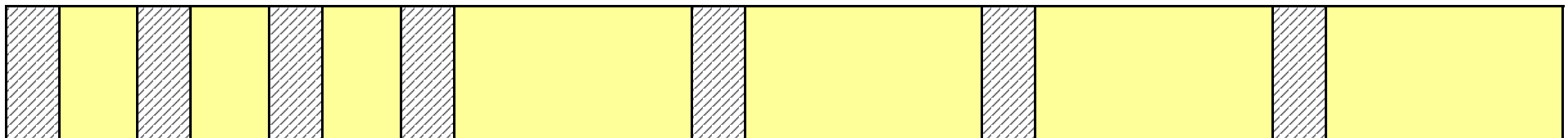




- When calculating the bandwidth distributions  $p$  we have assumed that misses are uniformly distributed throughout the task's critical path.

☞ In reality this is NOT the case.

Task  $\tau_j$

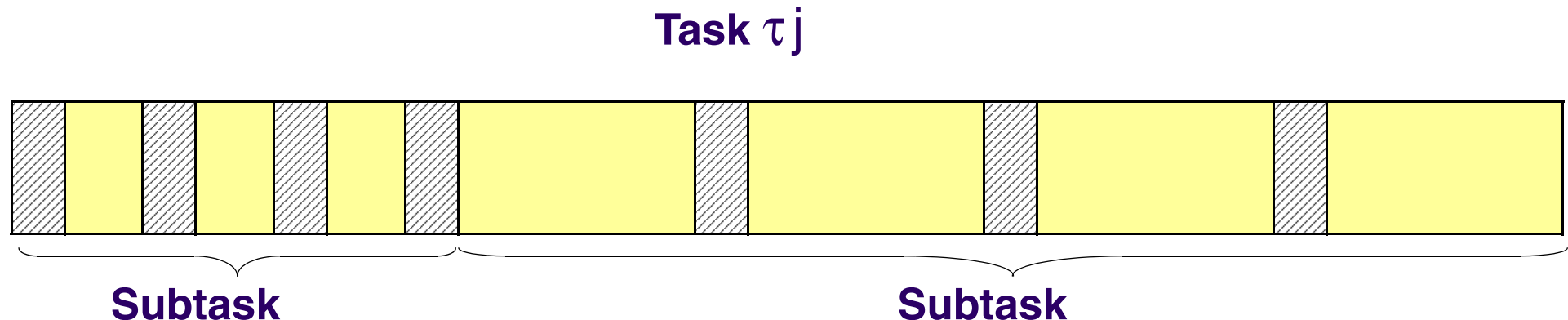




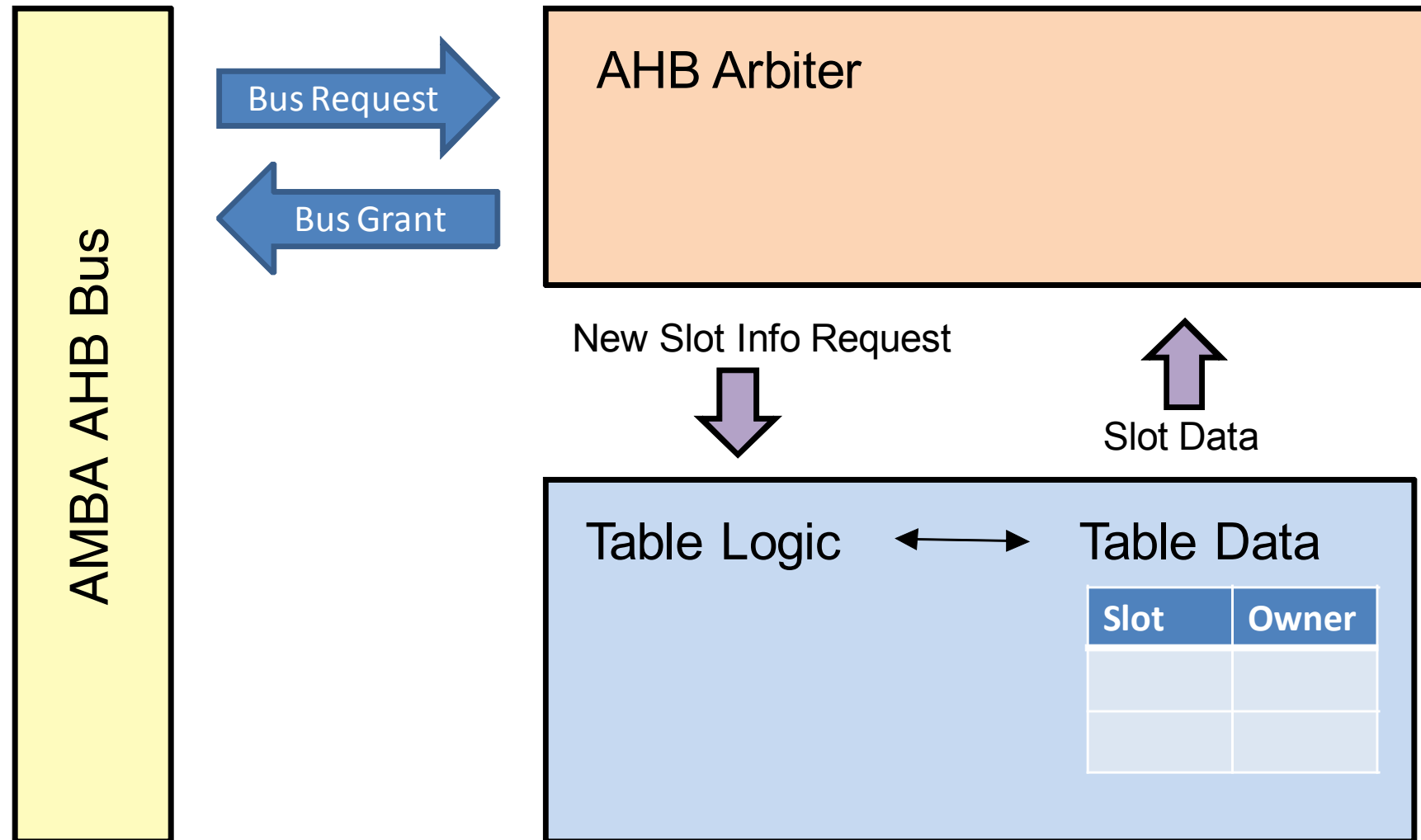
- When calculating the bandwidth distributions  $p$  we have assumed that misses are uniformly distributed throughout the task's critical path.

☞ In reality this is NOT the case.

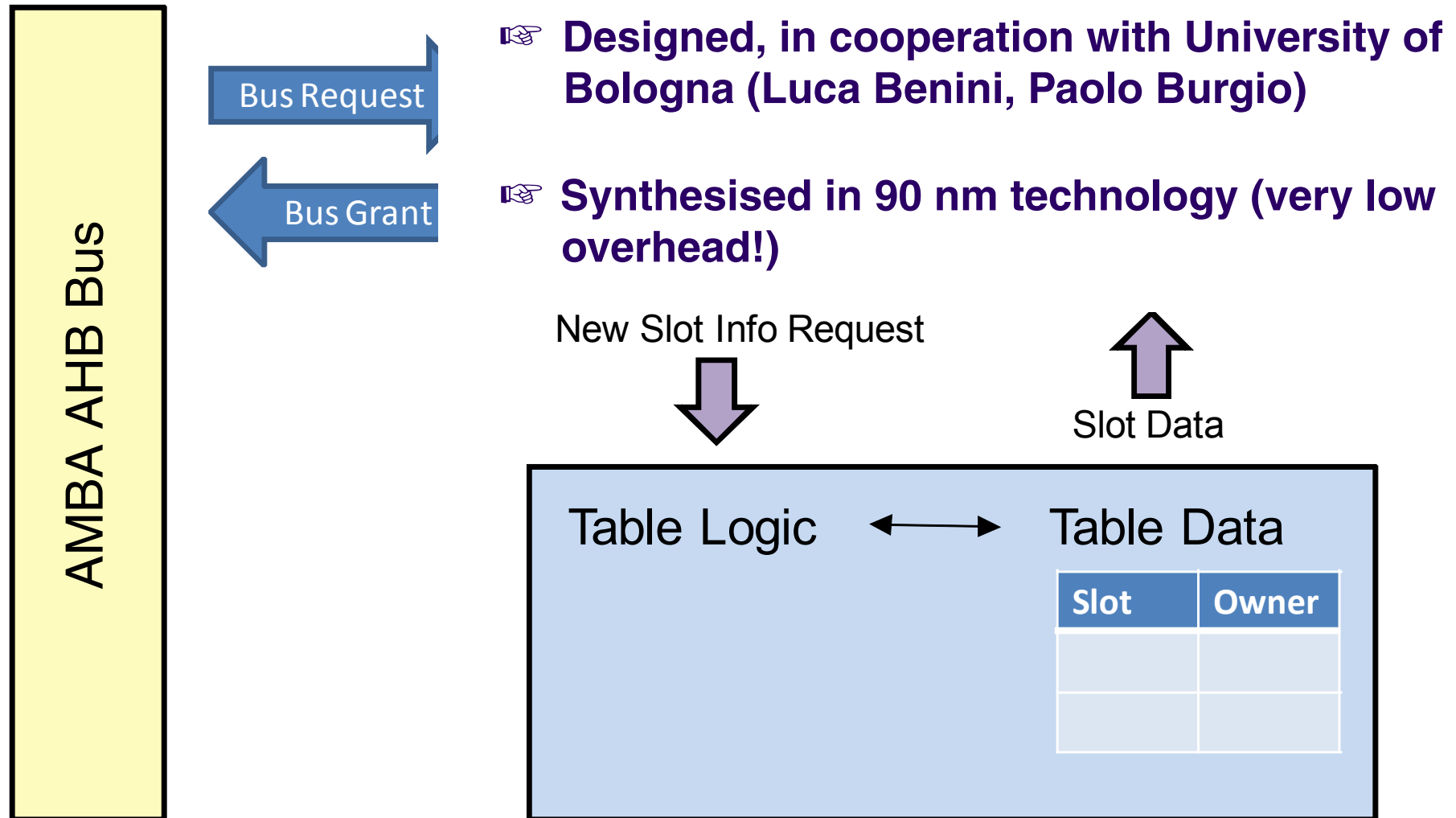
- We divide a task into subtasks according to *density regions*.

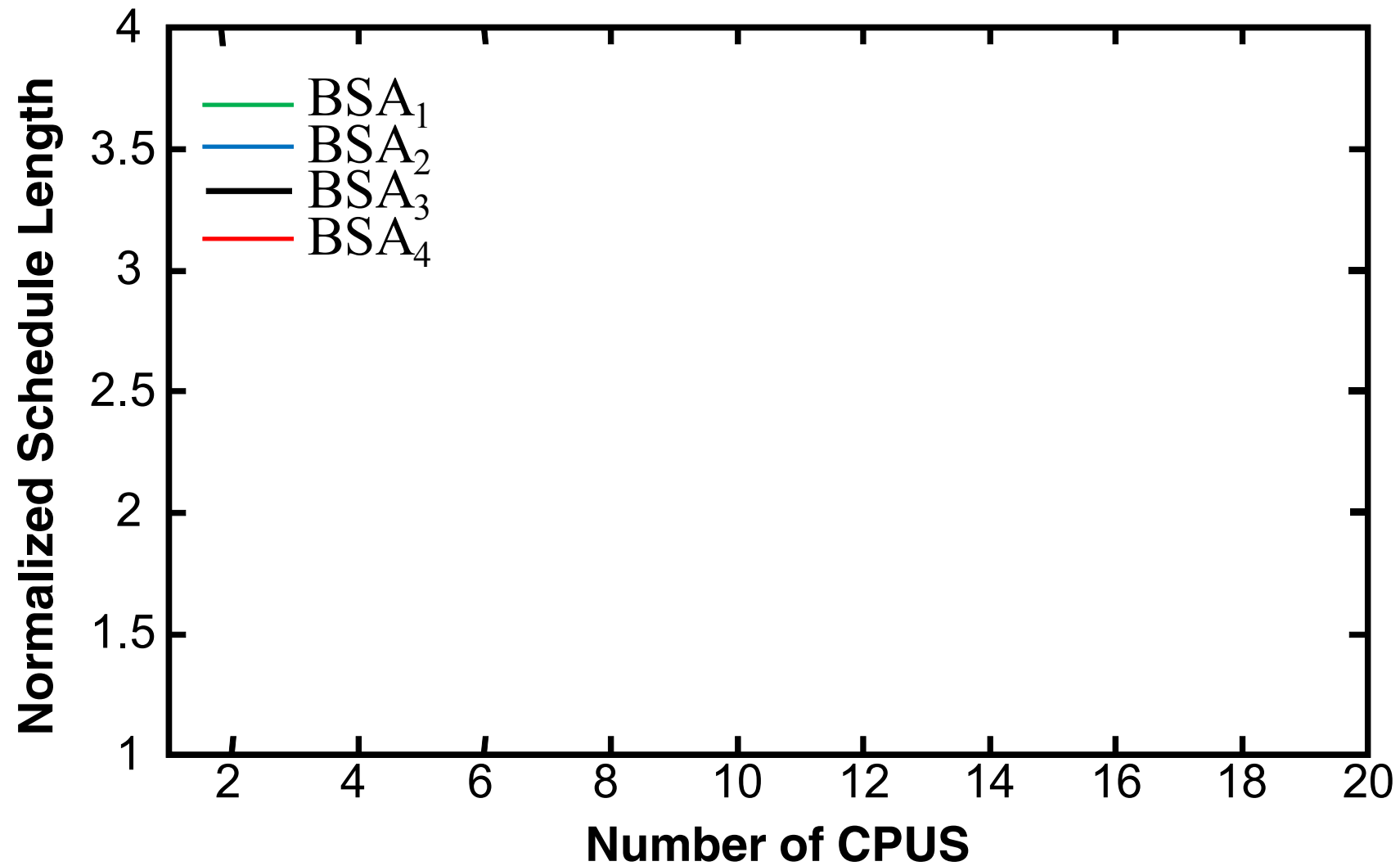


# The Bus Arbiter

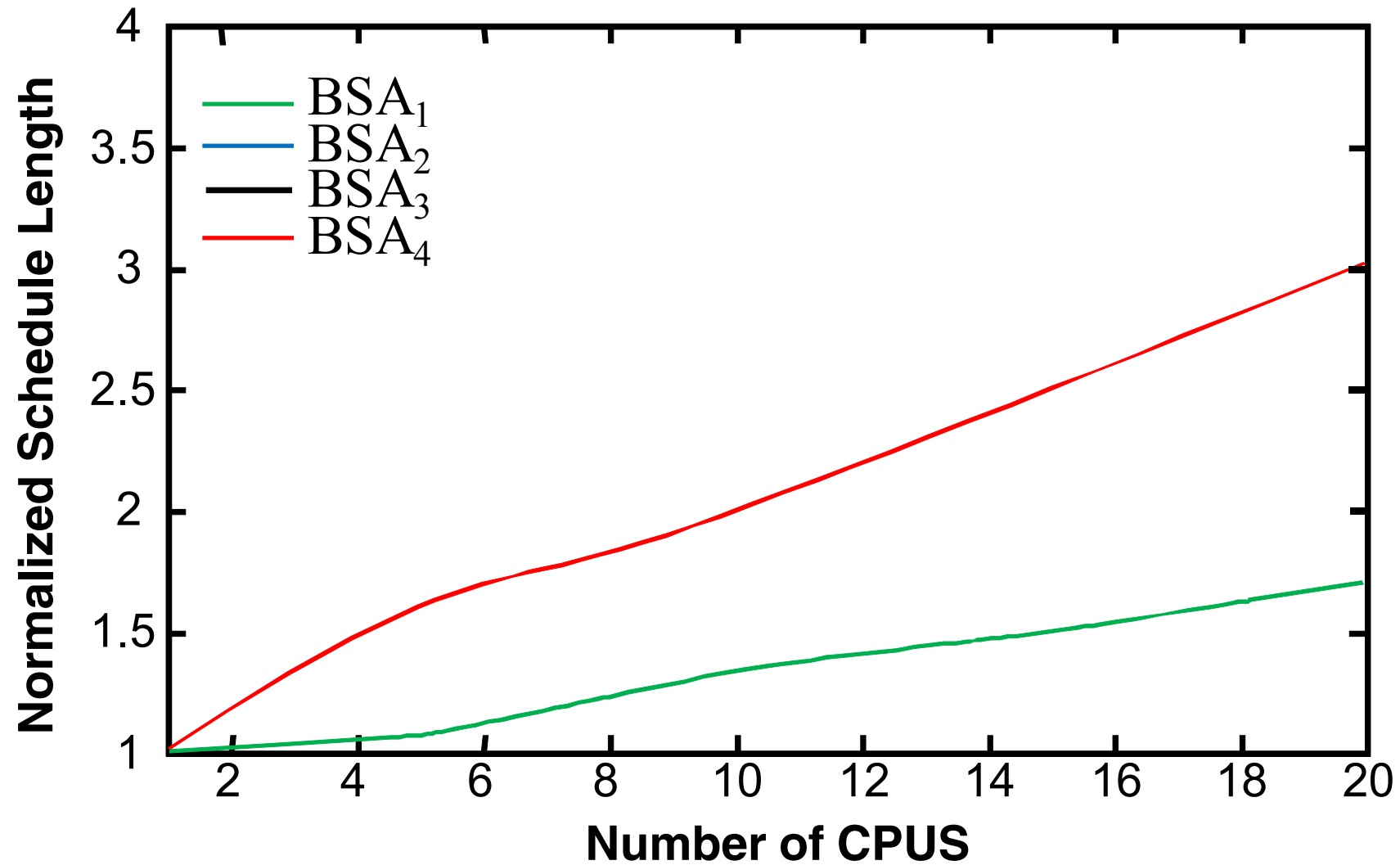


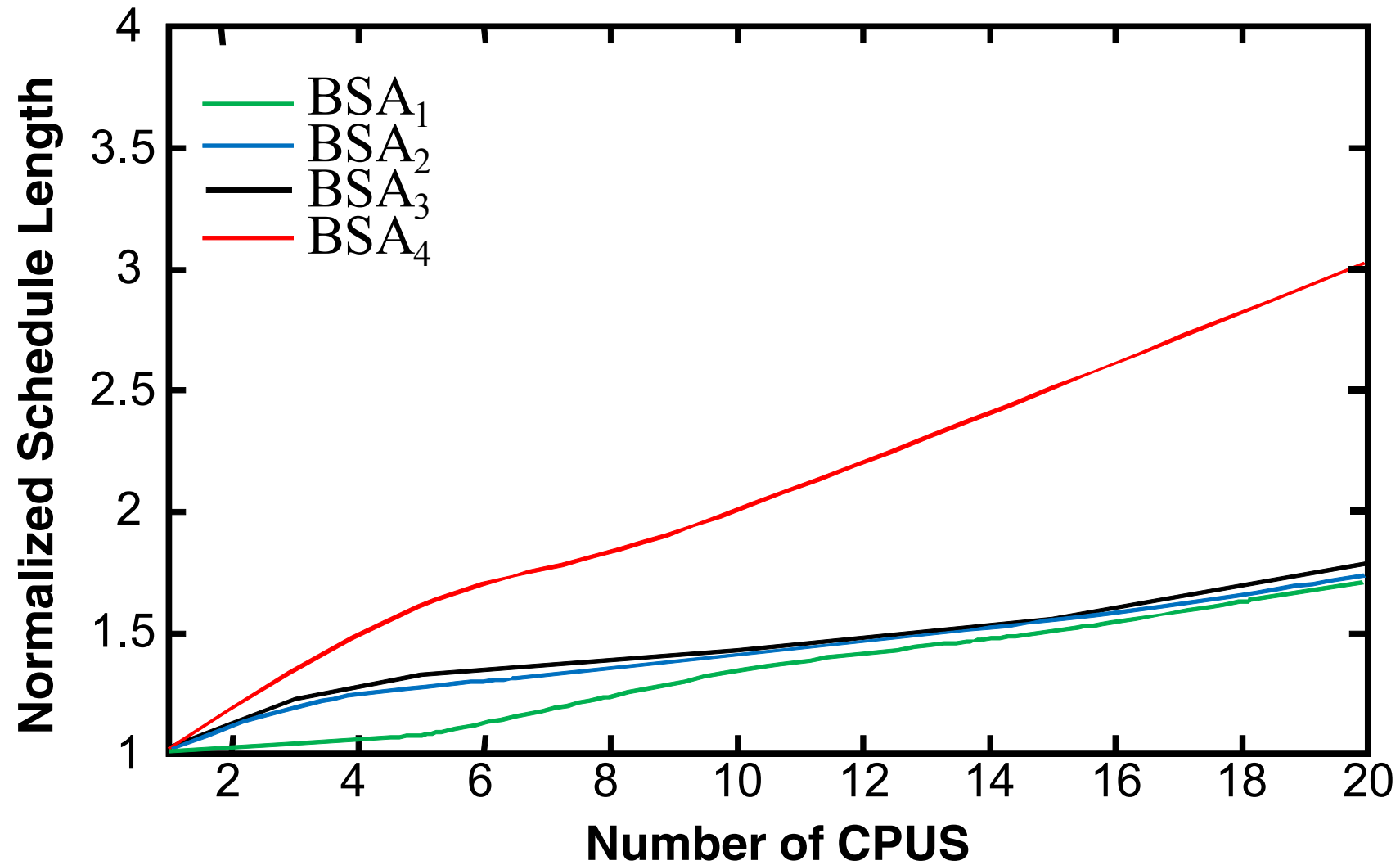
# The Bus Arbiter











- **An Approach to Predictable Implementation on Multiprocessors**
  - **TDMA Bus Schedule**
  - **WCET Analysis with TDMA**
  - **Bus schedule generation**



- **An Approach to Predictable Implementation on Multiprocessors**
  - **TDMA Bus Schedule**
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**Predictable implementation on MPSoC  
is possible without excessive overhead.**

