

A Problem of Time vs. Density Tradeoff in Multicore Fluid Scheduling

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Fluid Scheduling

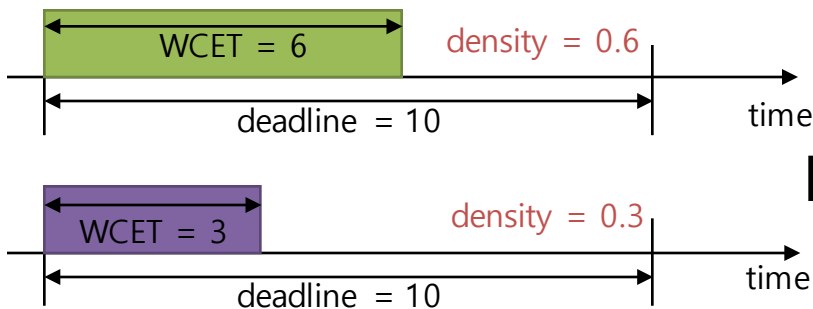
Fluid Scheduling

- Based on P-Fair (Proportionate Fairness)
- Schedule tasks proportional to their density

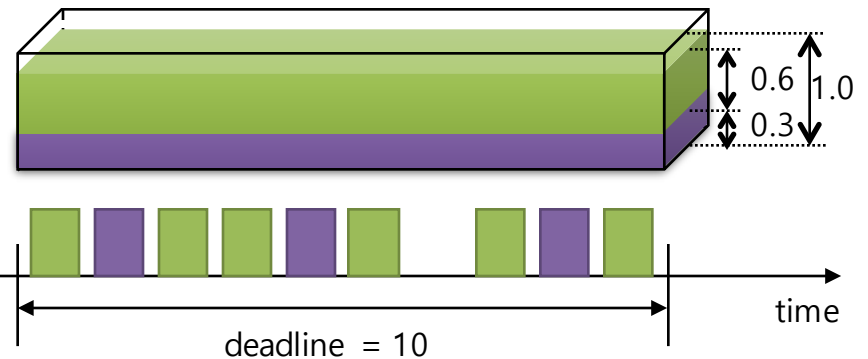
$$\text{density} = \text{WCET} / \text{deadline}$$

(WCET = Worst Case Execution Time)

Tasks

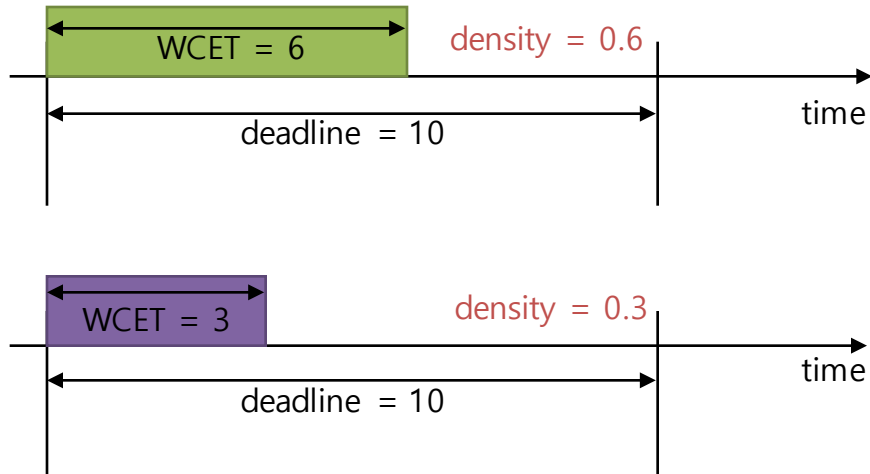


Fluid Scheduling

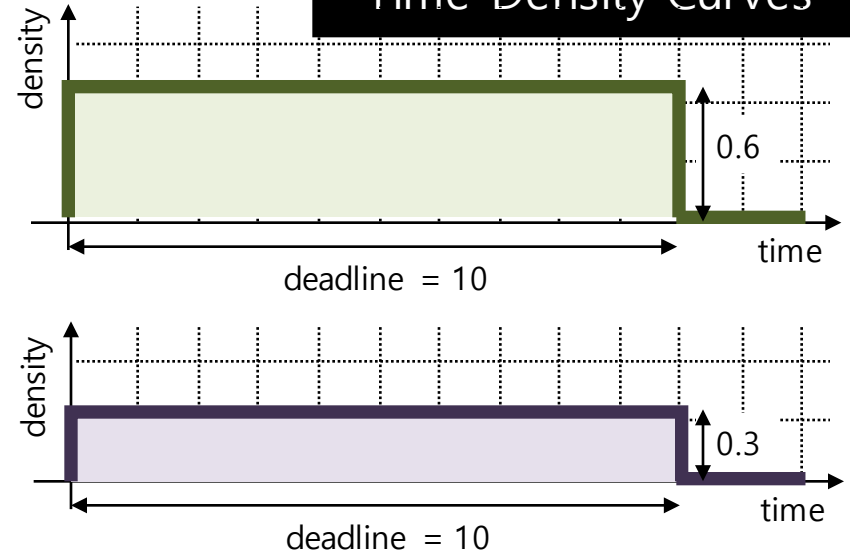


Schedulability of Fluid Schedule

Tasks



Time-Density Curves



Schedulability of Fluid Schedule

- Tasks are **schedulable**, if **sum of densities** of all active tasks is **smaller or equal to the number of processors** at any time instant



Research Goal

Maximize schedulability of
real-time multicore fluid scheduling



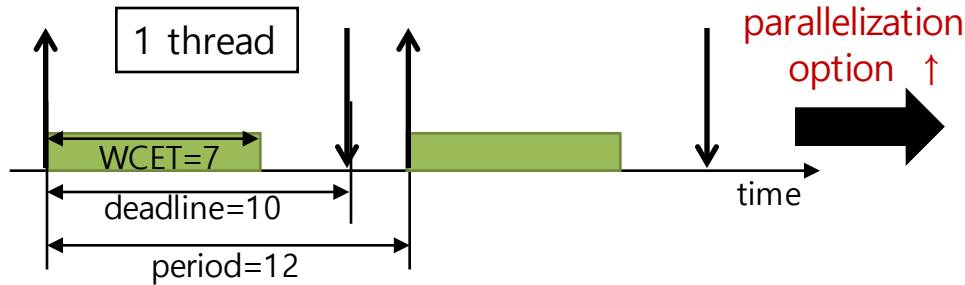
Minimize system peak density of
fluid scheduling

by controlling

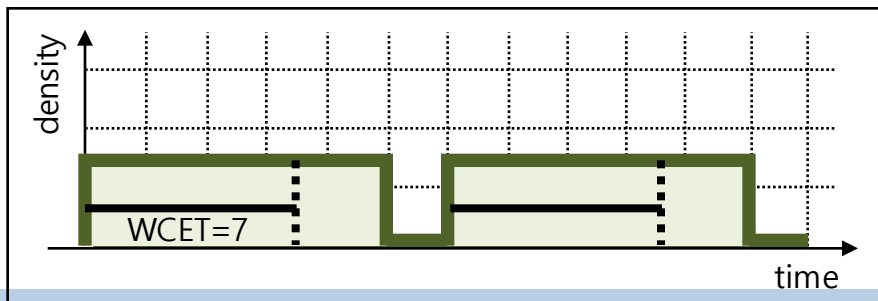
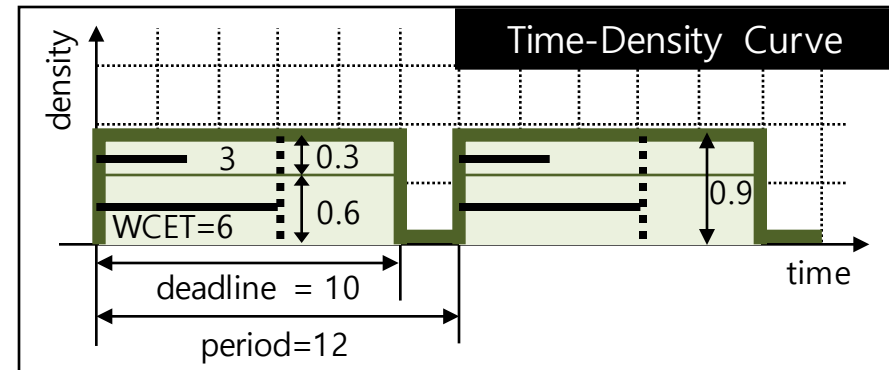
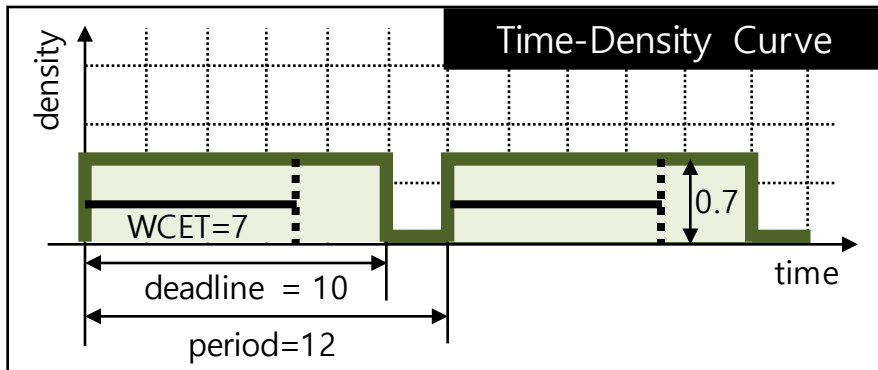
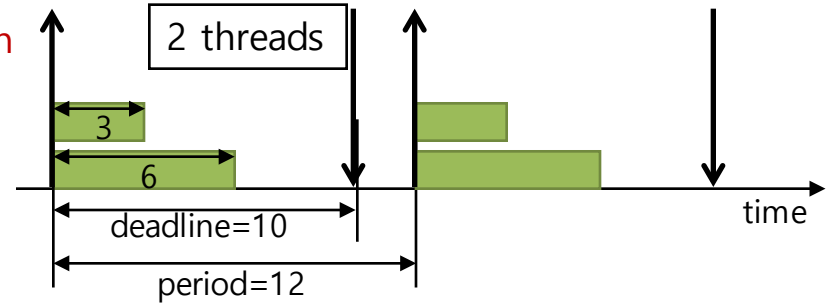
- 1) **parallelization option** (number of threads)
- 2) **artificial deadline** (shorter than original deadline)
- 3) **artificial period** (shorter than original period)
- 4) **task offset**

Open Problem 1: Time vs. Density Tradeoff

Artificial deadline control

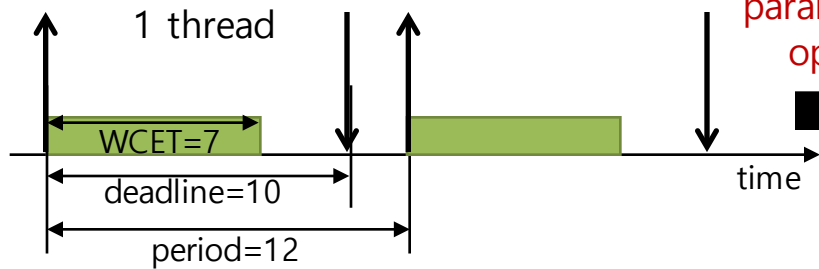


Parallelization option control

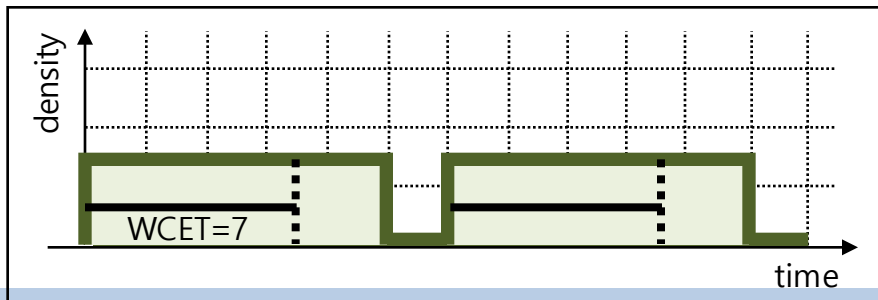
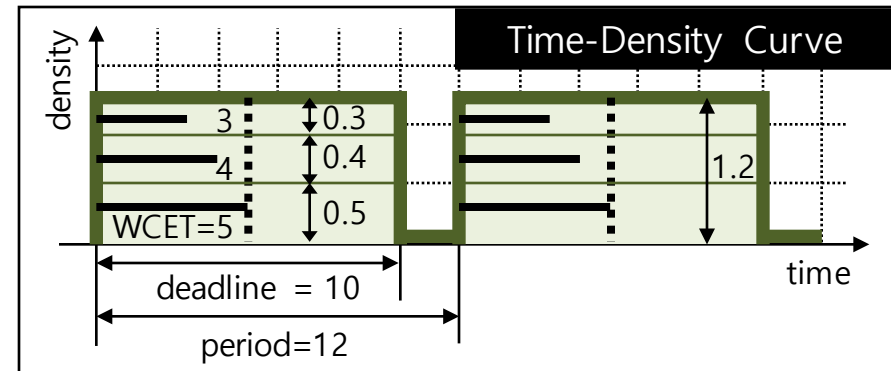
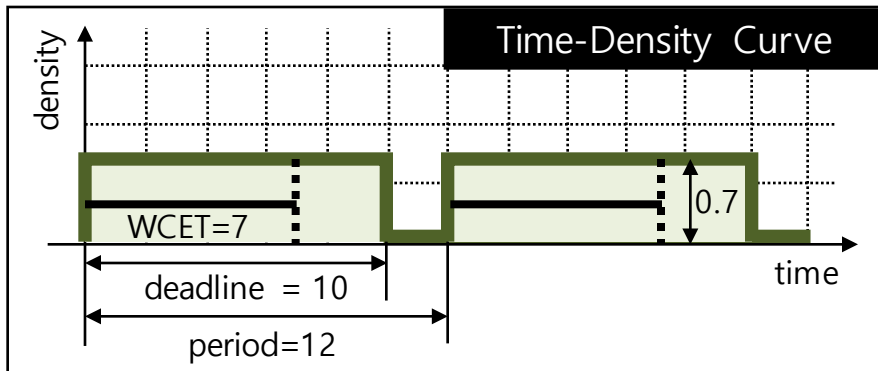
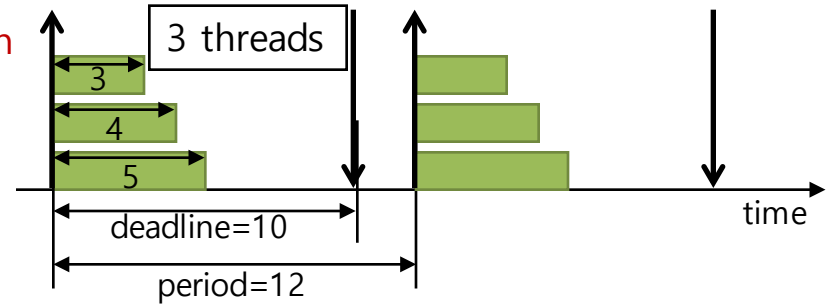


Open Problem 1: Time vs. Density Tradeoff

Artificial deadline control

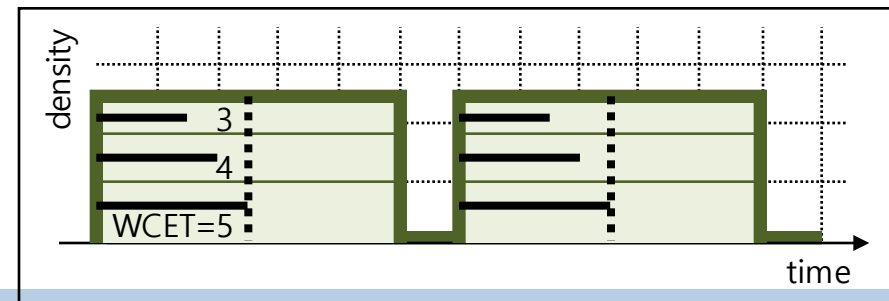
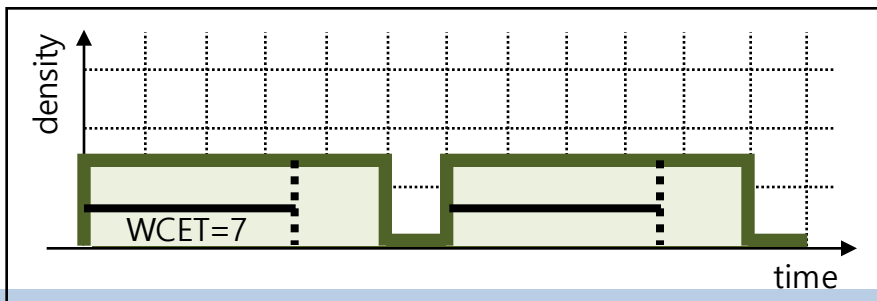
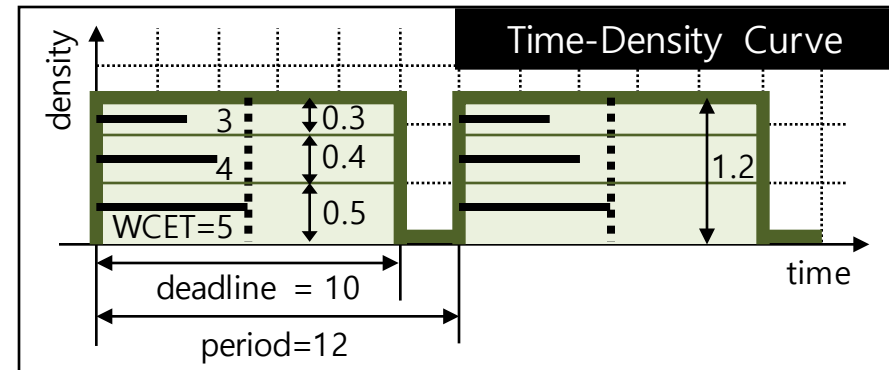
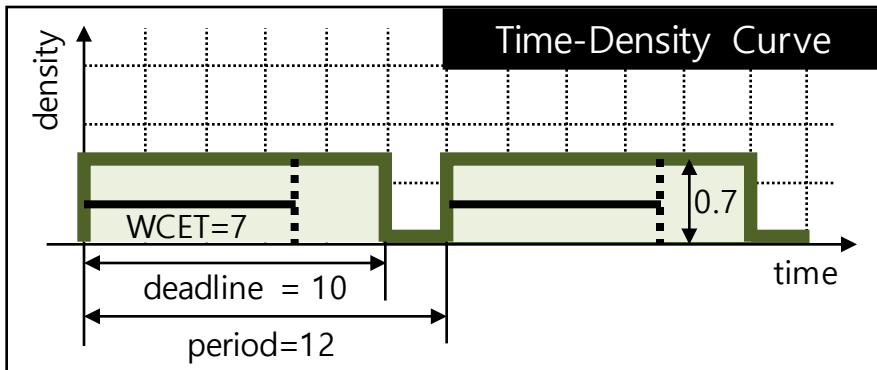
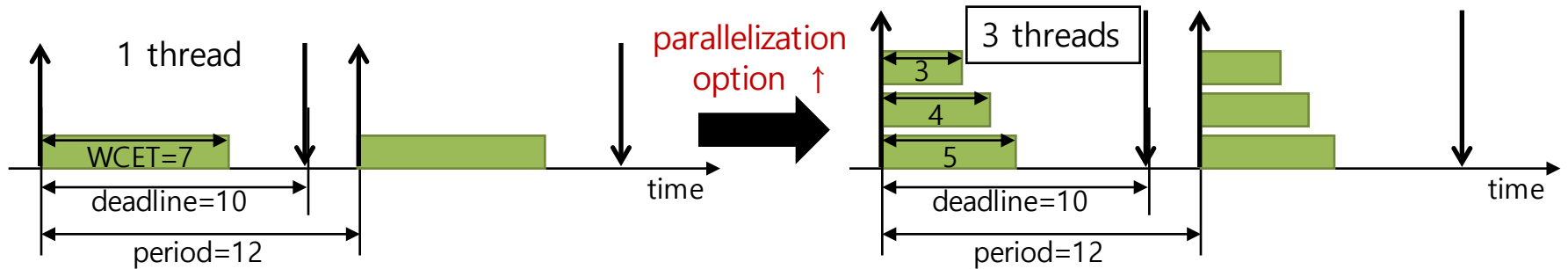


Parallelization option control



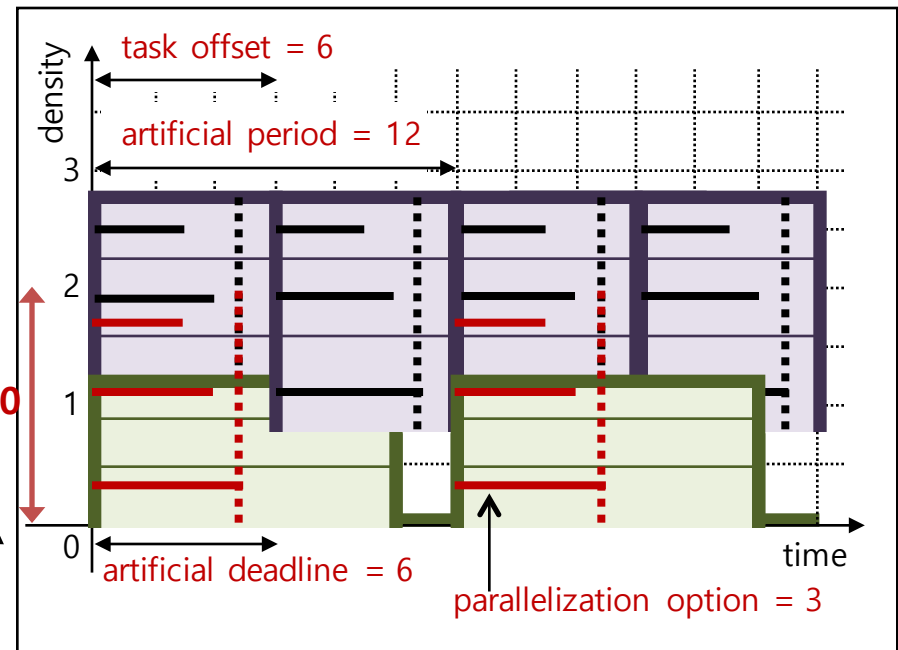
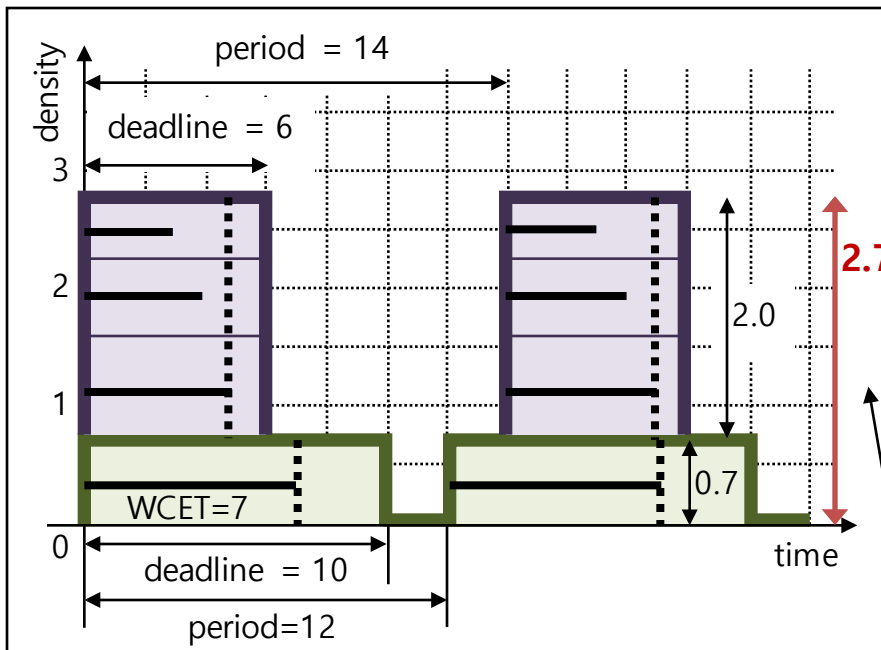
Open Problem 1: Time vs. Density Tradeoff

Artificial deadline and parallelization option control



Open Problem 2: System-wide Tradeoff?

artificial deadline and parallelization option
+
artificial period and task offset control



System peak density

Problem Formulation (1 / 2)

System with M homogeneous CPU cores,
 N parallelizable periodic tasks

$$\tau_i = (P_i, D_i, C_i(O_i))$$

P_i : original period



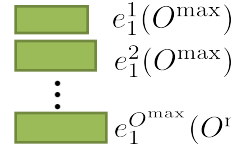
D_i : original deadline

O_i : parallelization option

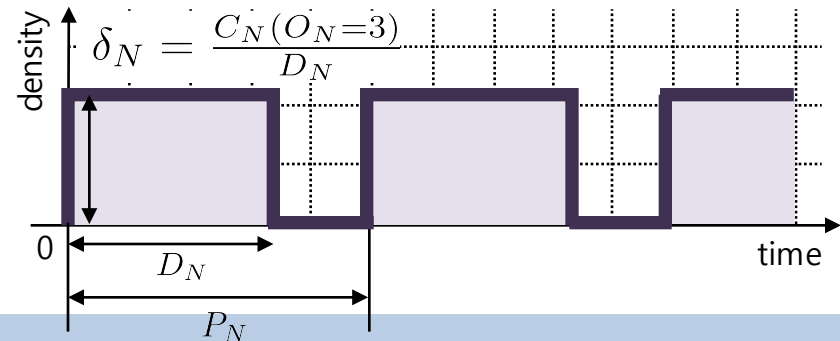
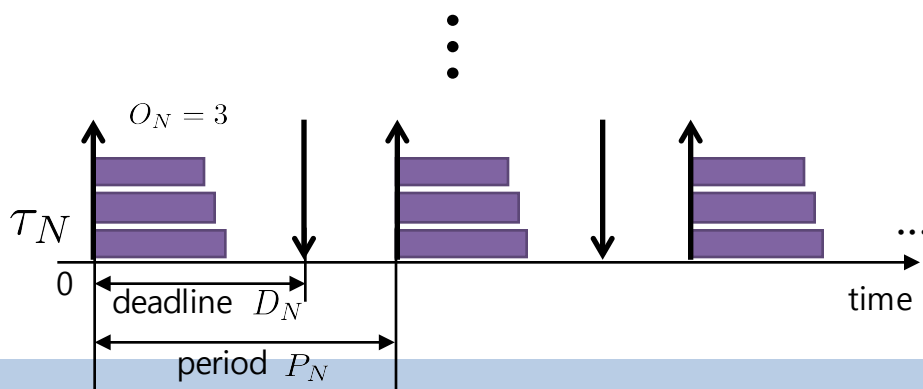
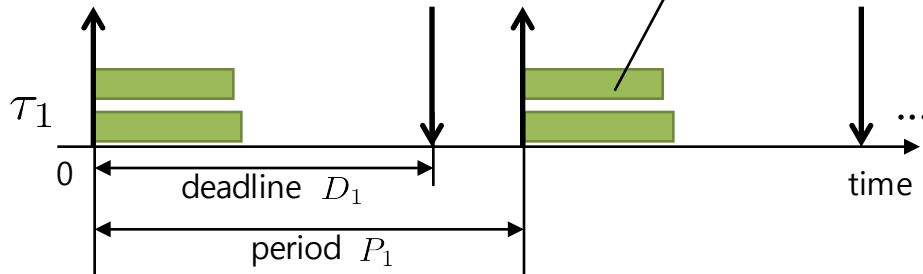
$e_i^k(O_i)$: WCET of k -th thread

when parallelized into O_i threads

$C_i(O_i)$: total computation amount

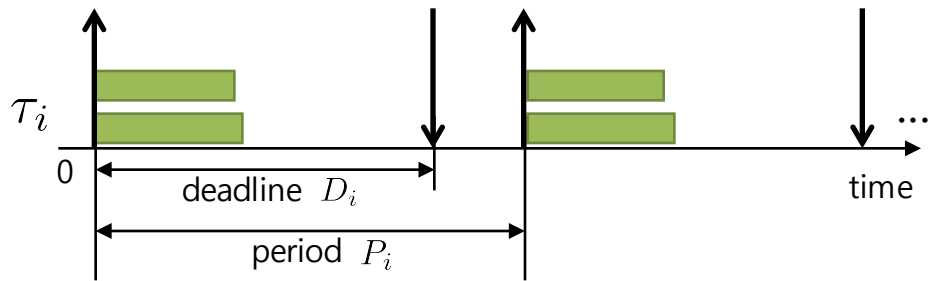
$O_1 = 1$	 $e_1^1(1) = C_1(1)$	} $C_1(2)$
$O_1 = 2$		
\vdots	\vdots	} $C_1(O_{\max})$
$O_1 = O_{\max}$		

Parallelizable Periodic Tasks



Problem Formulation (2 / 2)

Four control parameters

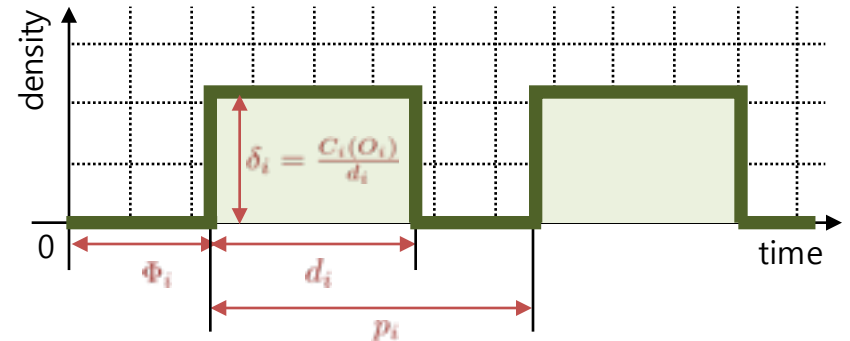
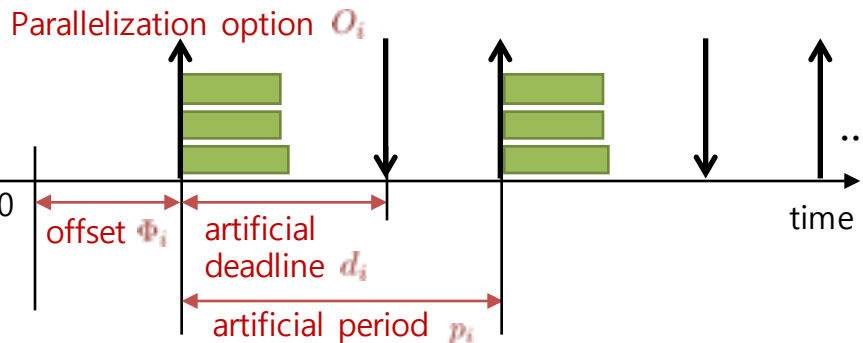


d_i : artificial deadline ($d_i < D_i$)

O_i : parallelization option

p_i : artificial period ($p_i < P_i$)

Φ_i : task offset



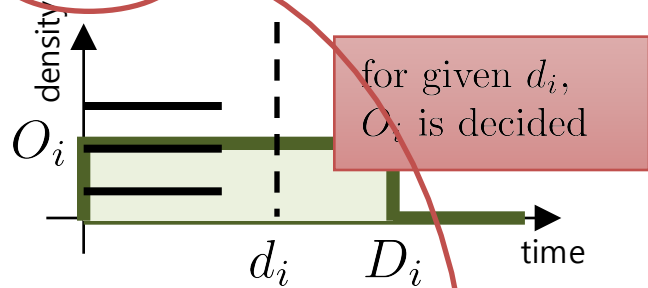
$$\delta_i((\Phi_i, O_i, d_i, p_i), t) = \begin{cases} C_i(O_i)/d_i & (t - \Phi_i) \bmod p_i \leq d_i \\ 0 & (t - \Phi_i) \bmod p_i > d_i \end{cases}$$

$$\text{minimize} \quad \max_{0 \leq t < HP} \sum_{i=1}^N \delta_i((\Phi_i, O_i, d_i, p_i), t)$$

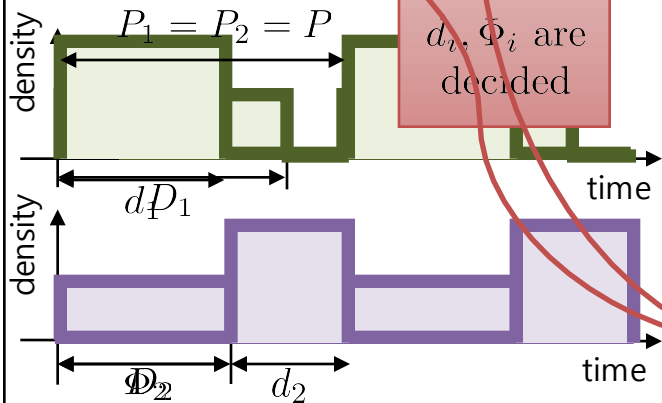
Preliminary Solution

3-step approach

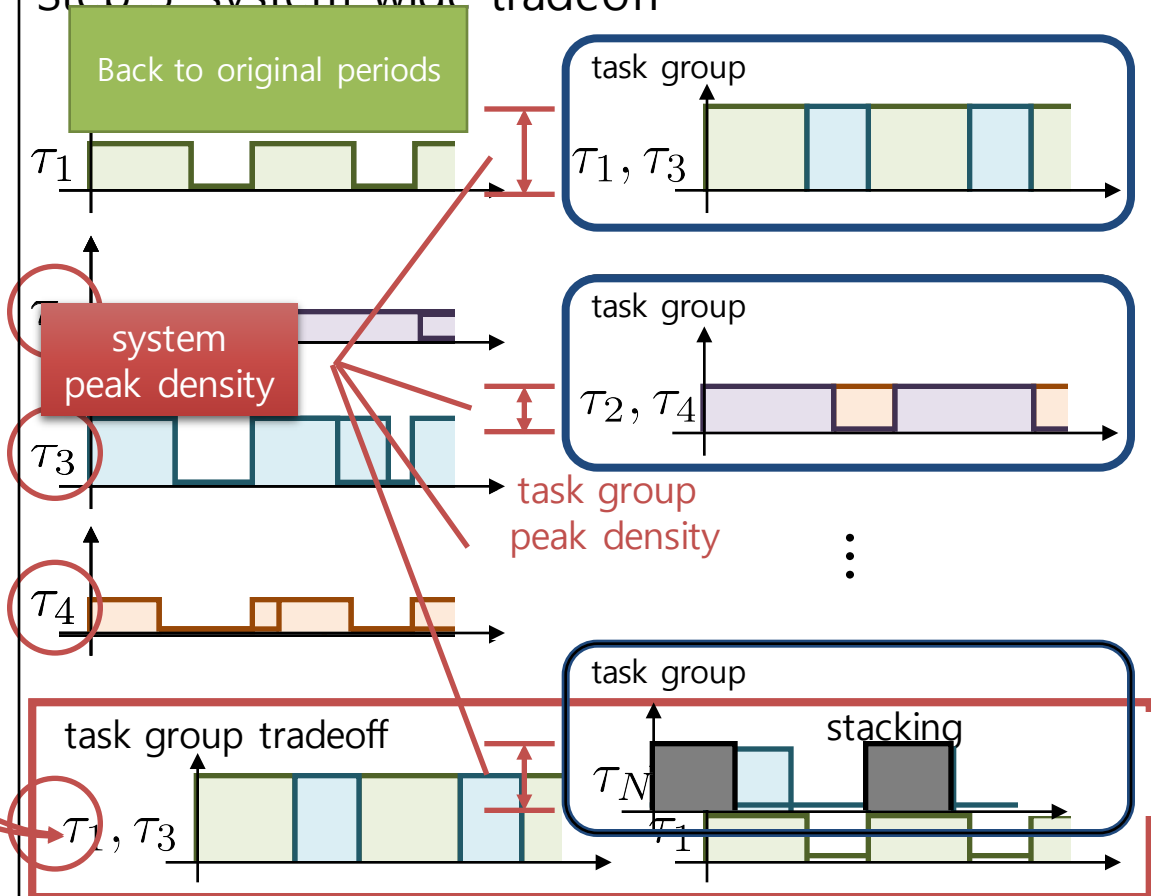
Step 1. per-task tradeoff



Step 2. tradeoff of task group with same period



Step 3. system-wide tradeoff



Simulation Result

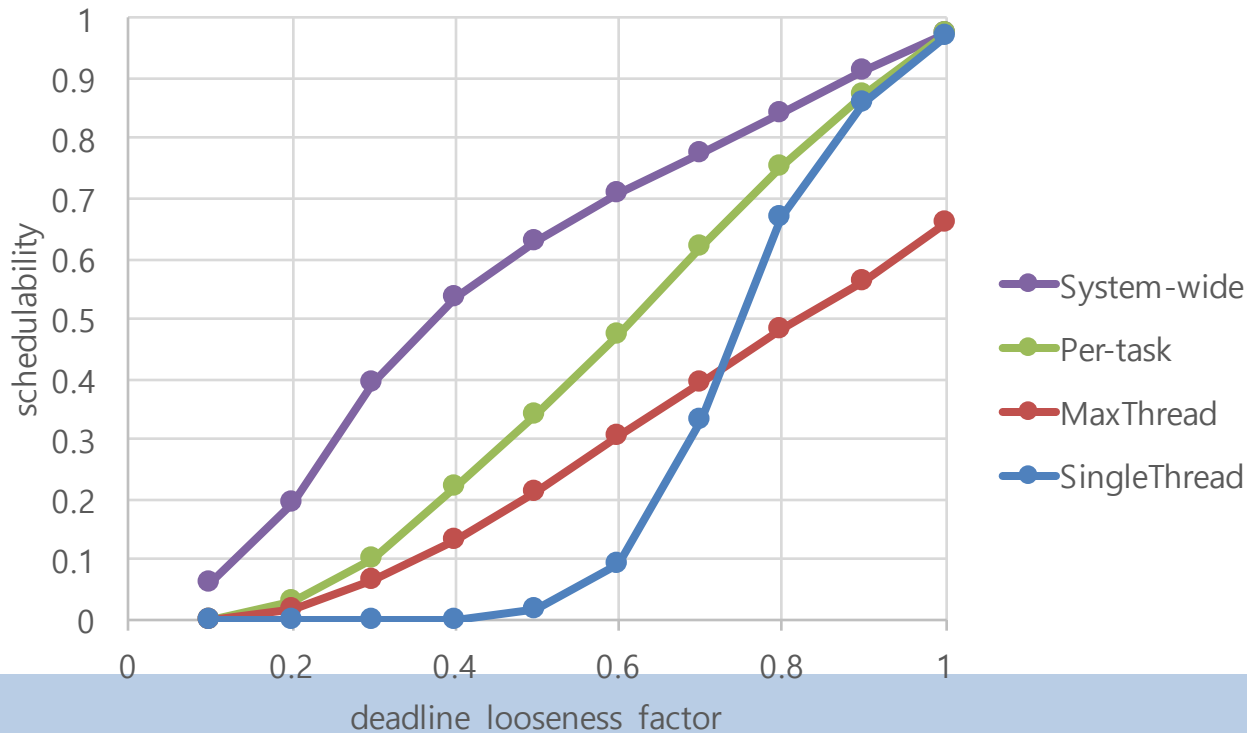
Simulation Environment

1000 task sets

$N = [3, 15]$

$M = 8$

deadline looseness factor = deadline / period



Remaining Issues

- Considering Inter-core Memory Interference
- Complicated Task Model
 - Multi-segment task model
 - Fork-join task model
- Tradeoff in G-EDF

<https://github.com/rubis-lab/RealTimeTaskSimulator>

Thank you